

Correlations of Heavy Flavor Electrons in Au+Au & p+p Collisions in PHENIX

Anne M. Sickles
January 25, 2011

PHENIX arXiv:1011.1477

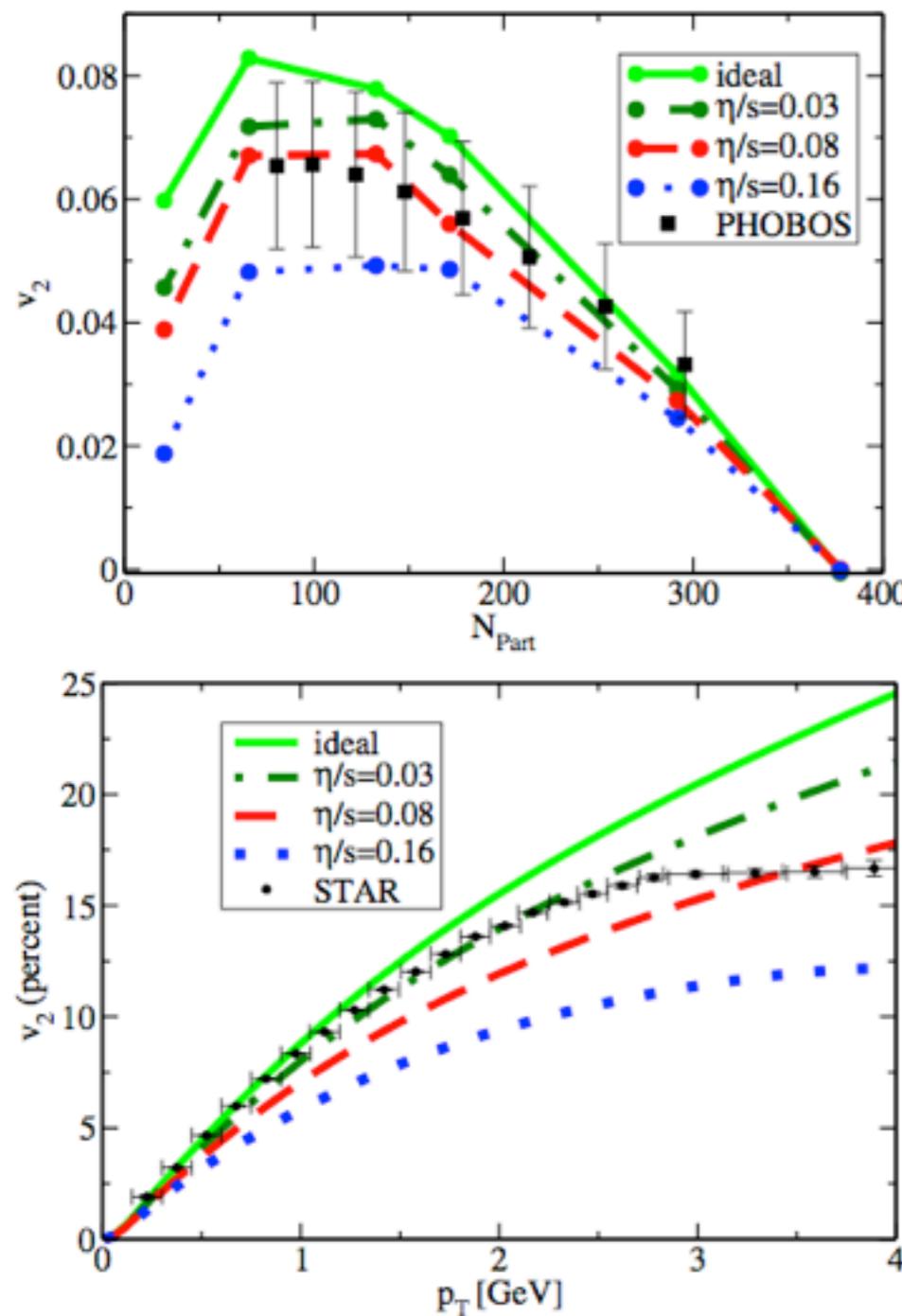


why heavy ion collisions?

- what happens to dense QCD matter at extremely high temperature?

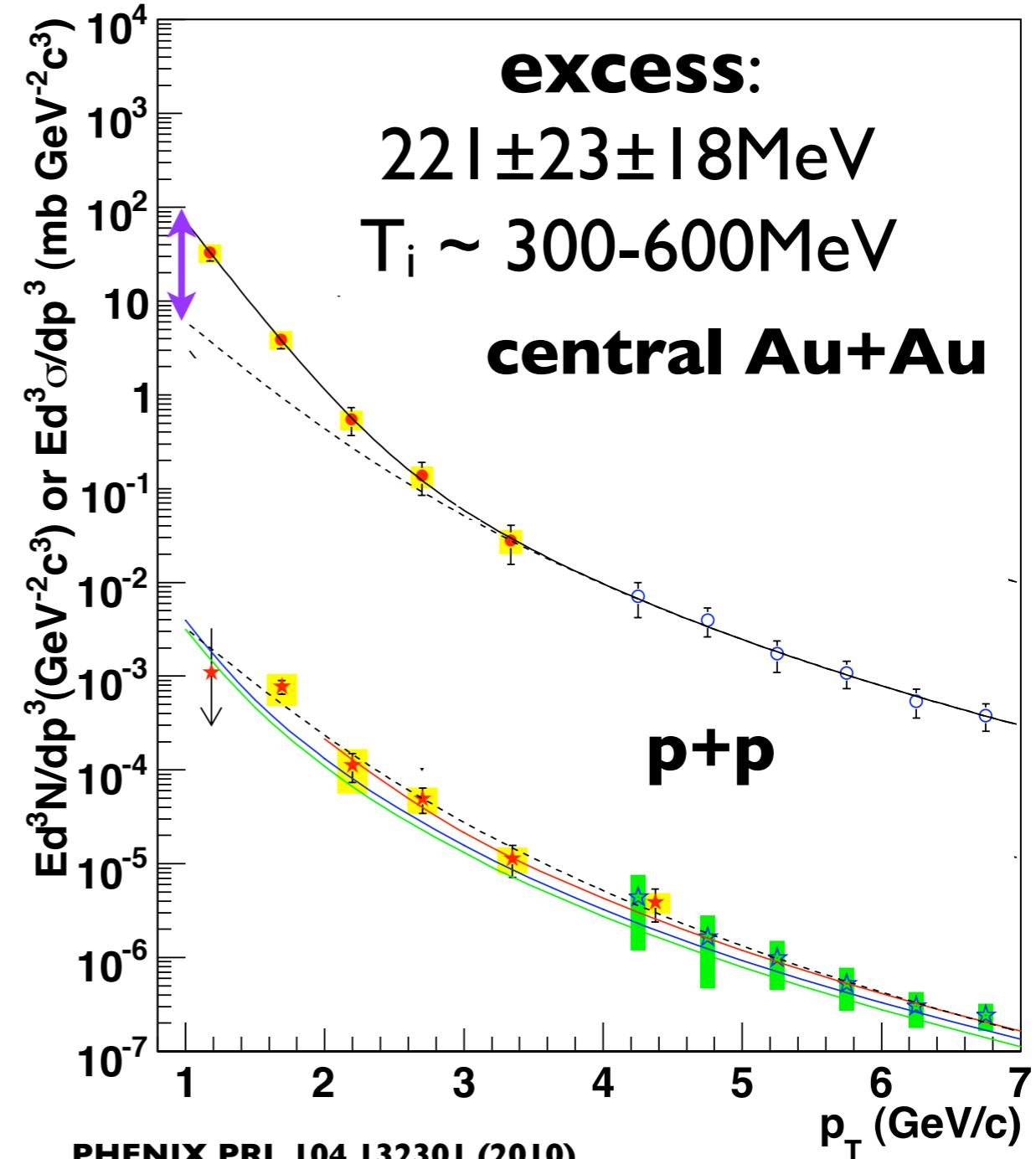


hot nuclear matter



Romatschke & Romatschke PRL 99 172301 (2007)

Direct γ^* (via e^+e^-)

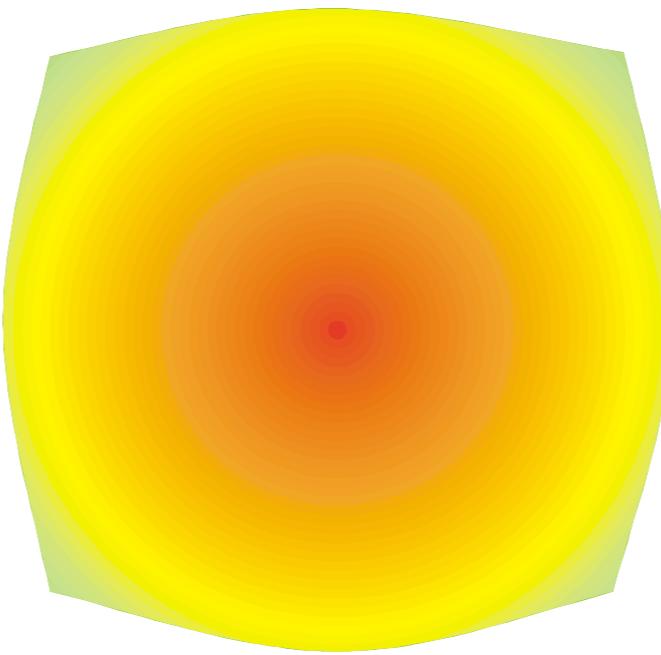


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BNL Nucl. Phys. Seminar

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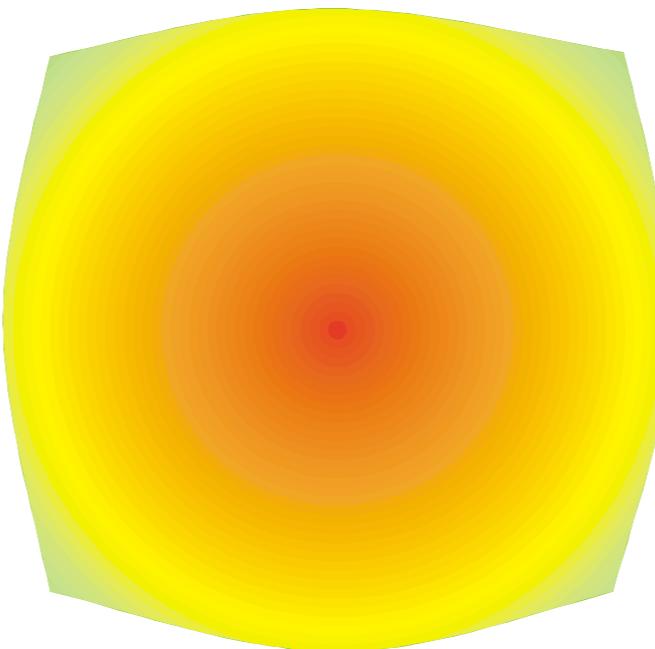
What is our goal?



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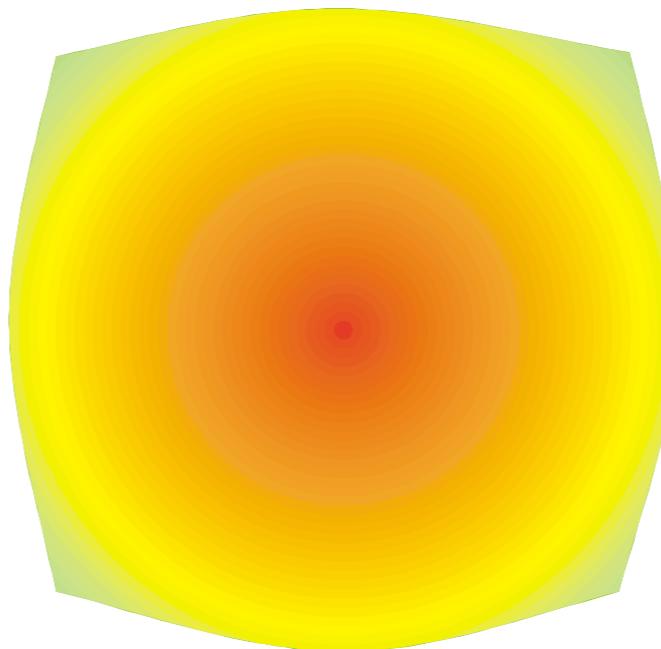
partoni(E)



What is our goal?



partoni(E)

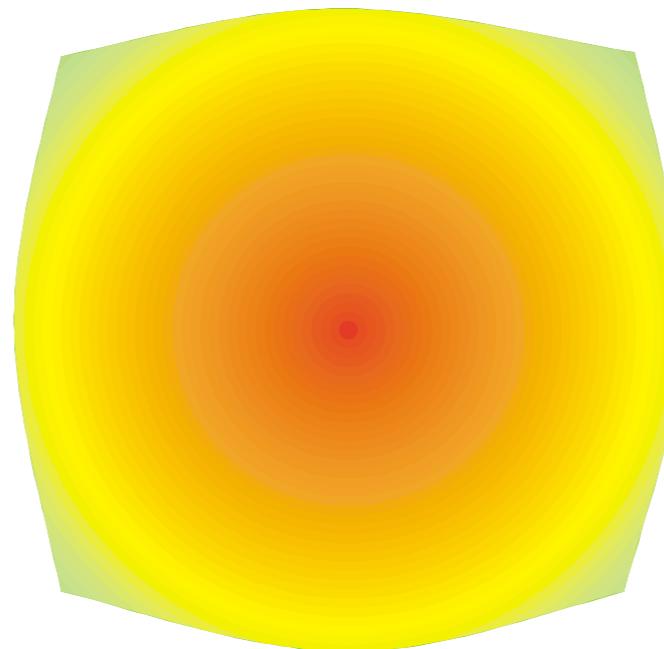


?

What is our goal?



parton_i(E)



- determine the mechanism(s) of energy loss
- determine the strength of the interactions

reality more complicated

$\xrightarrow{\hspace{1cm}}$
parton_i(E)

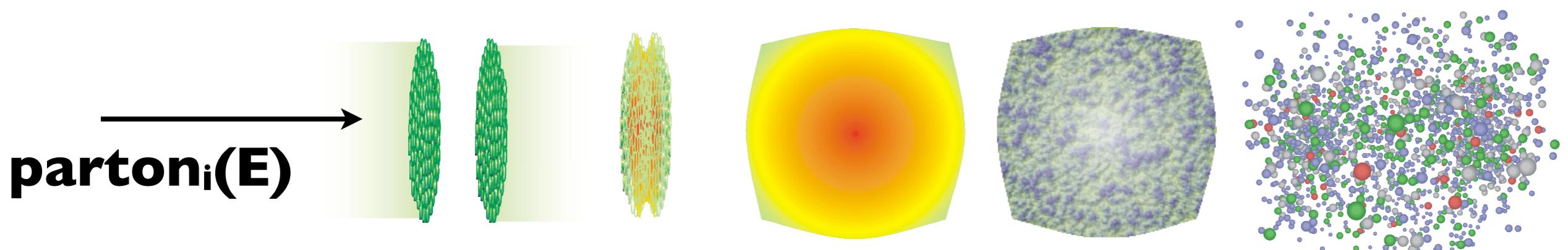
reality more complicated

geometry, initial state effects, time evolution,
fragmentation, flow of various kinds

$\xrightarrow{\hspace{1cm}}$
parton_i(E)

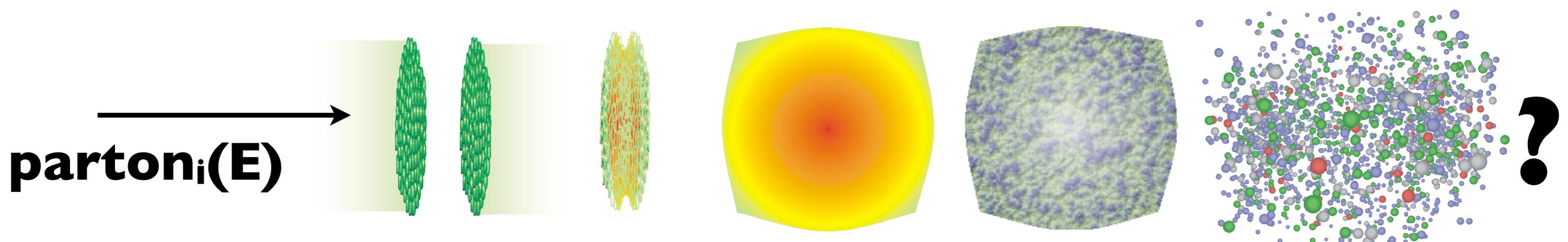
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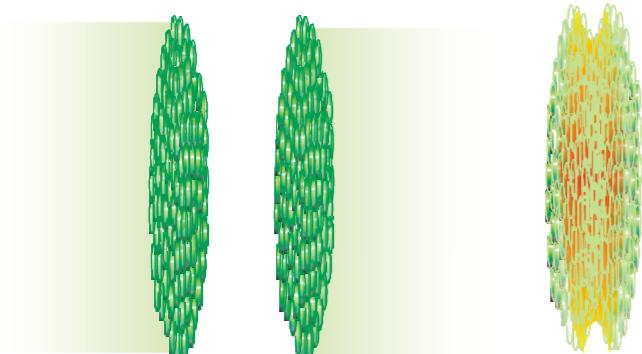
geometry, initial state effects, time evolution,
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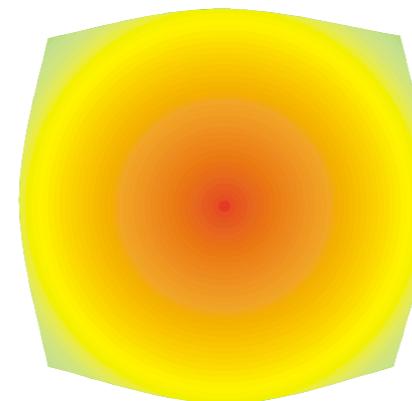
approaching realistic models

initial conditions

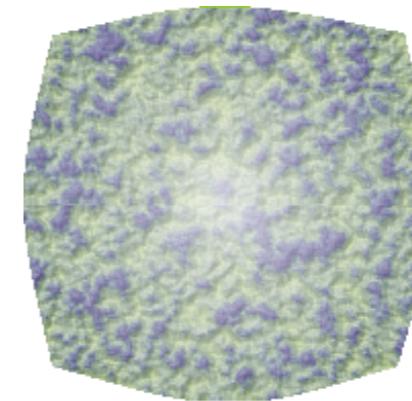
**Glauber
CGC**



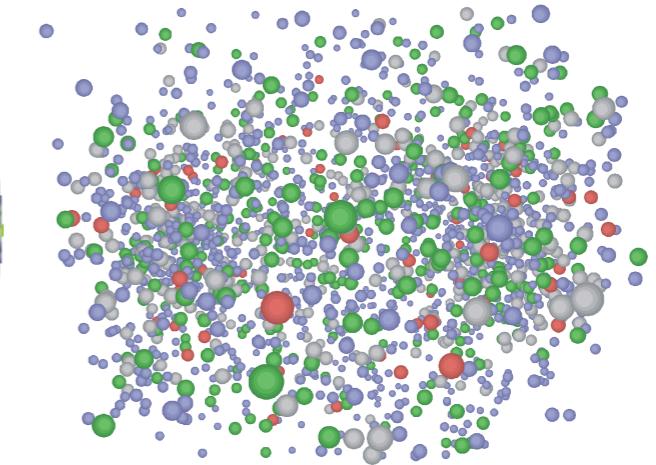
sQGP



pre-equilibrium



freeze out



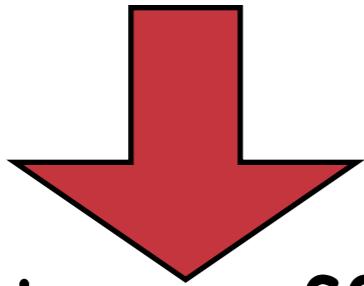
hadronization

any colored probe interacts in all phases of the collision!

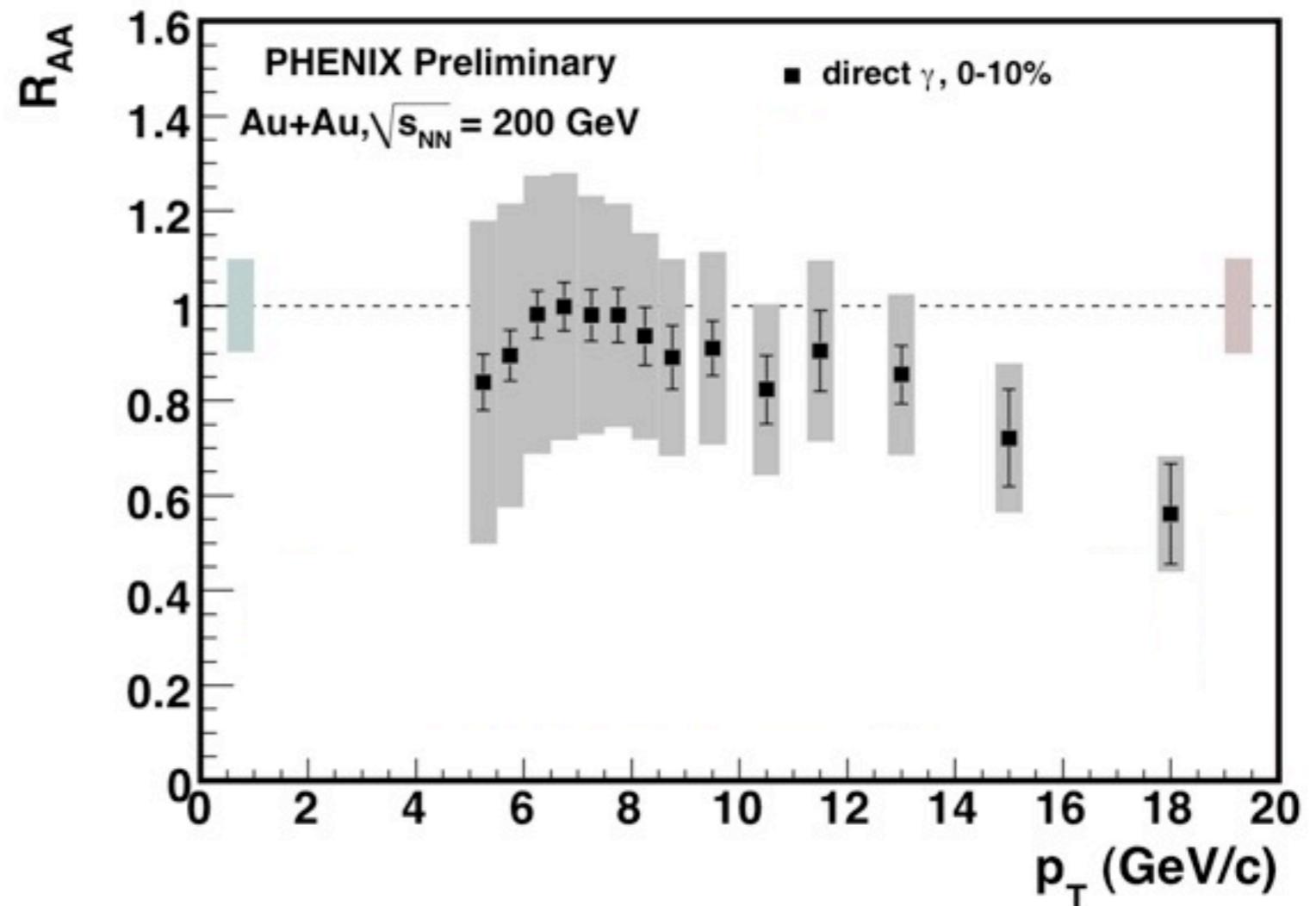
γ : control measurement

$$R_{AA} = \frac{\text{yield}_{AA}}{\text{yield}_{pp} * N_{\text{coll}}}$$

$$R_{AA} = 1$$



no nuclear effects

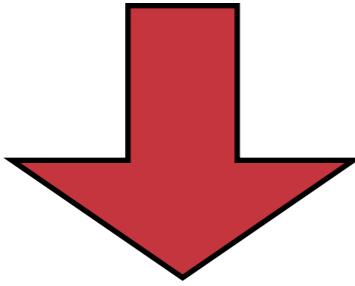


γ : no color charge \rightarrow insensitive to produced matter
 $R_{AA}(p_T < 14 \text{ GeV}/c)$ consistent with unity

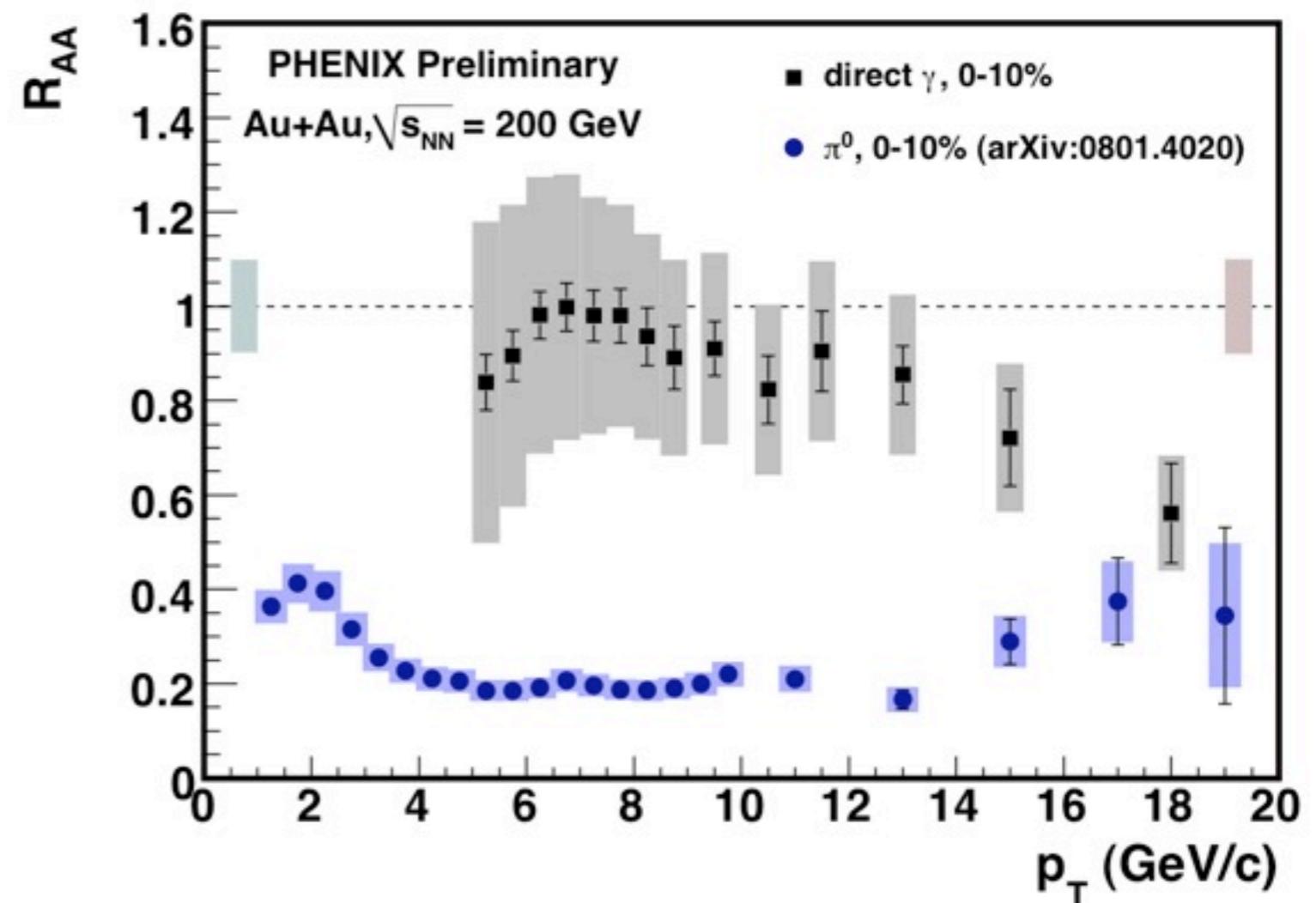
π^0 RAA

$$R_{AA} = \frac{yield_{AA}}{yield_{pp} * N_{coll}}$$

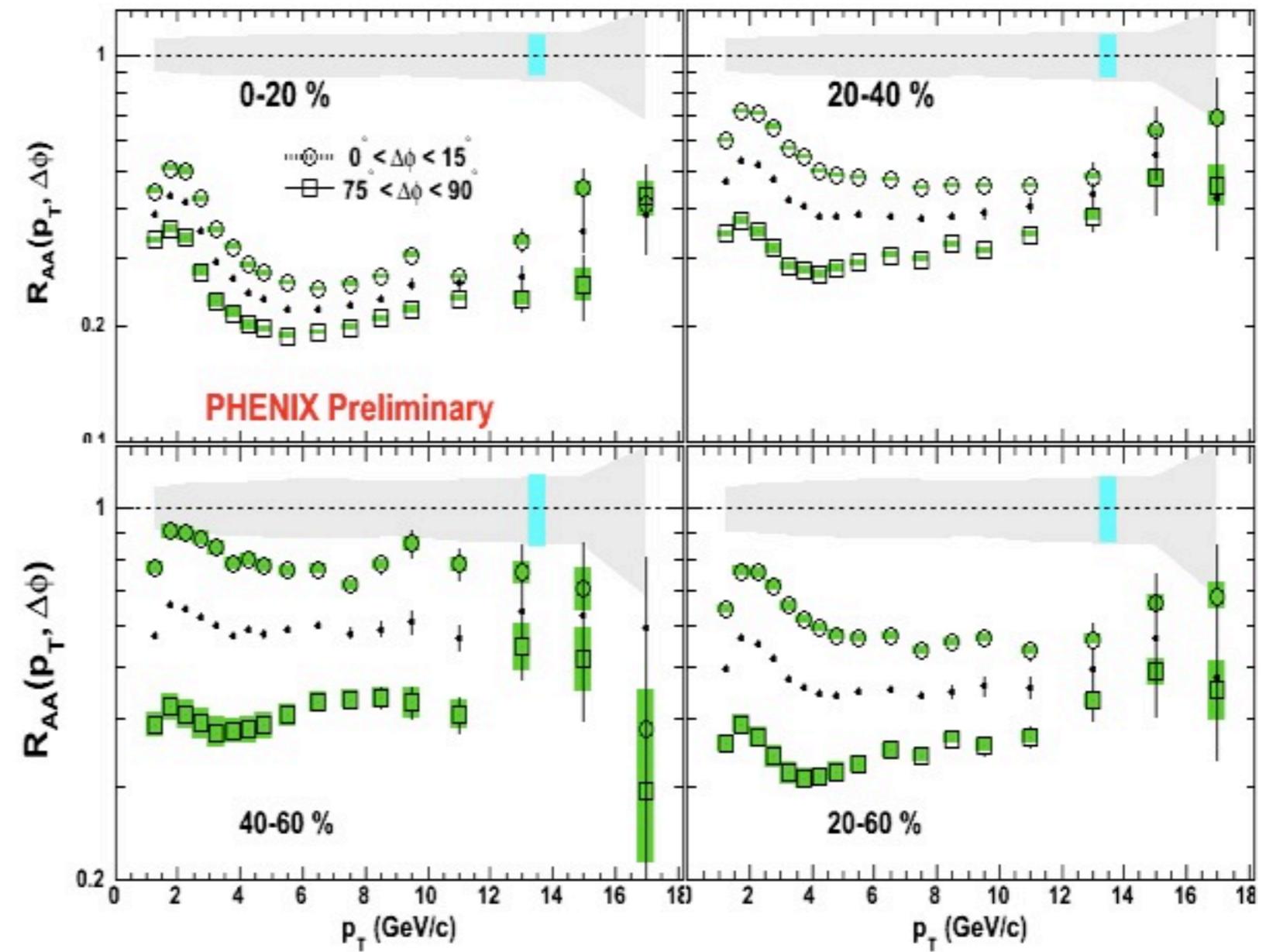
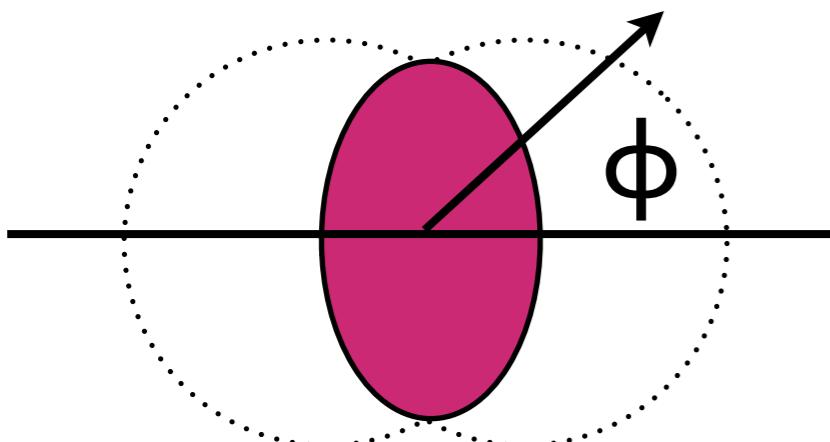
$R_{AA} \ll 1$



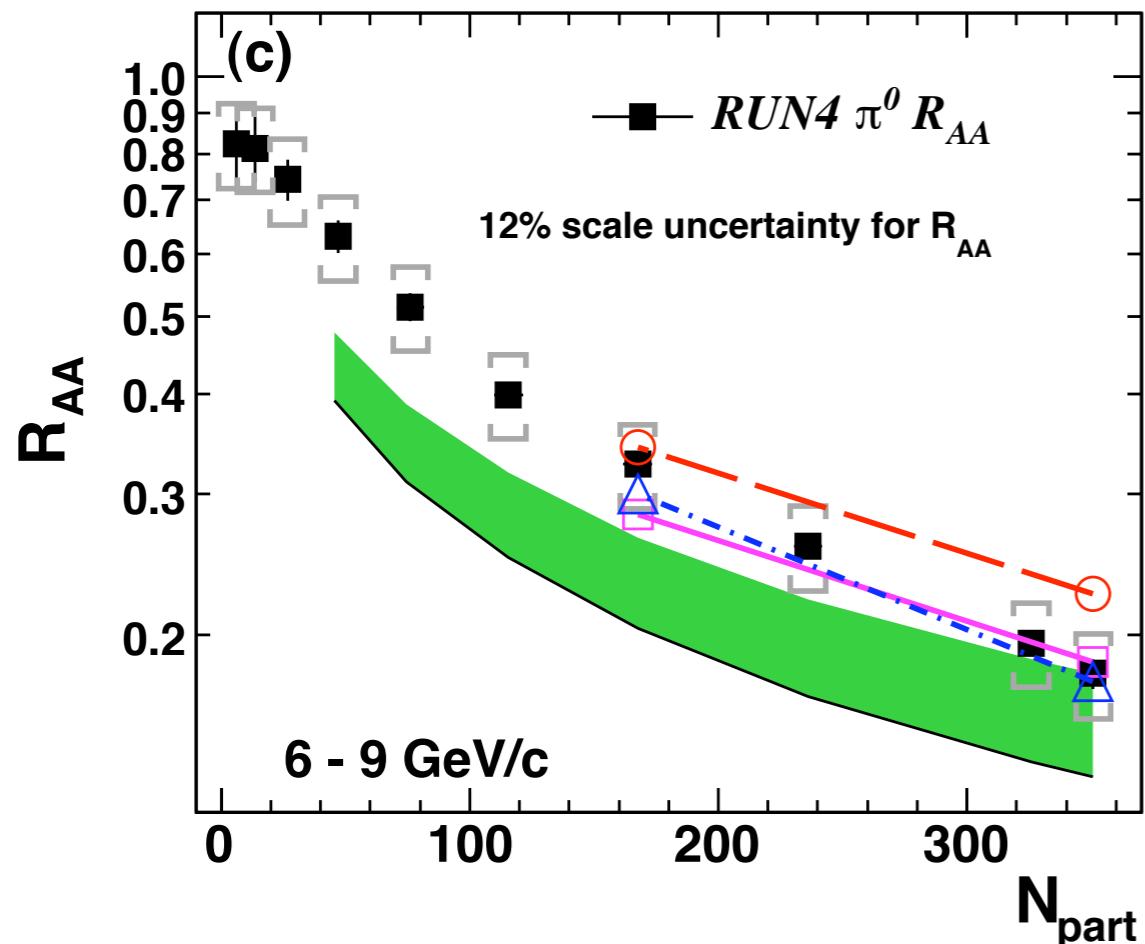
parton energy loss



path length dependence to R_{AA}

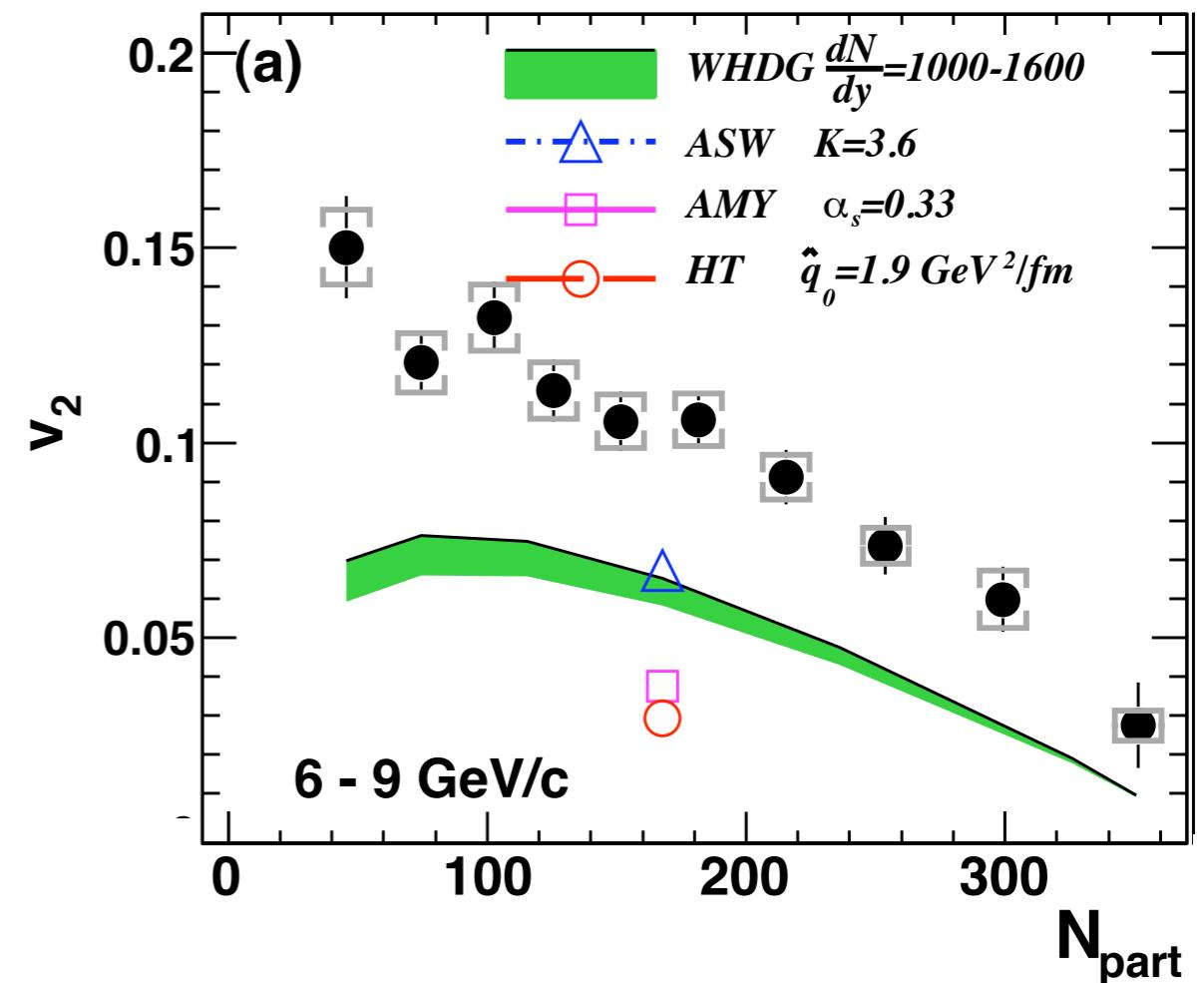
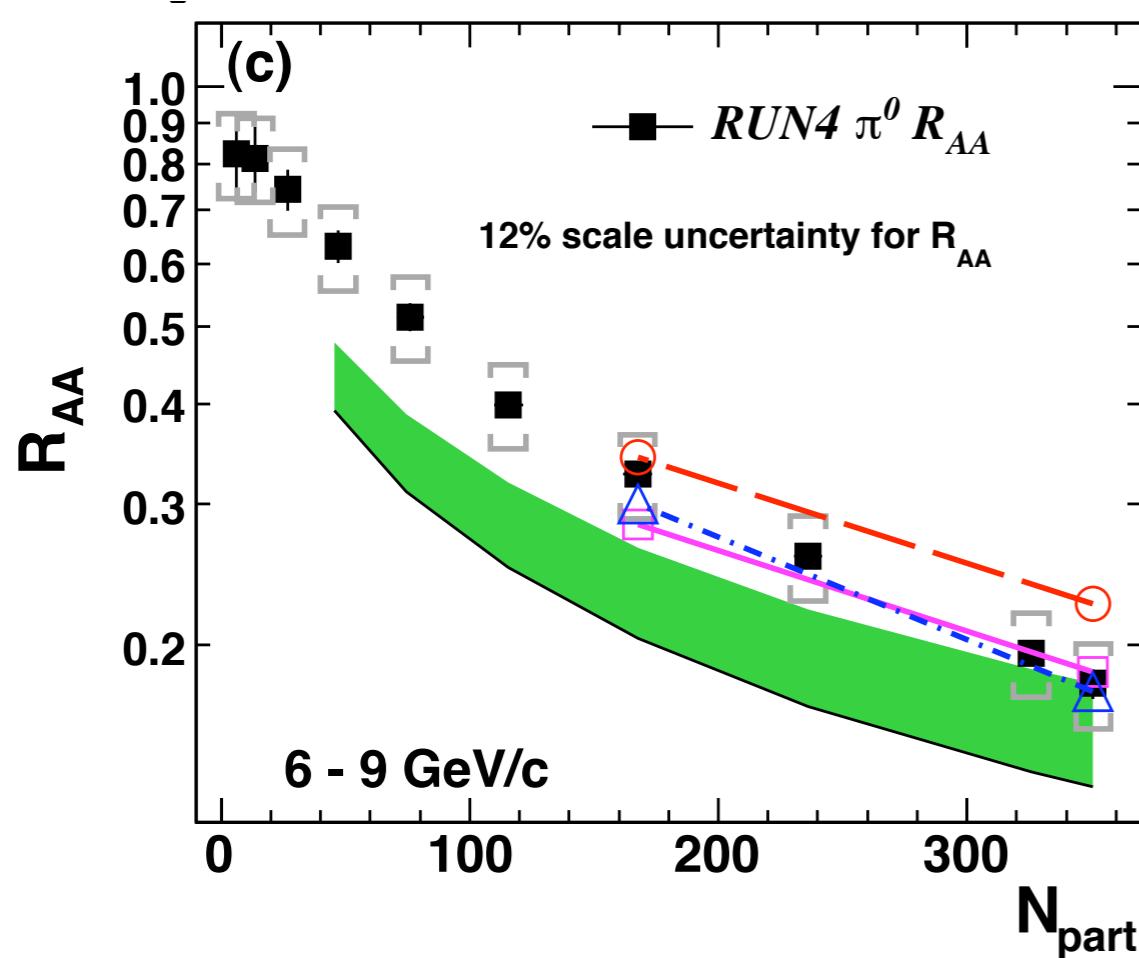


models which get R_{AA} right...



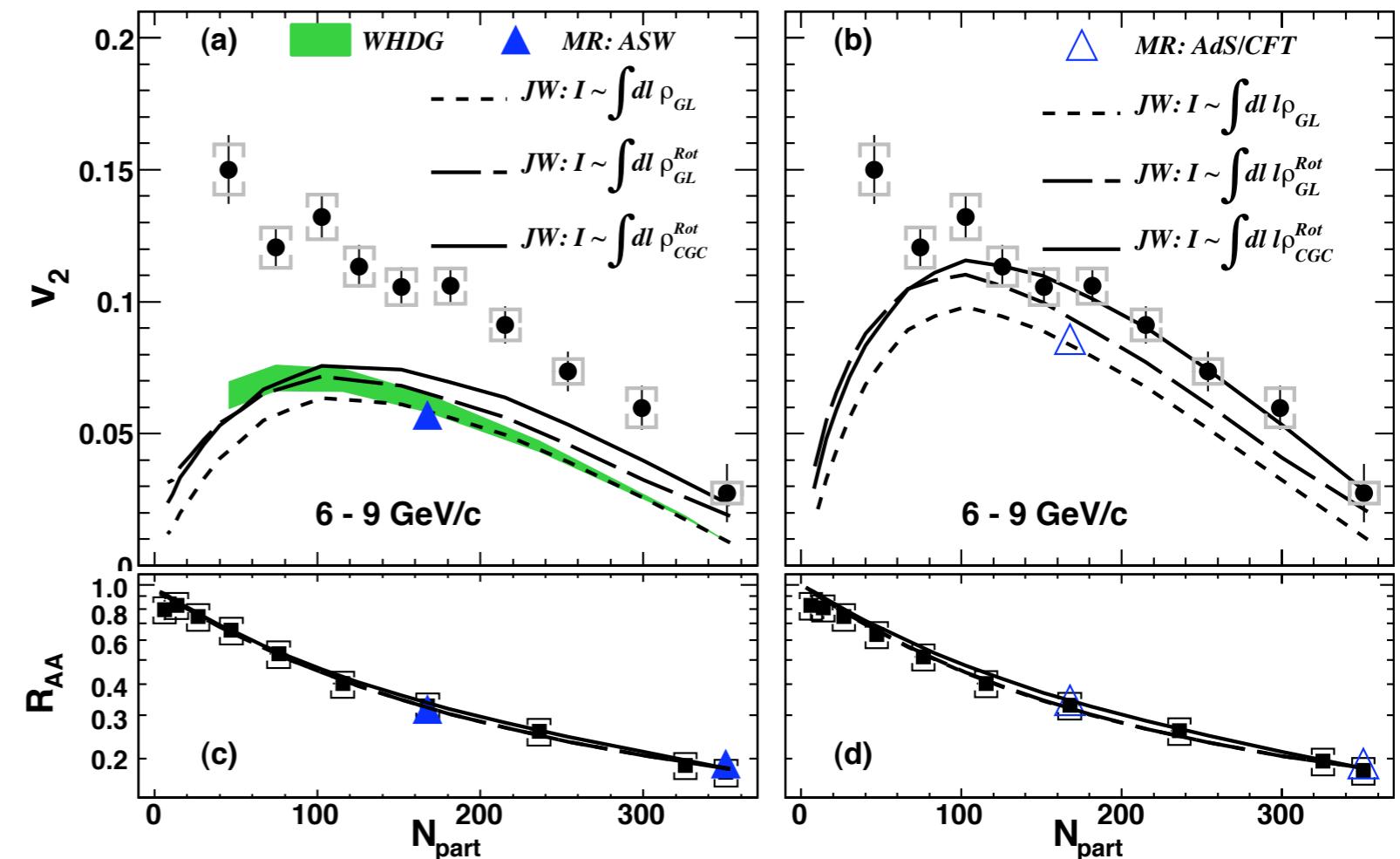
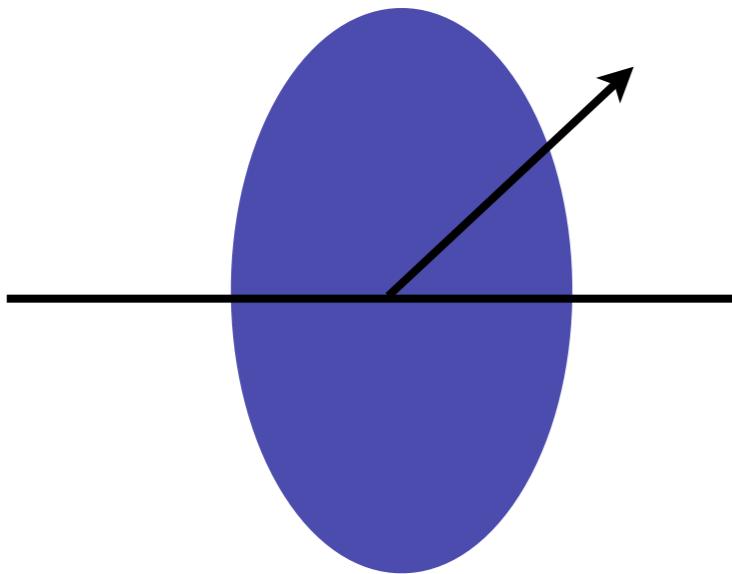
PHENIX PRL 105 142301 (2010)

models which get R_{AA} right...



...under predict v_2

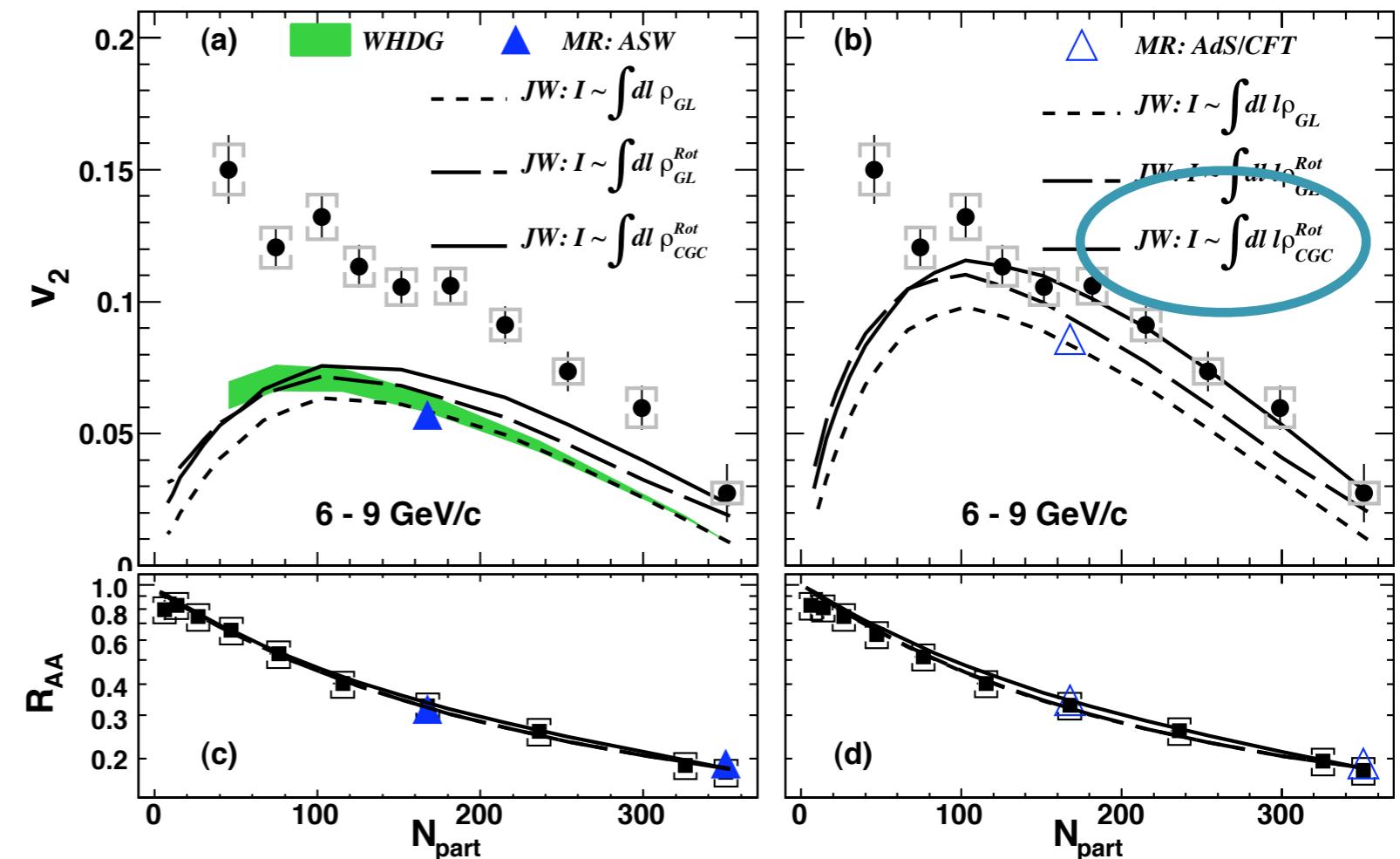
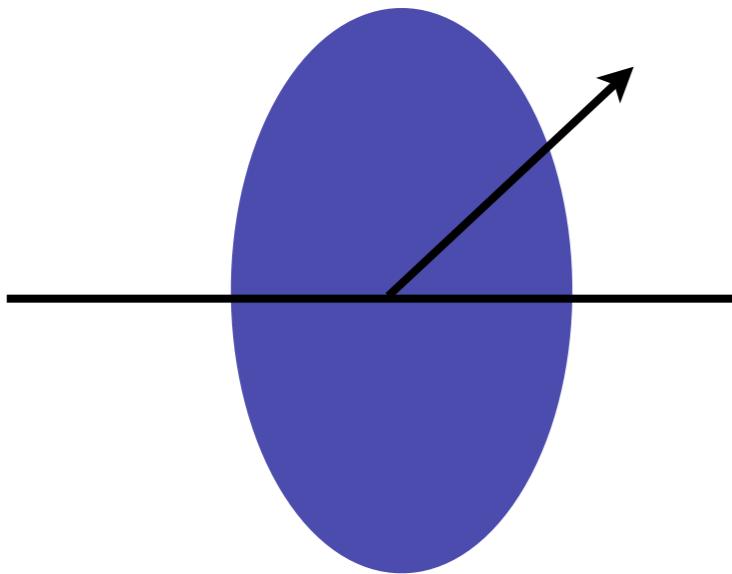
reaction plane: a closer look



points to very strong path length dependence

PHENIX PRL 105 142301 (2010)

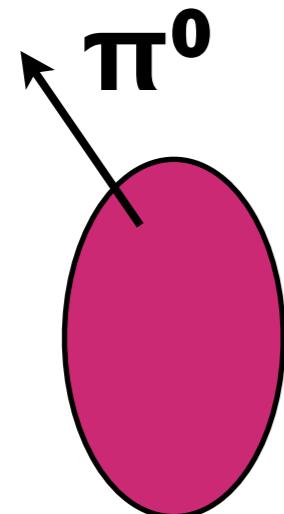
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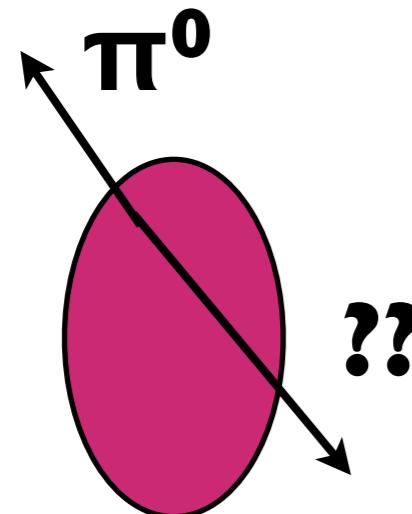
PHENIX PRL 105 142301 (2010)

I_{AA} : di-jet suppression



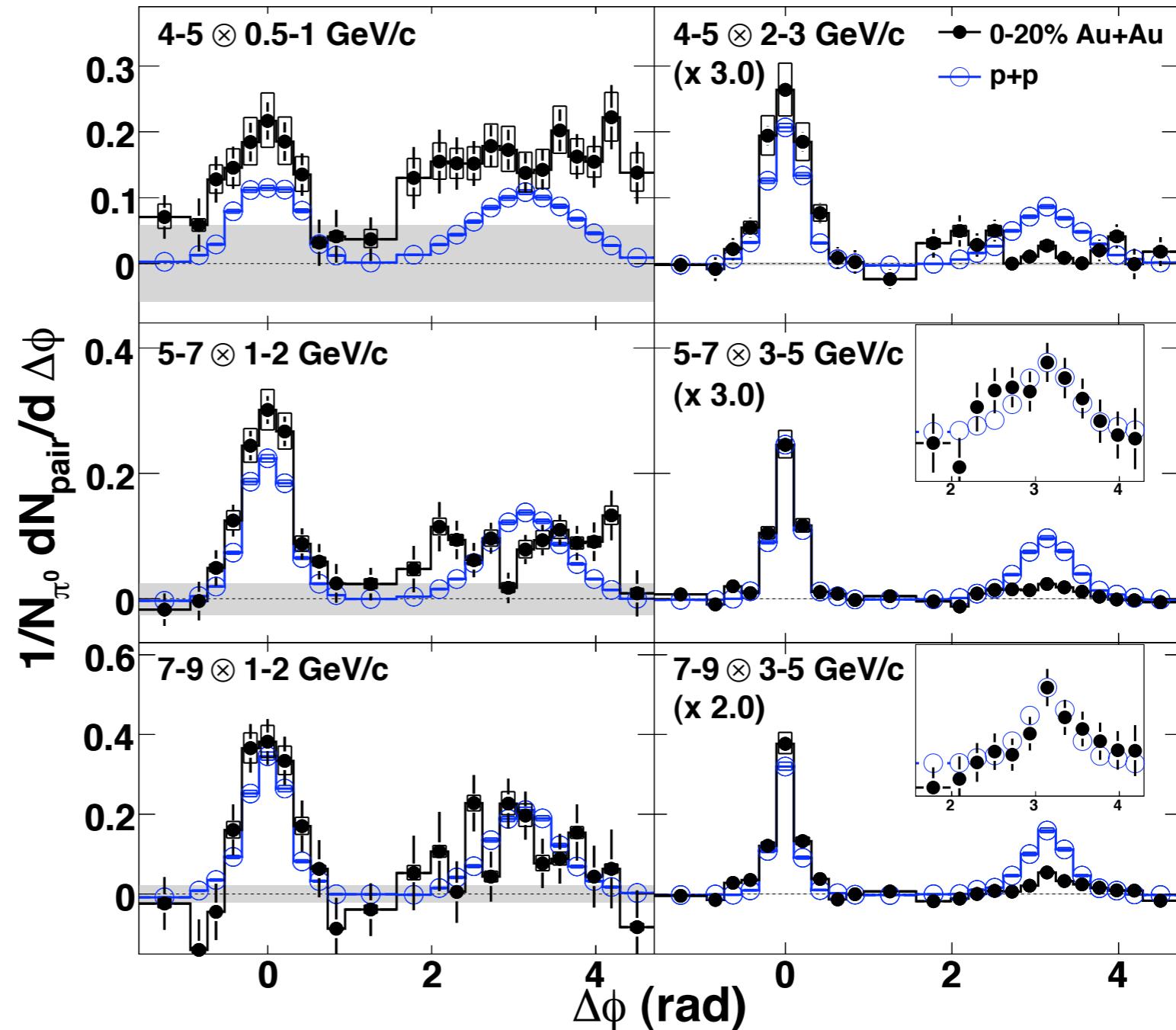
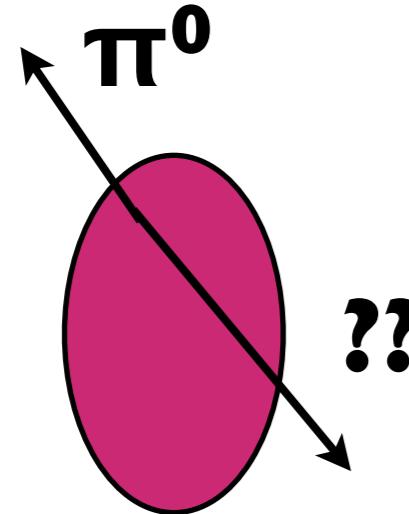
PHENIX PRL 104 252301 (2010)

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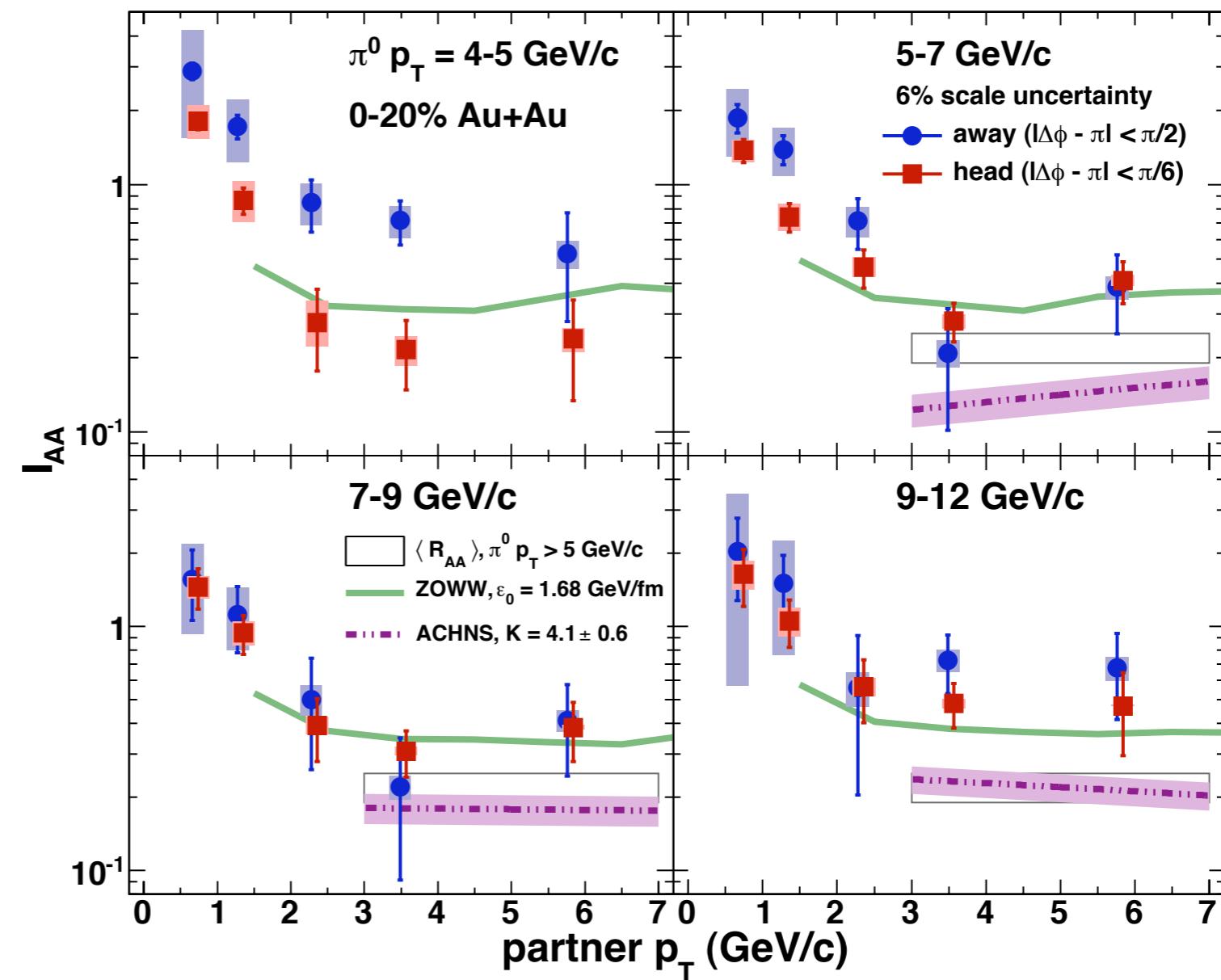
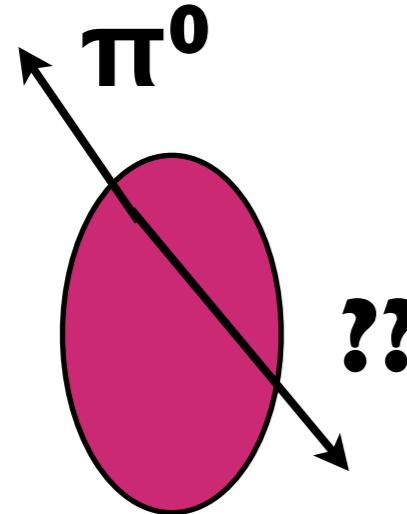


PHENIX PRL 104 252301 (2010)

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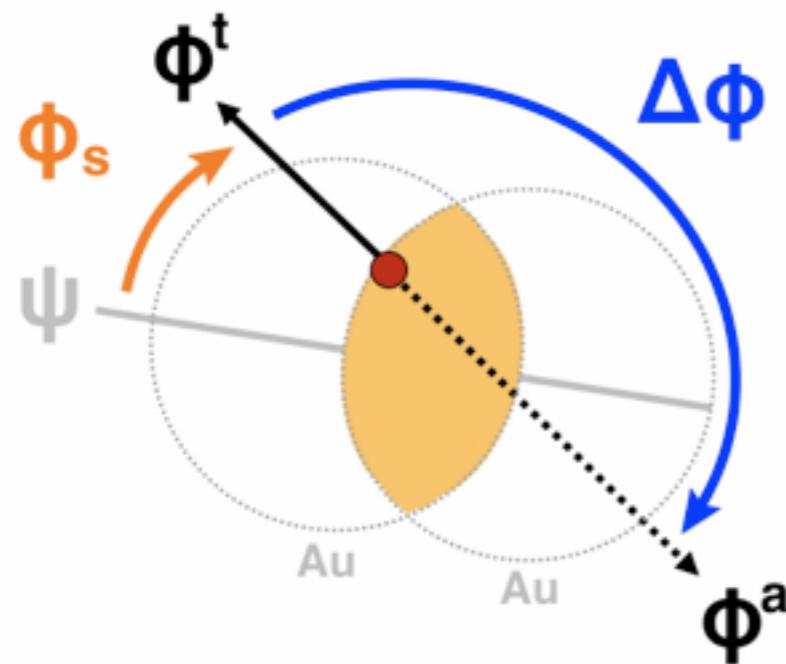


PHENIX PRL 104 252301 (2010)



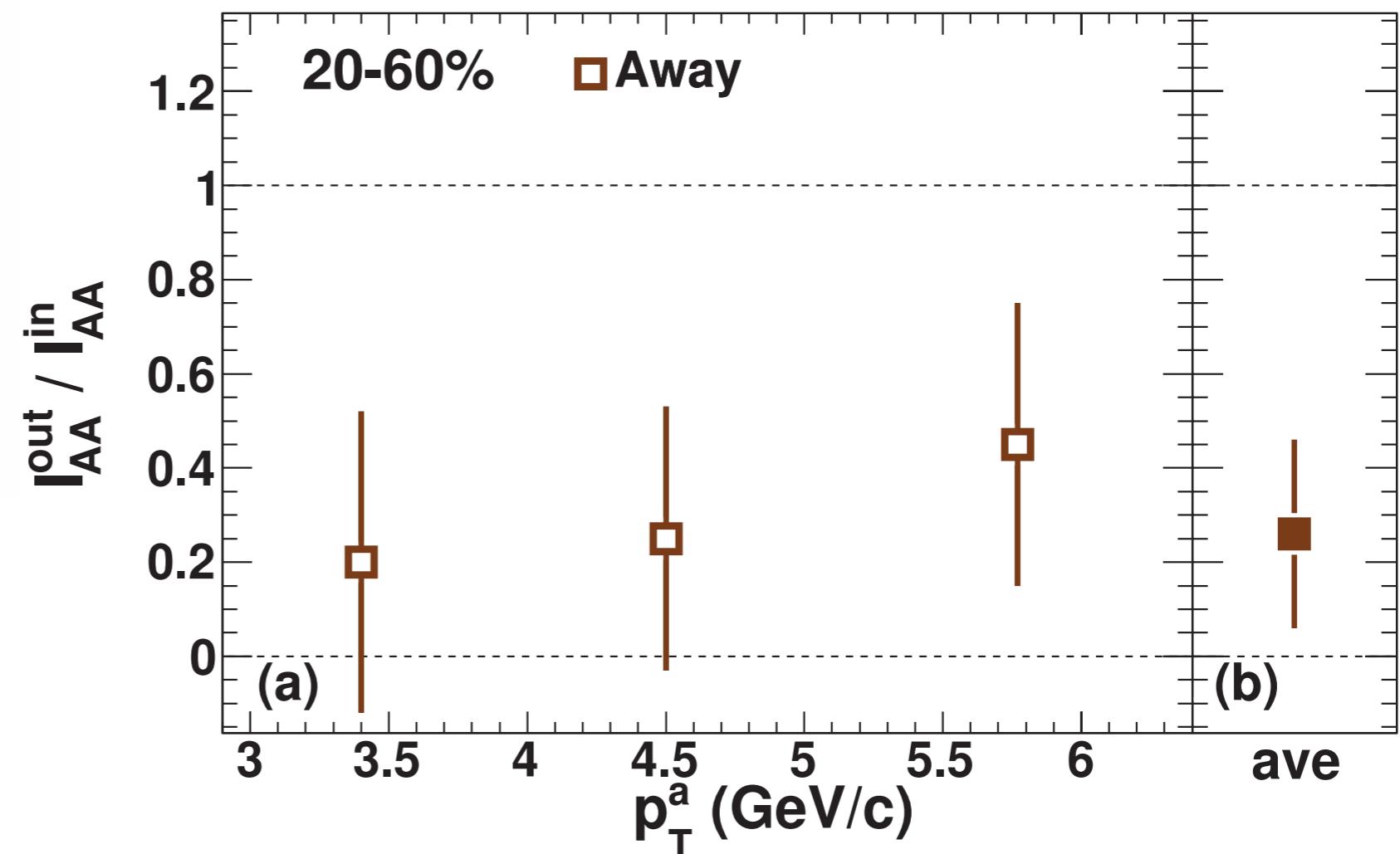
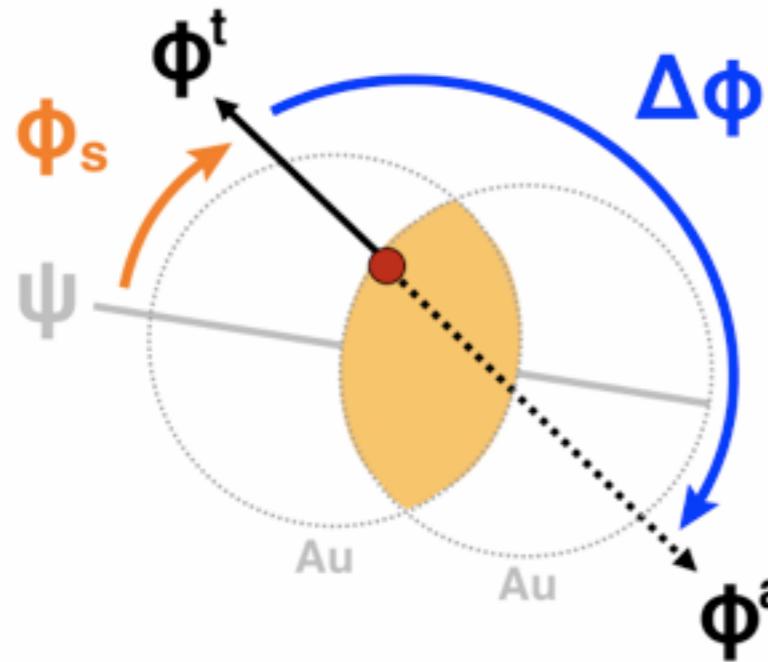
PHENIX PRL 104 252301 (2010)

same message from I_{AA}

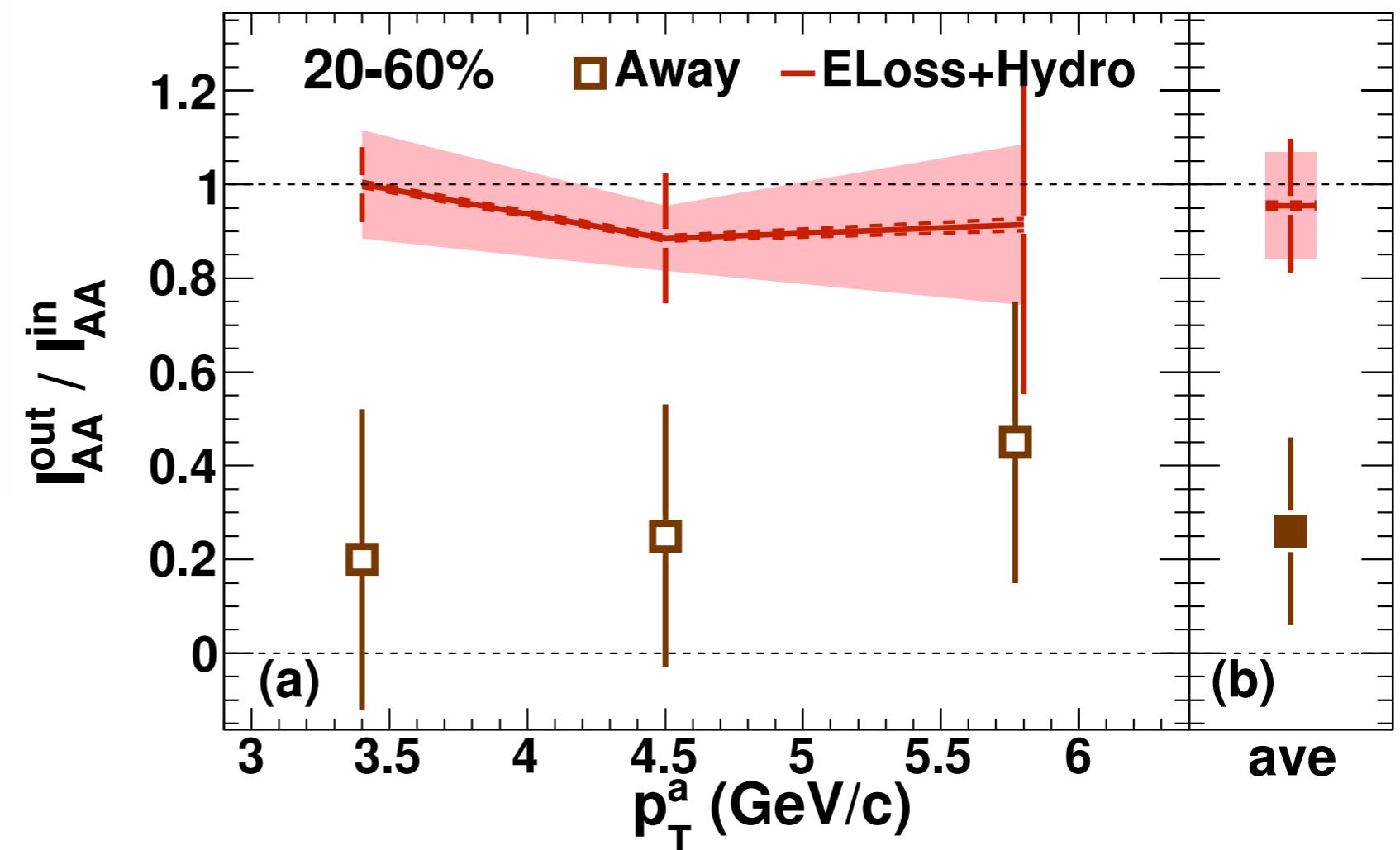
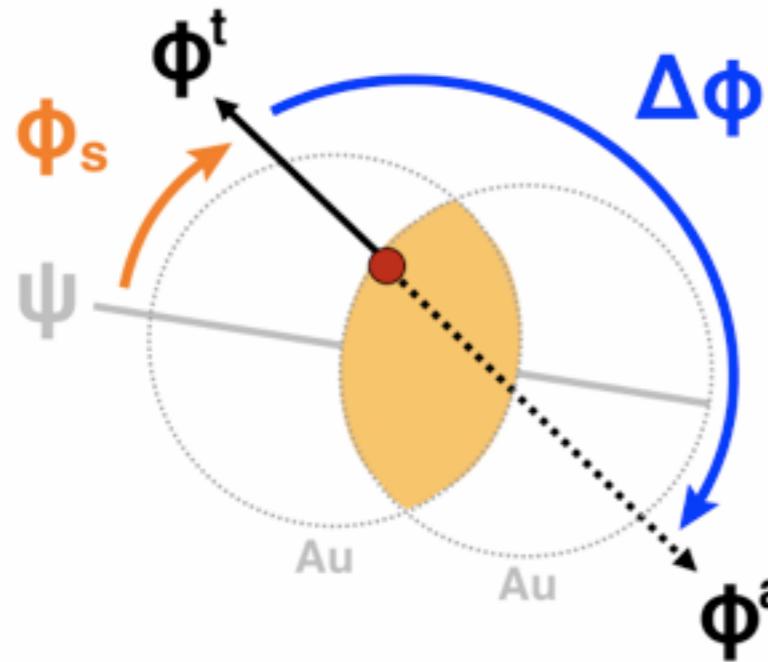


PHENIX 1010.1521

same message from $|l_{AA}|$



same message from $|I_{AA}|$



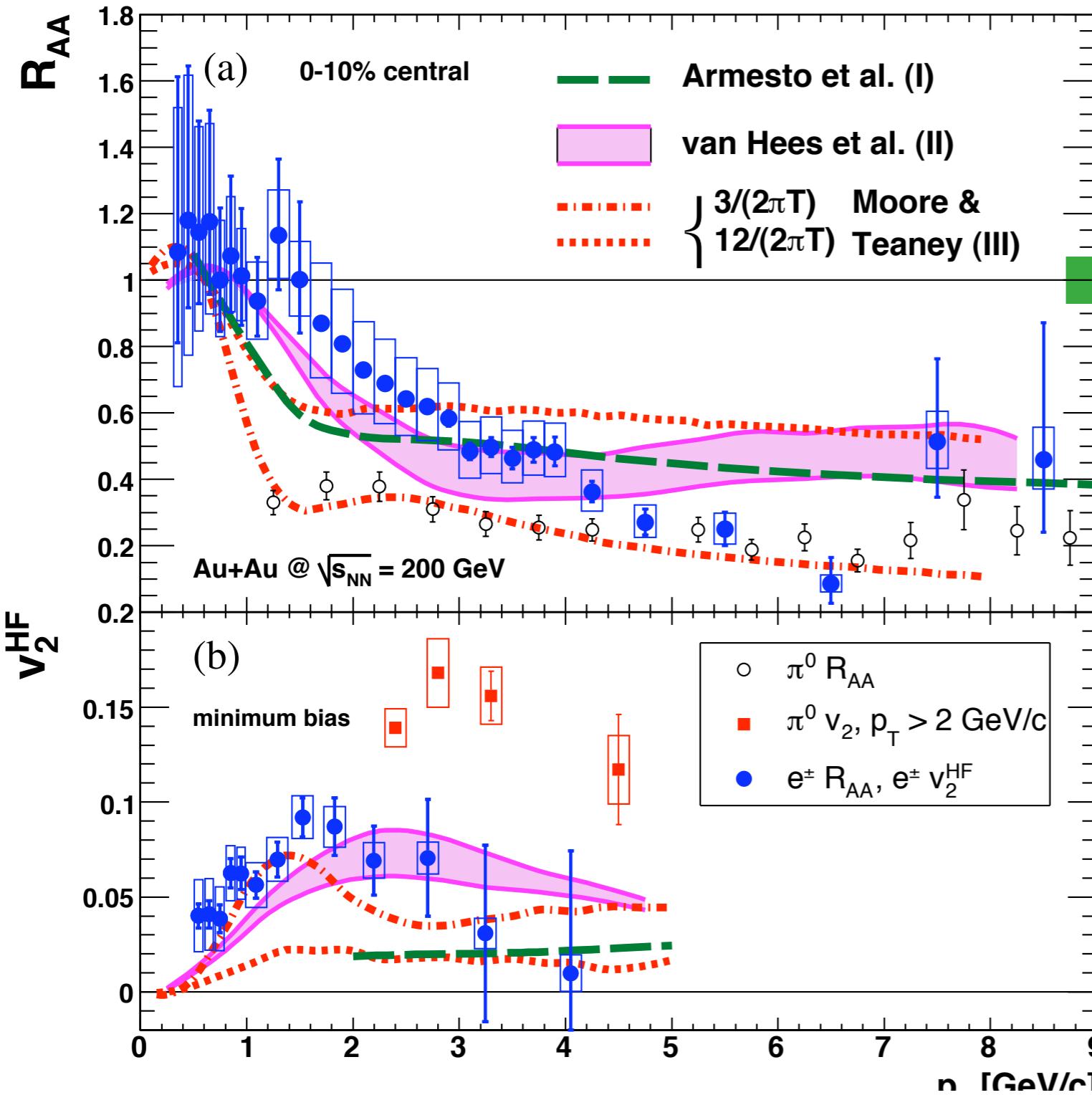
energy loss calculation from Renk in 2 hydro codes
(Nokana & Bass and Eskola et al.)

PHENIX 1010.1521

heavy flavor

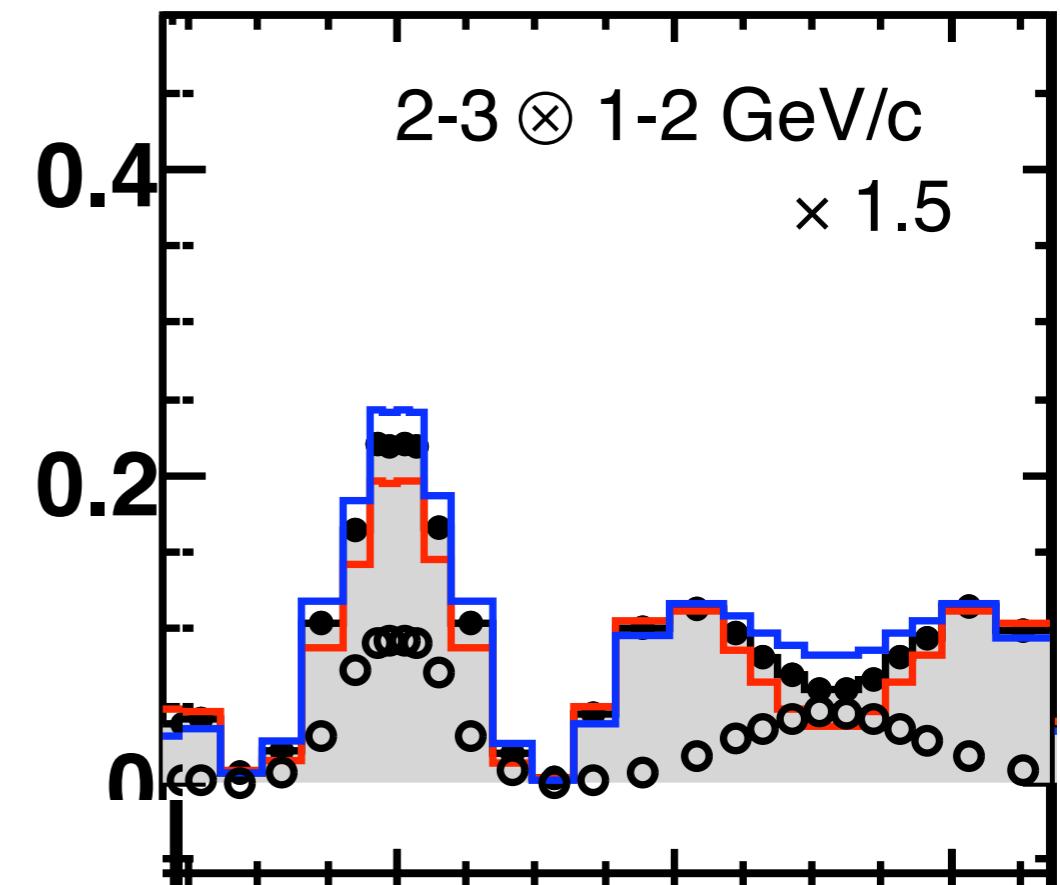
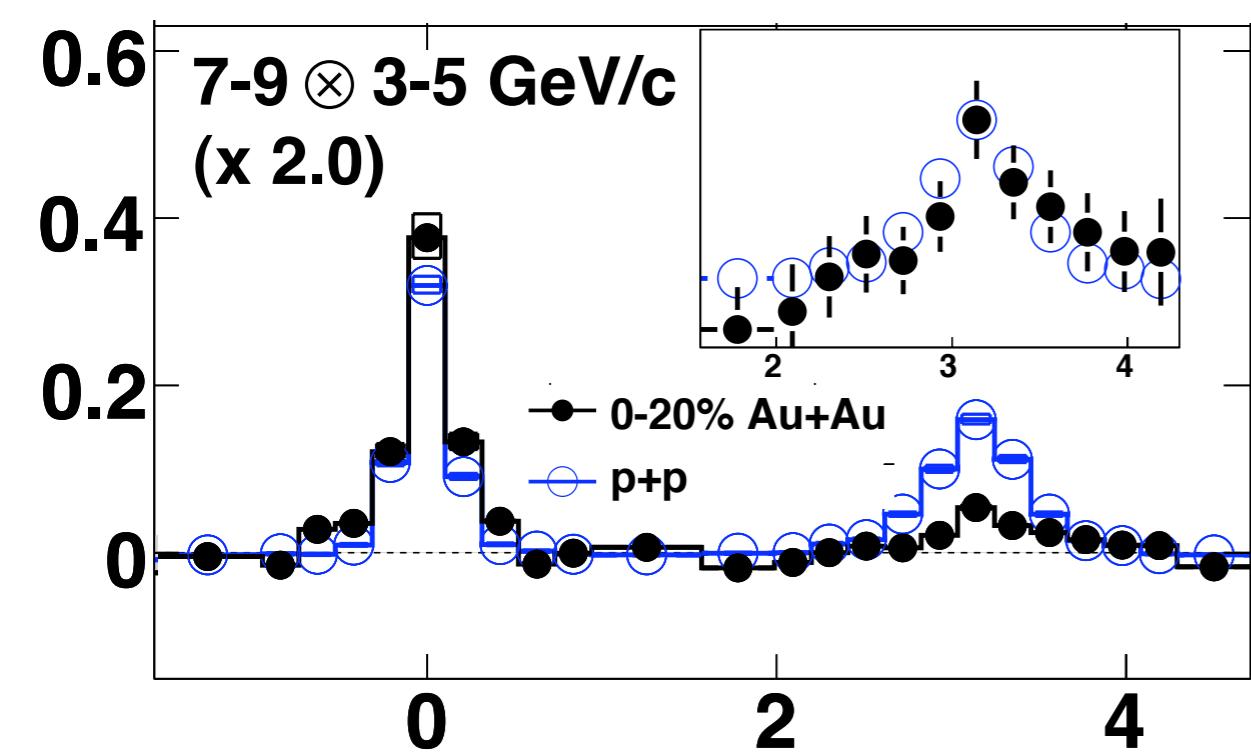
- collectivity and suppression
- not expected from radiative energy loss
- raises lots of questions:
 - c/b mixture in e^\pm
 - correlations
 - new theoretical ideas?

heavy flavor



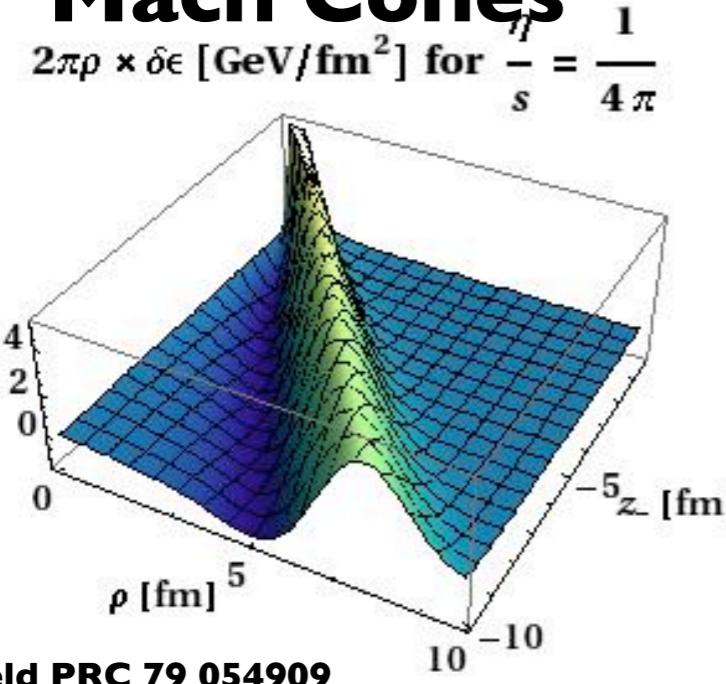
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double peak structure



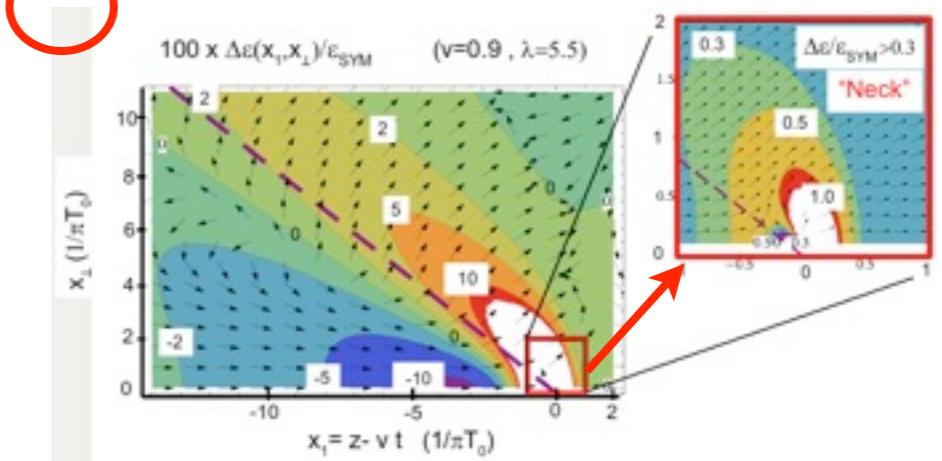
double peaks

Mach Cones



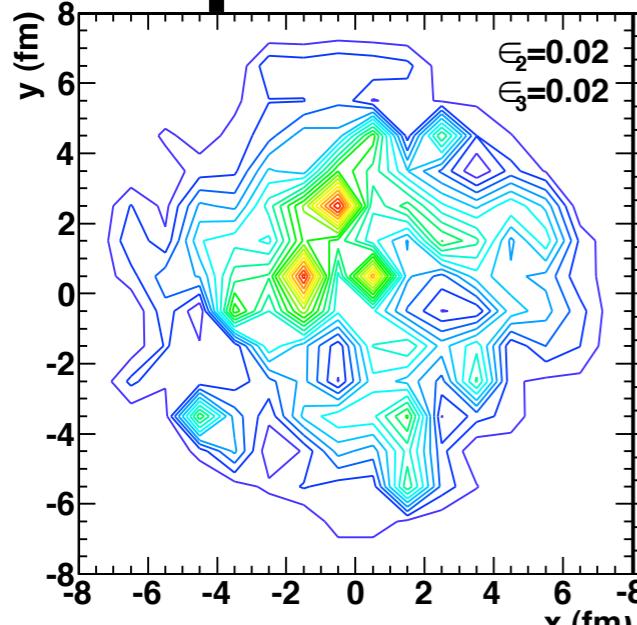
Neufeld PRC 79 054909

AdS/CFT



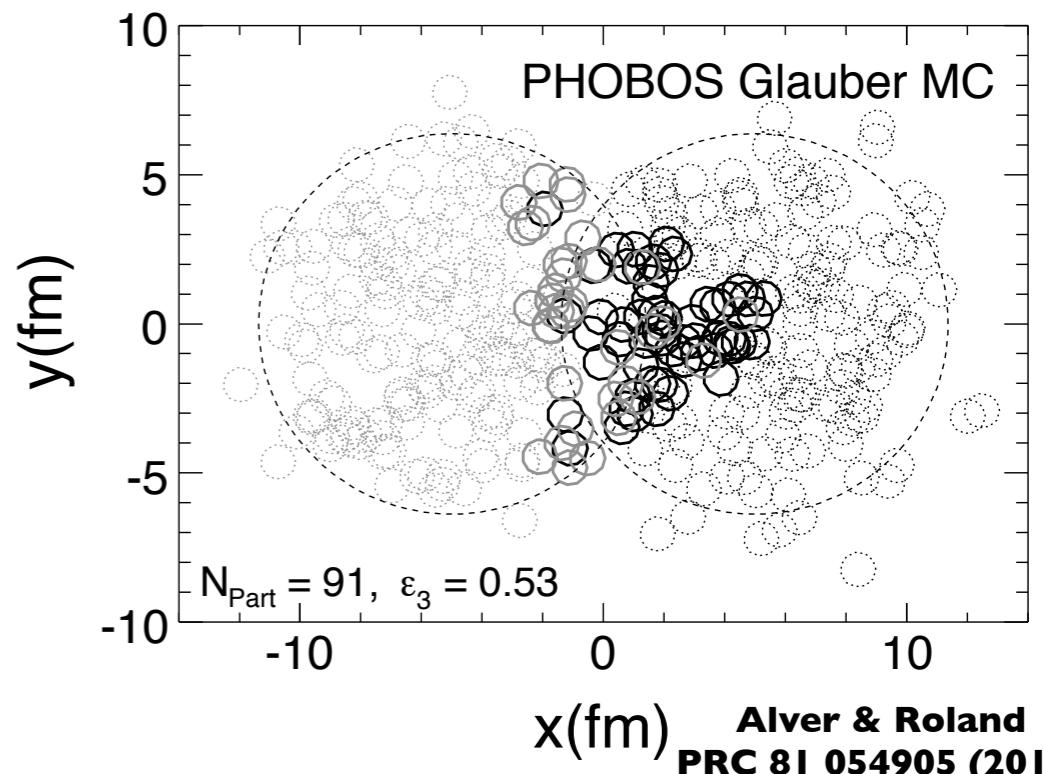
Noronha et al, PRL 102 102301 (2009)

Hot Spots



Ma & Wang 1011.5249

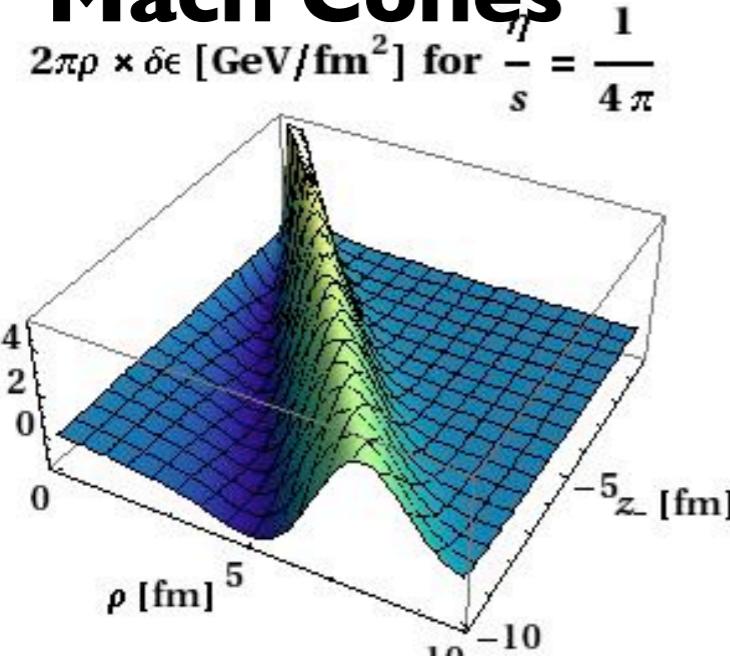
Initial State Fluct.



Alver & Roland
PRC 81 054905 (2010)

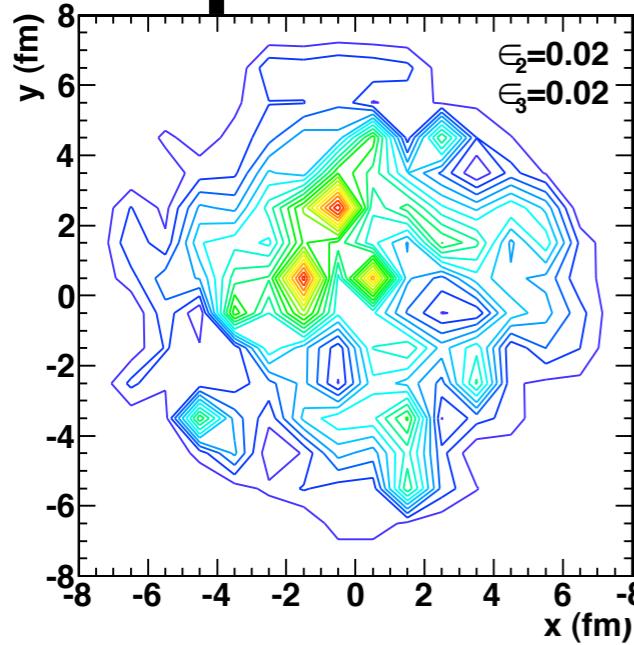
double peaks

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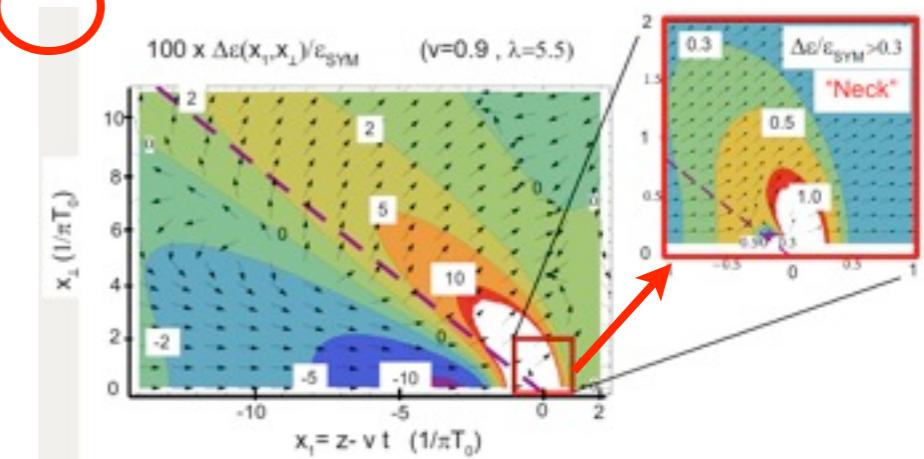


Ma & Wang 1011.5249

$$\cos\theta_M = \frac{\bar{c}_s}{v_{jet}}$$

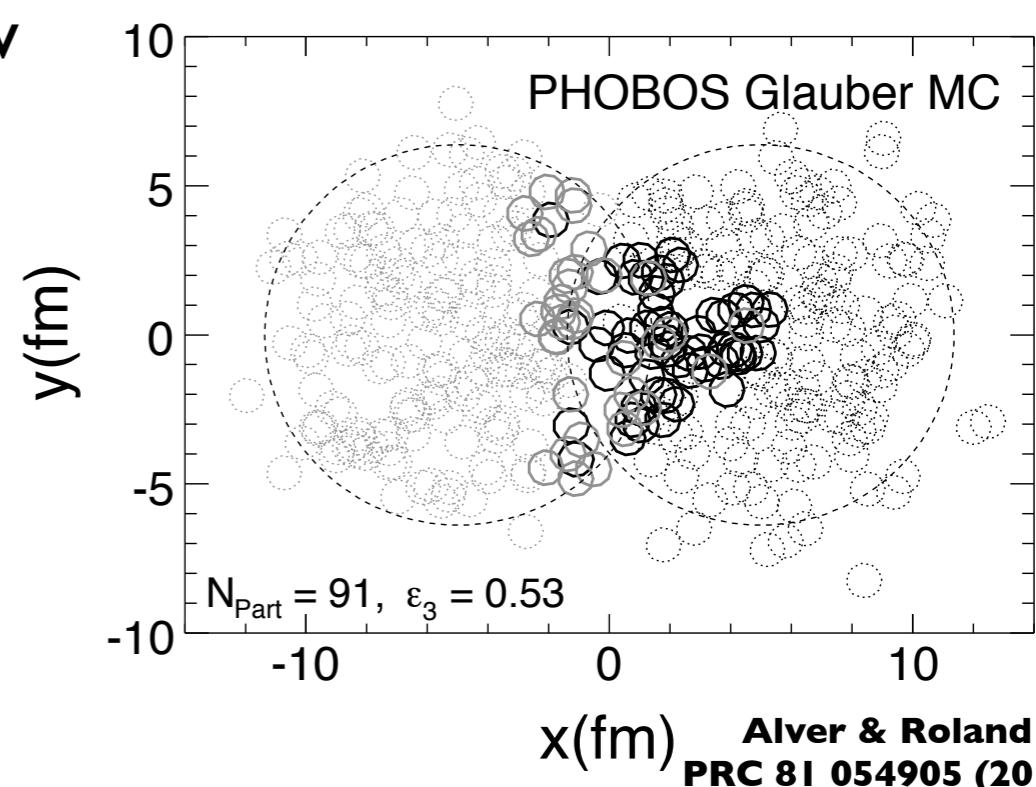
b-b correlations can
determine if correlations
follow Mach's Law

AdS/CFT



Noronha et al, PRL 102 102301 (2009)

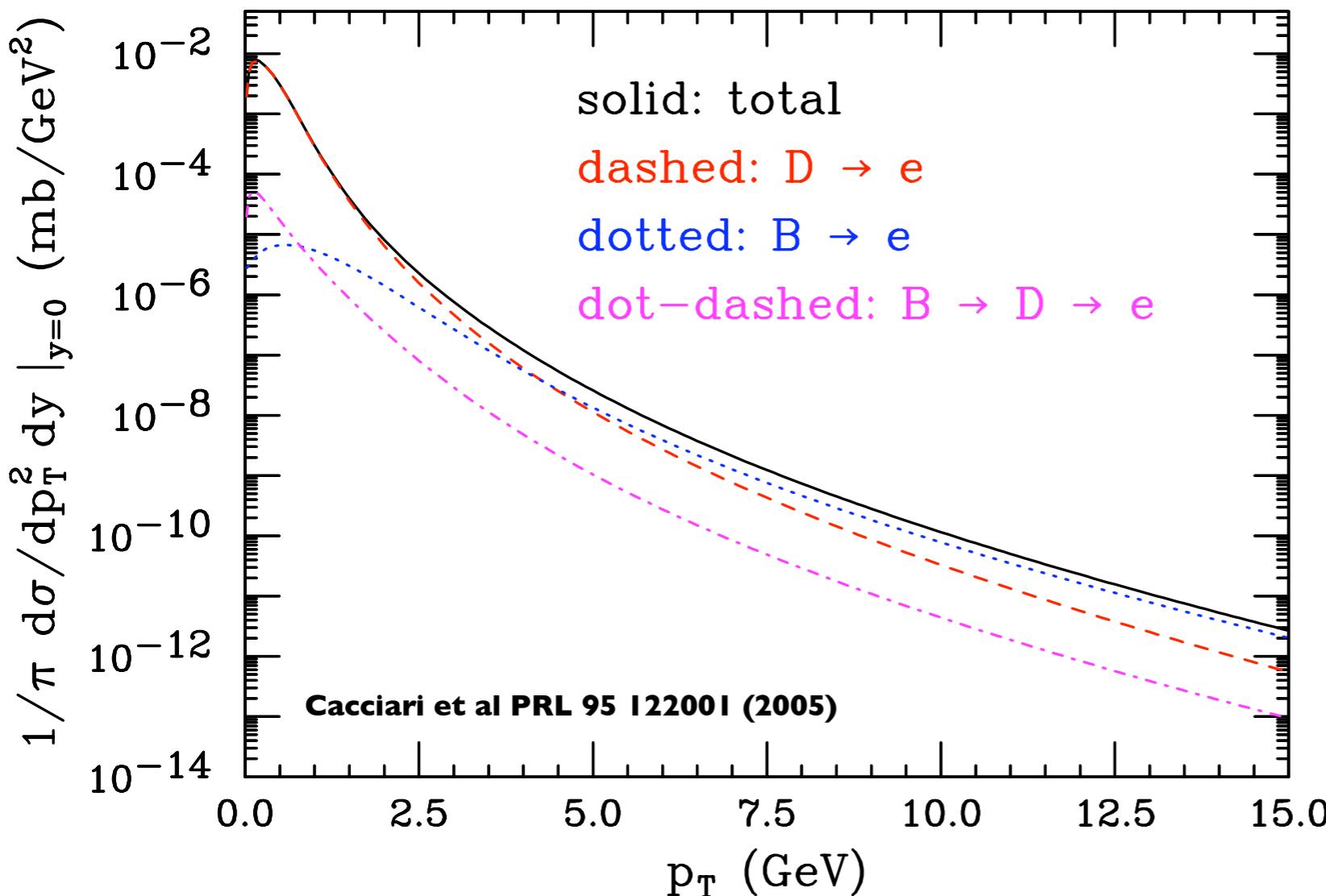
Initial State Fluct.



Alver & Roland
PRC 81 054905 (2010)

charm & bottom: theory

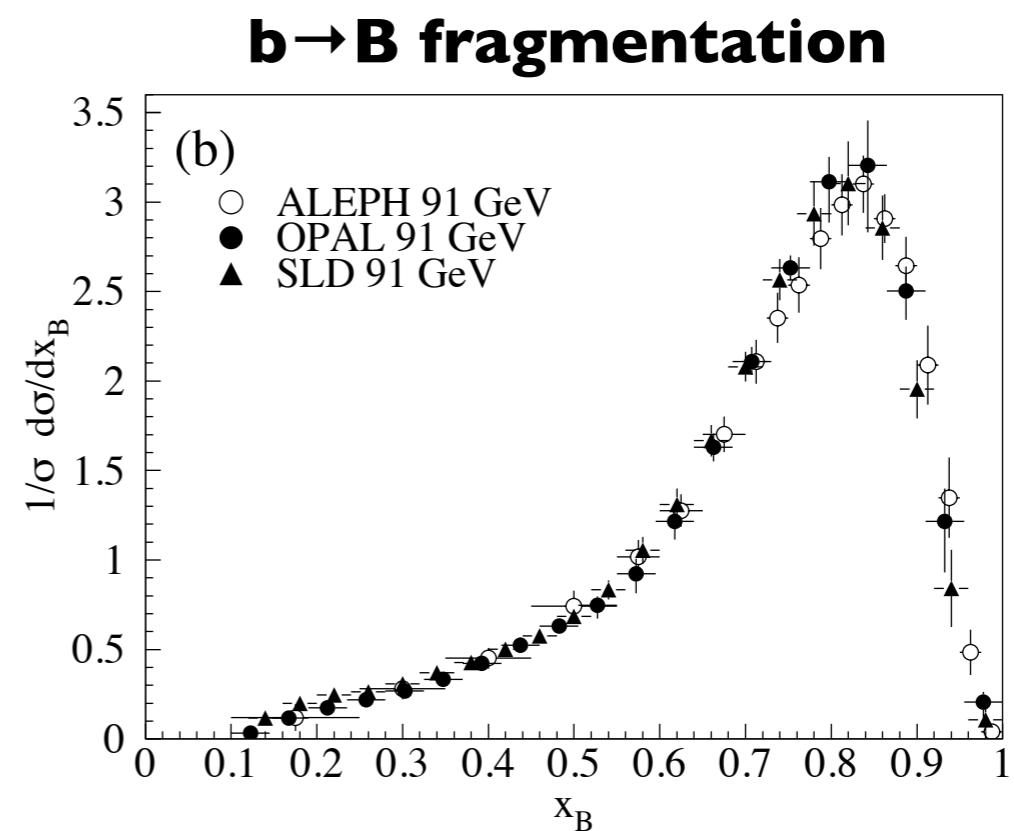
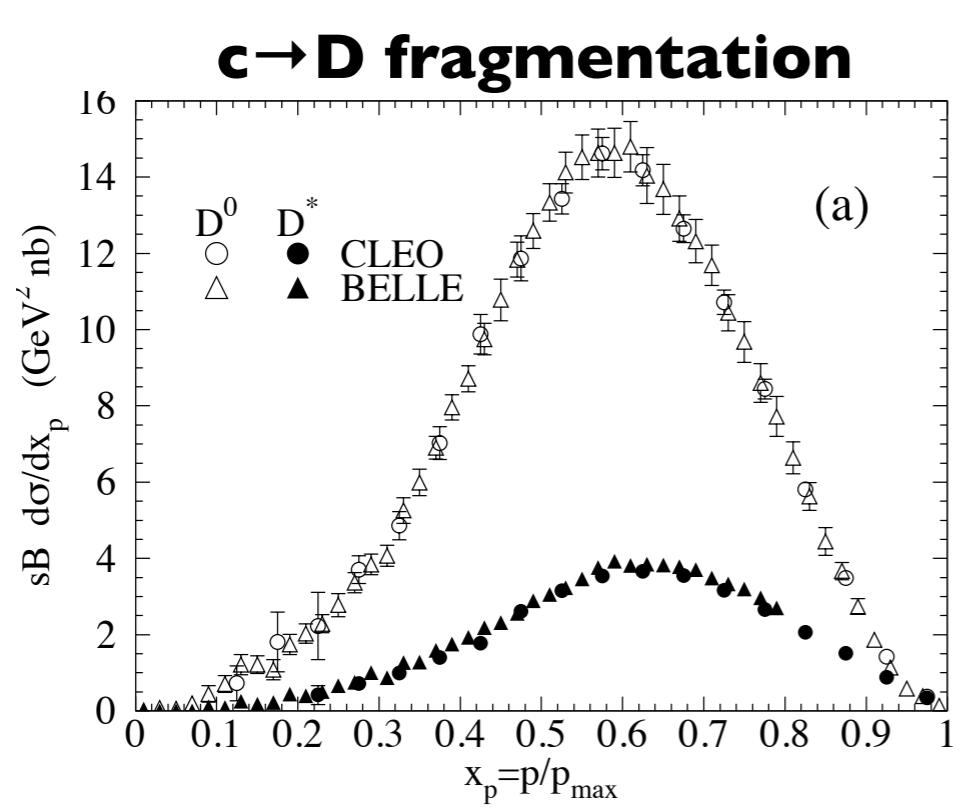
e \pm from c & b p+p $\sqrt{s}=200$ GeV



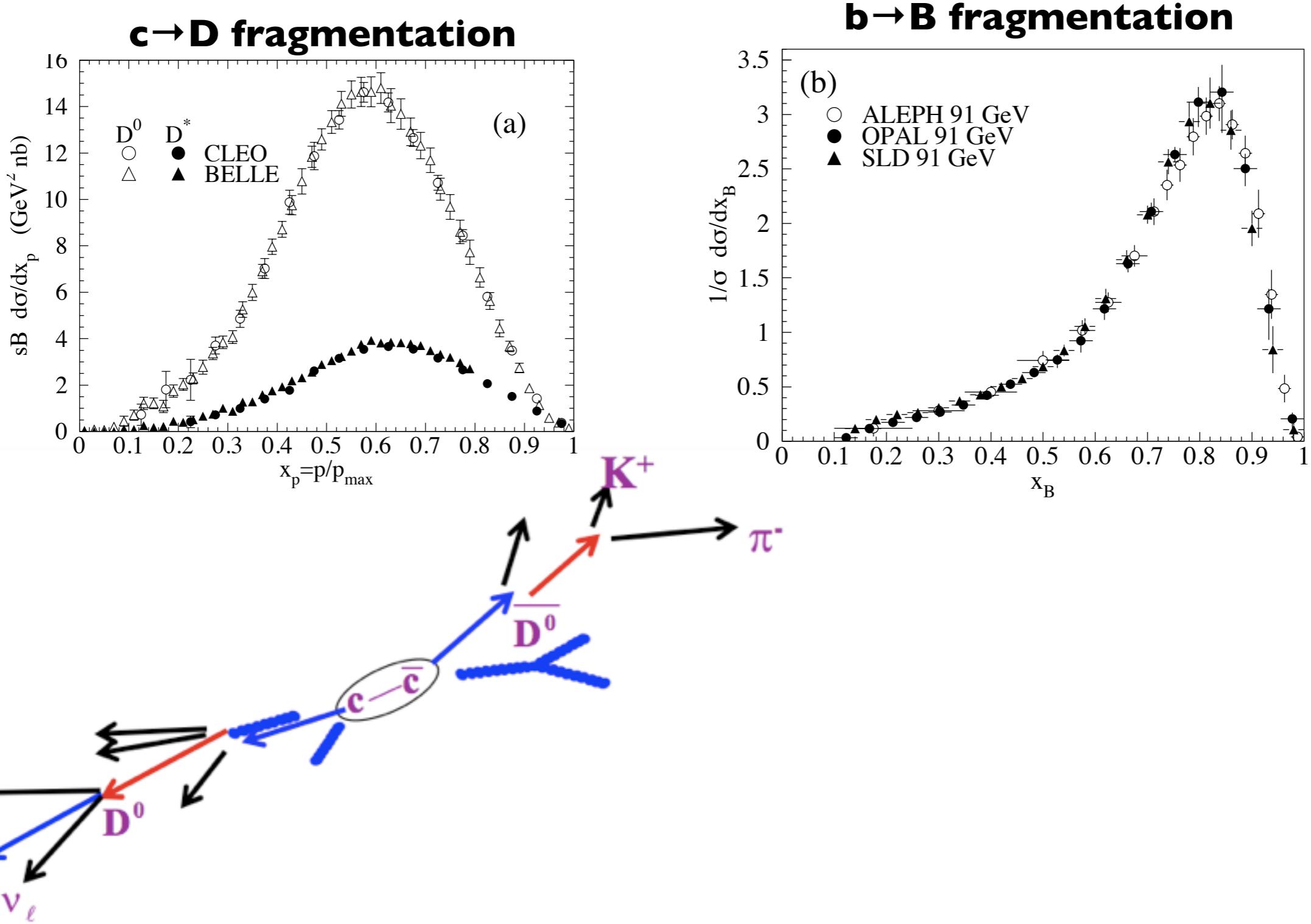
knowledge of relative c/b contributions crucial for understanding energy loss in Au+Au collisions

quarks to electrons

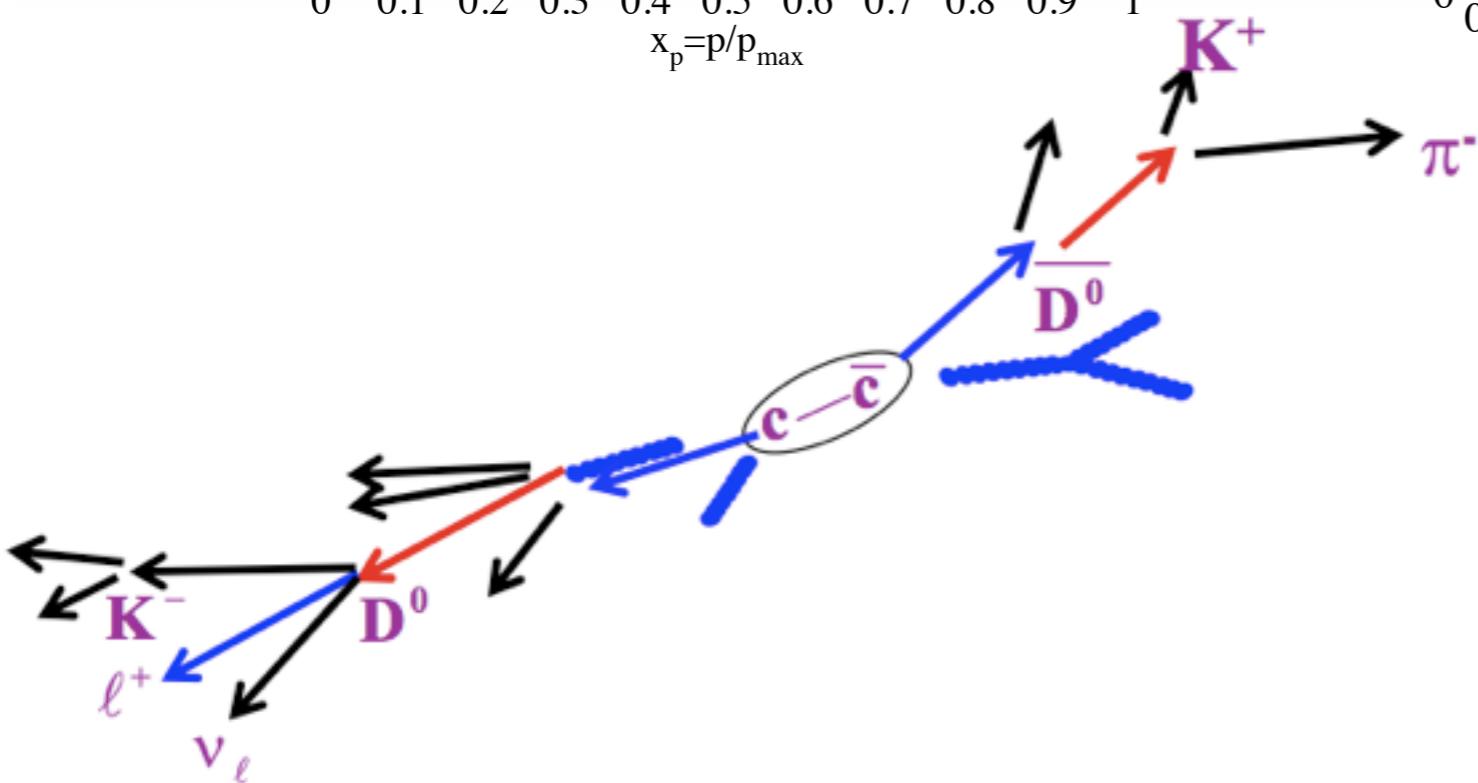
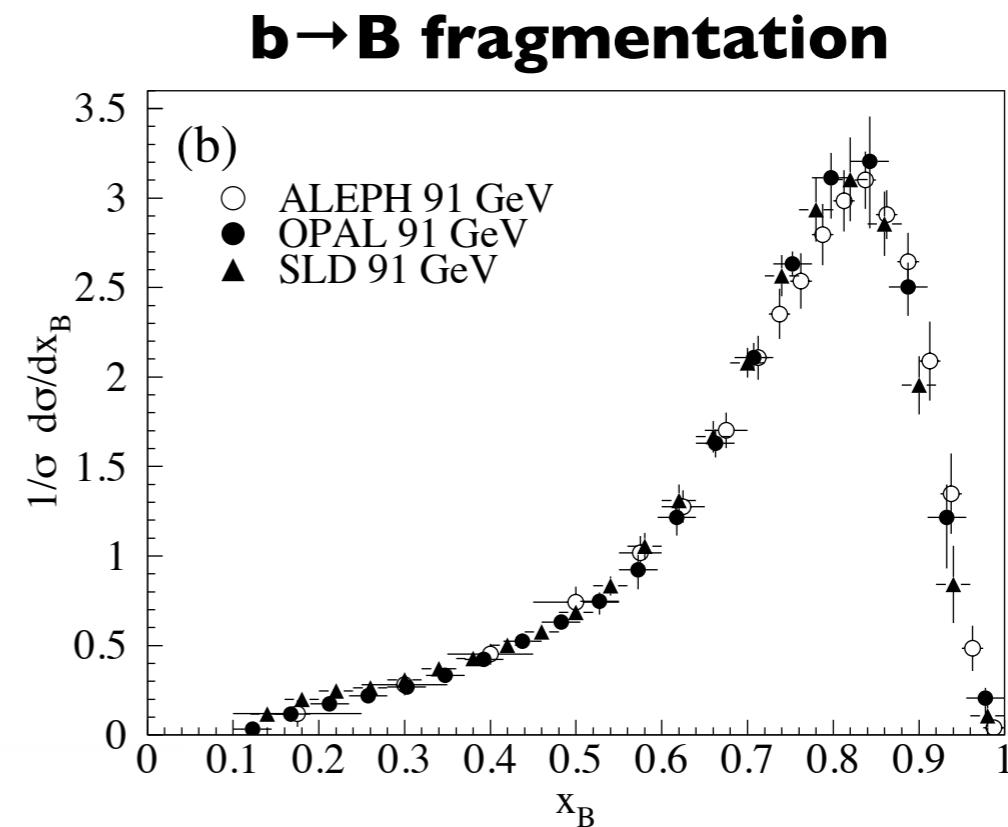
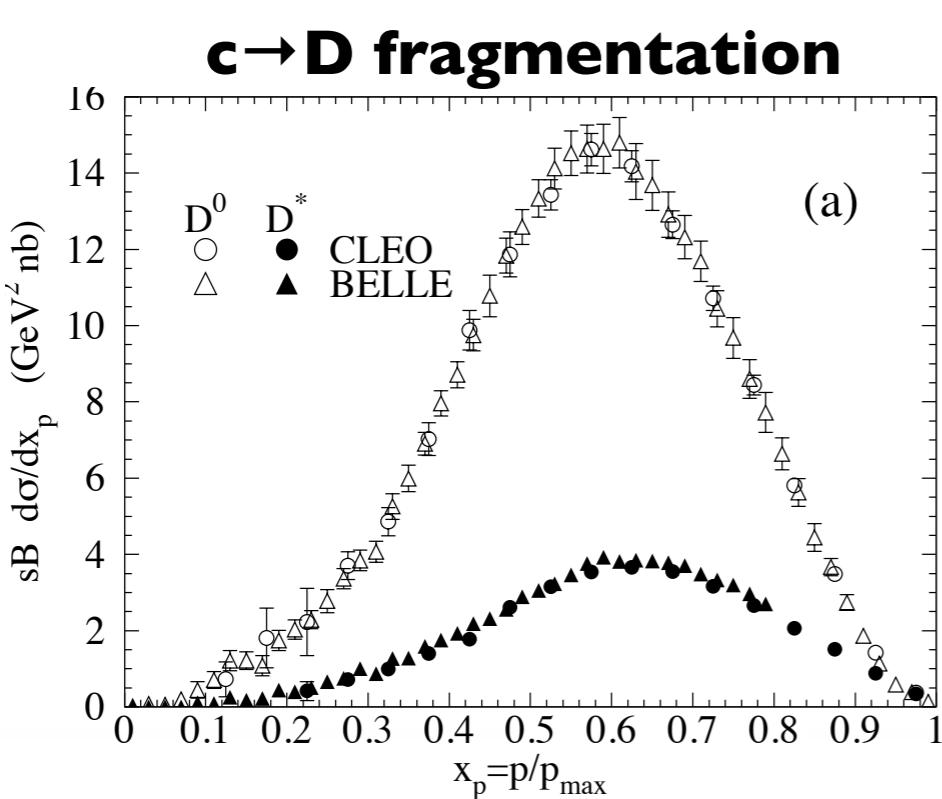
quarks to electrons



quarks to electrons

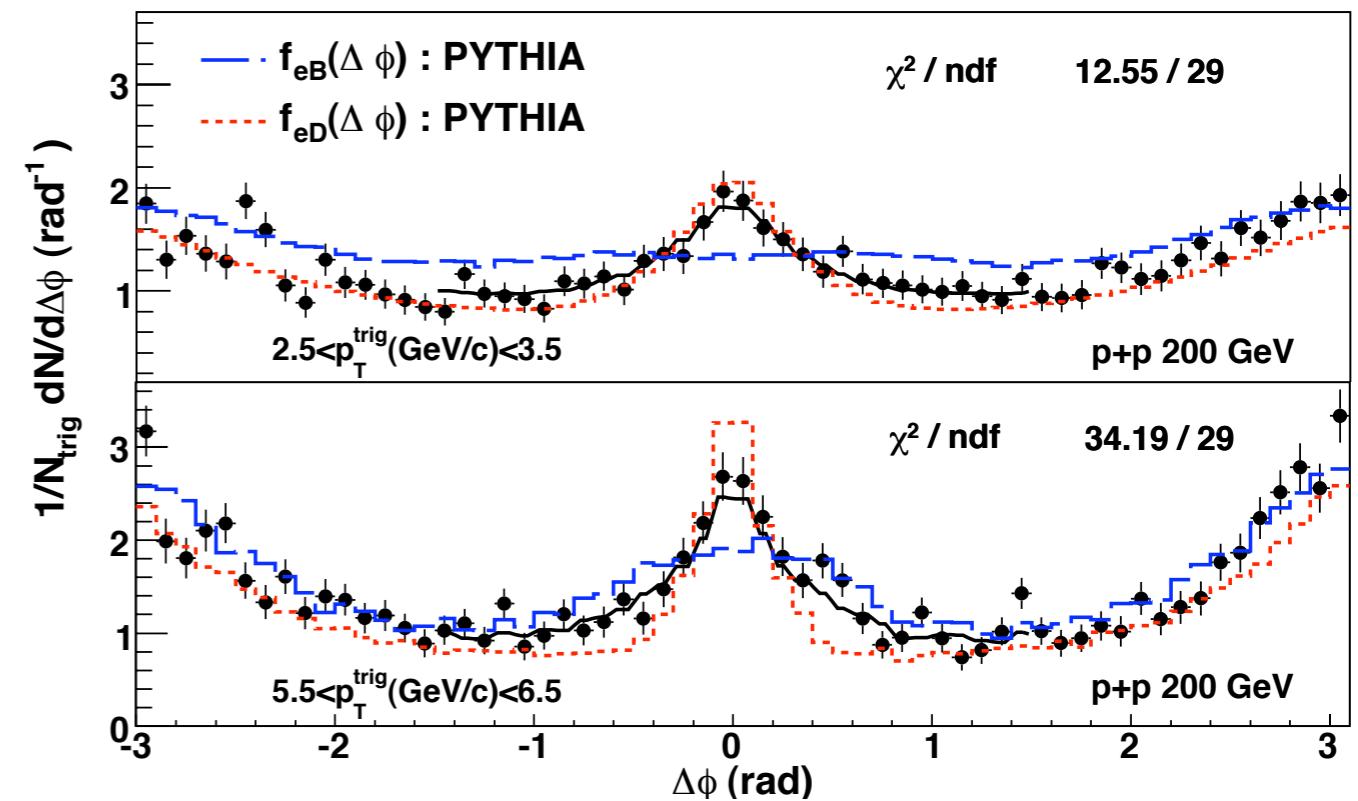
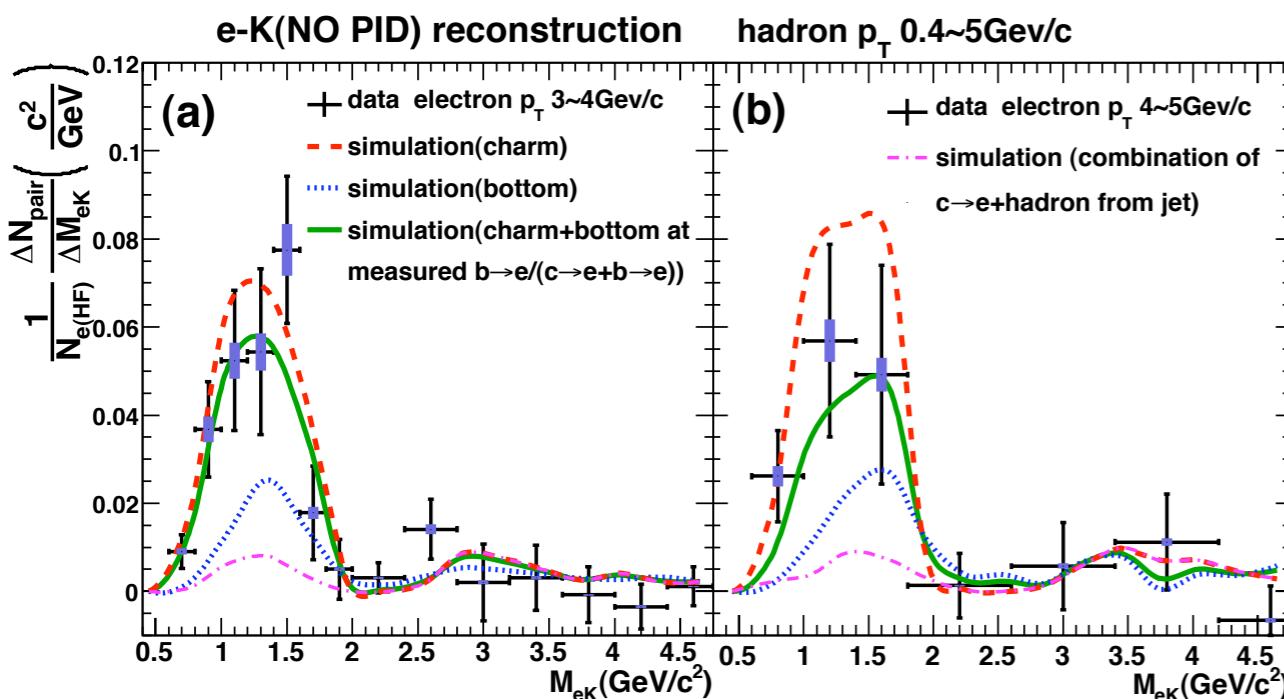


quarks to electrons



- small angle e-h correlations dominated by D & B decay products

model the near side



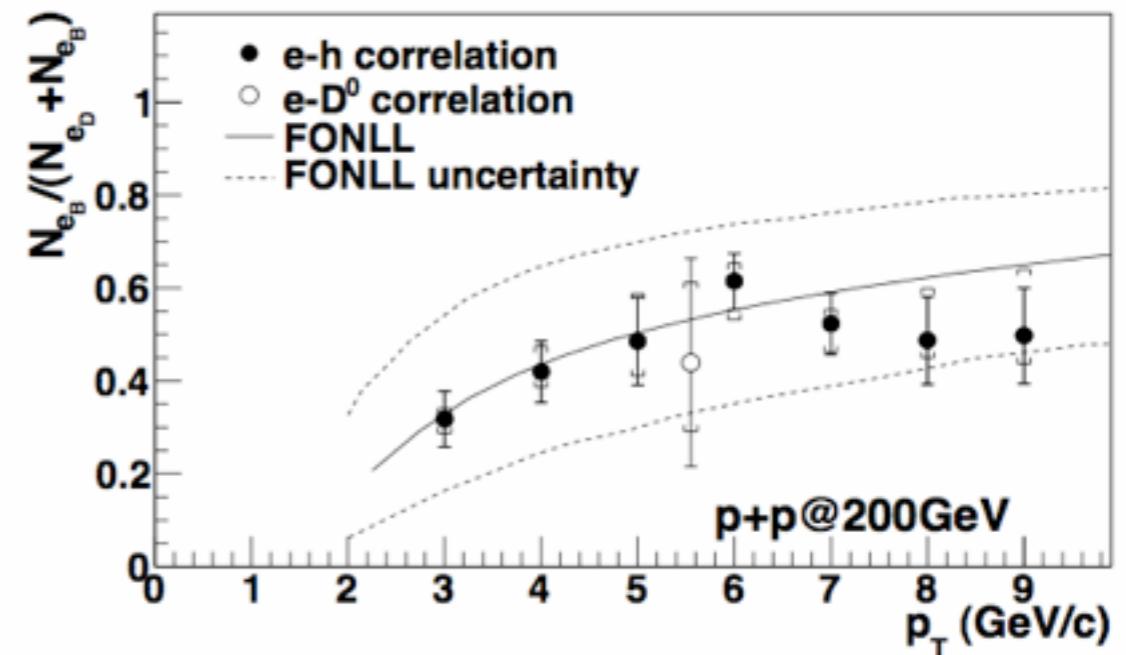
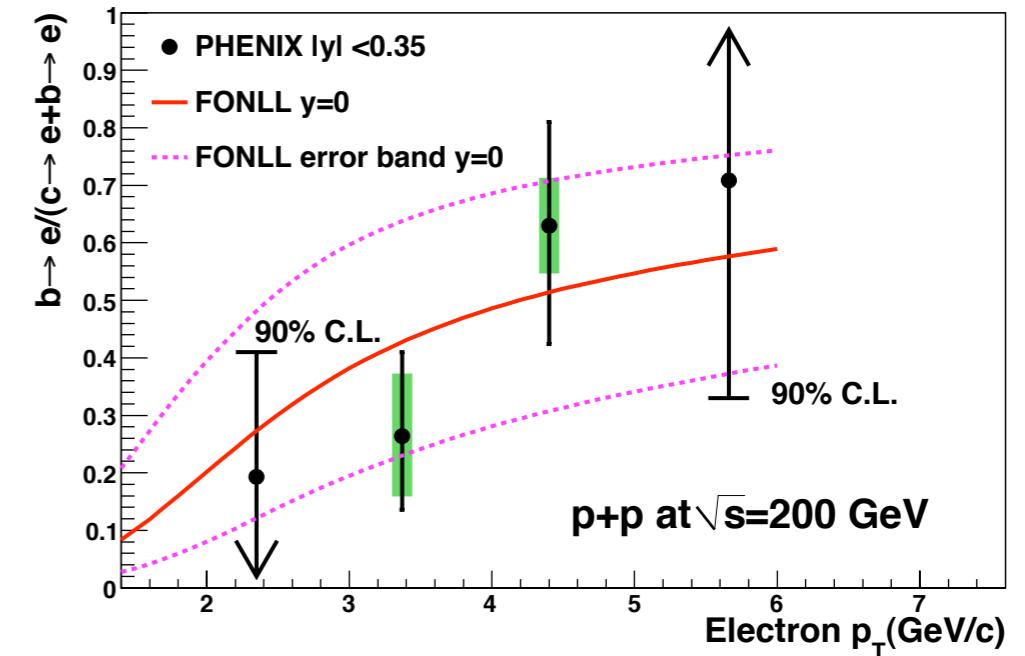
- introduces a dependence on MC for decays and particle mix
- PYTHIA to handle decays

PHENIX PRL 103 082002 (2009)
STAR: PRL 105 202301 (2010)

charm vs. bottom: experiment

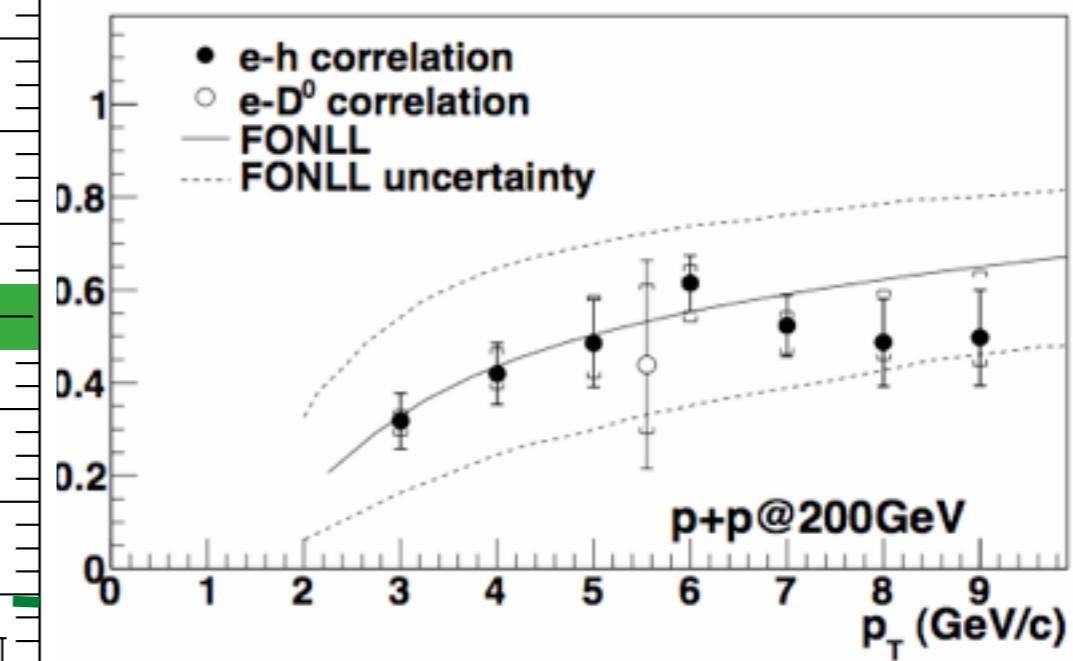
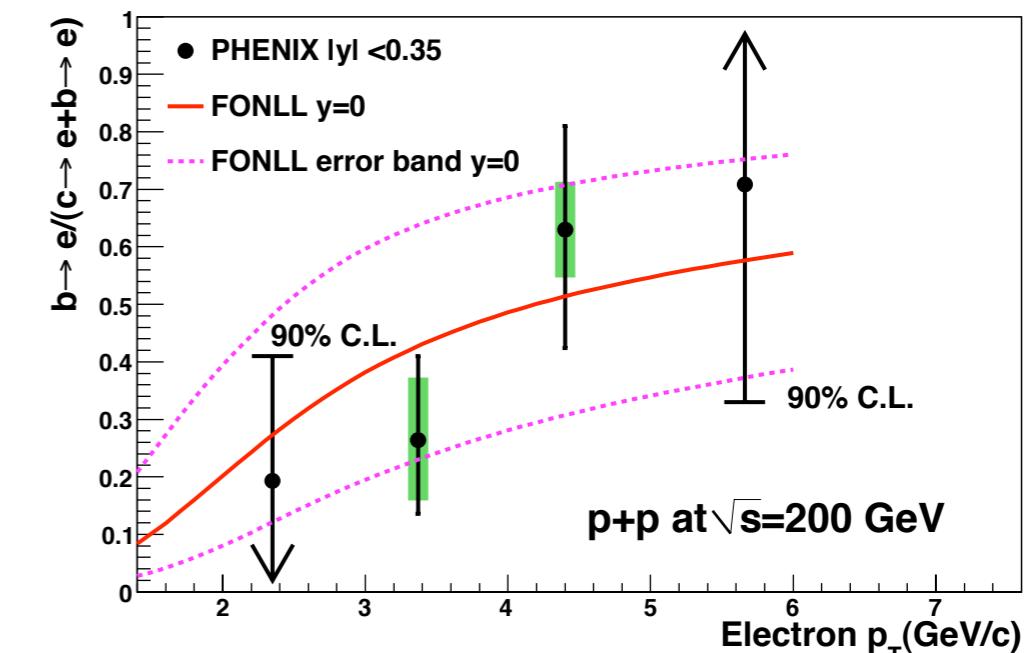
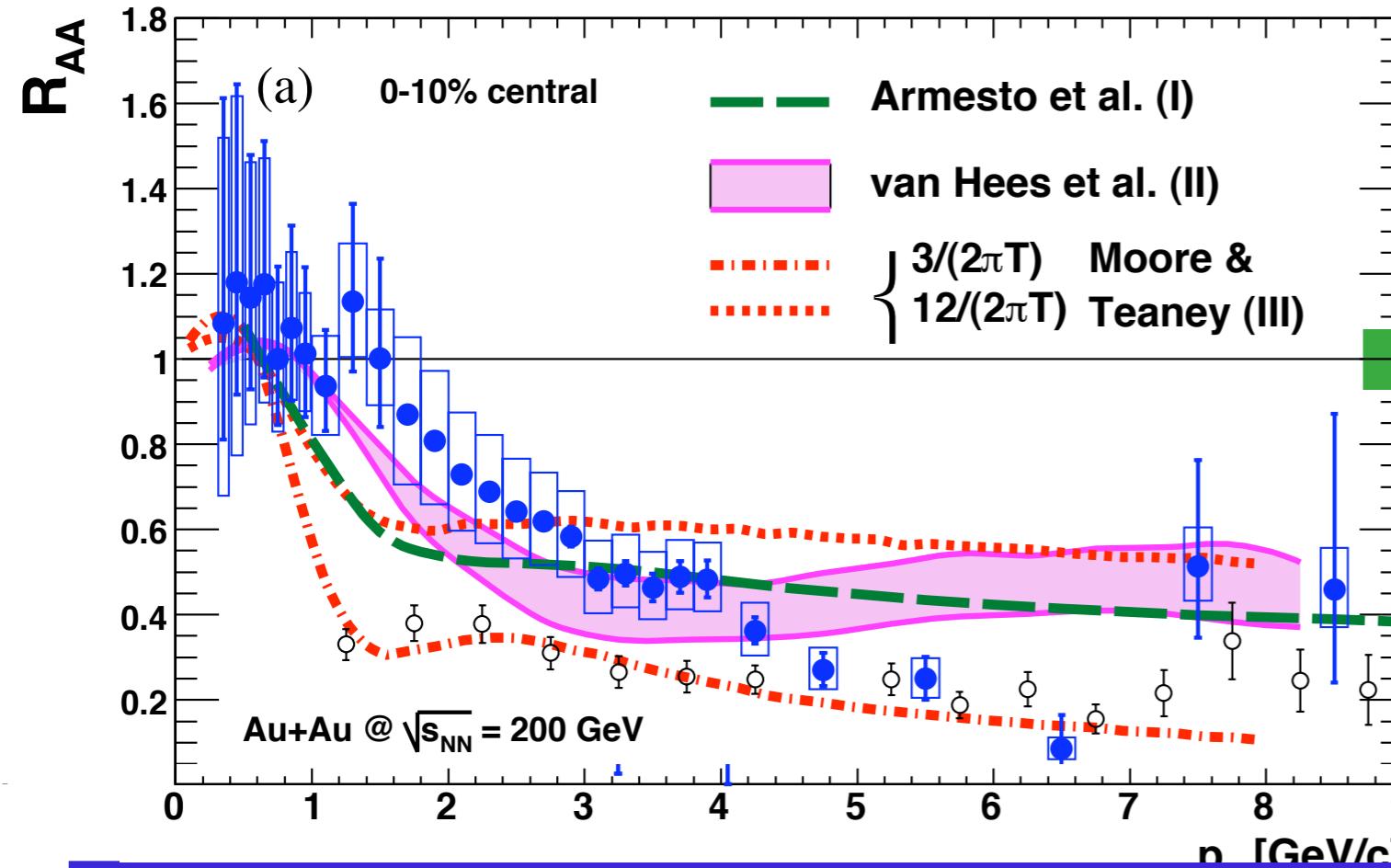
PHENIX PRL 103 082002 (2009)
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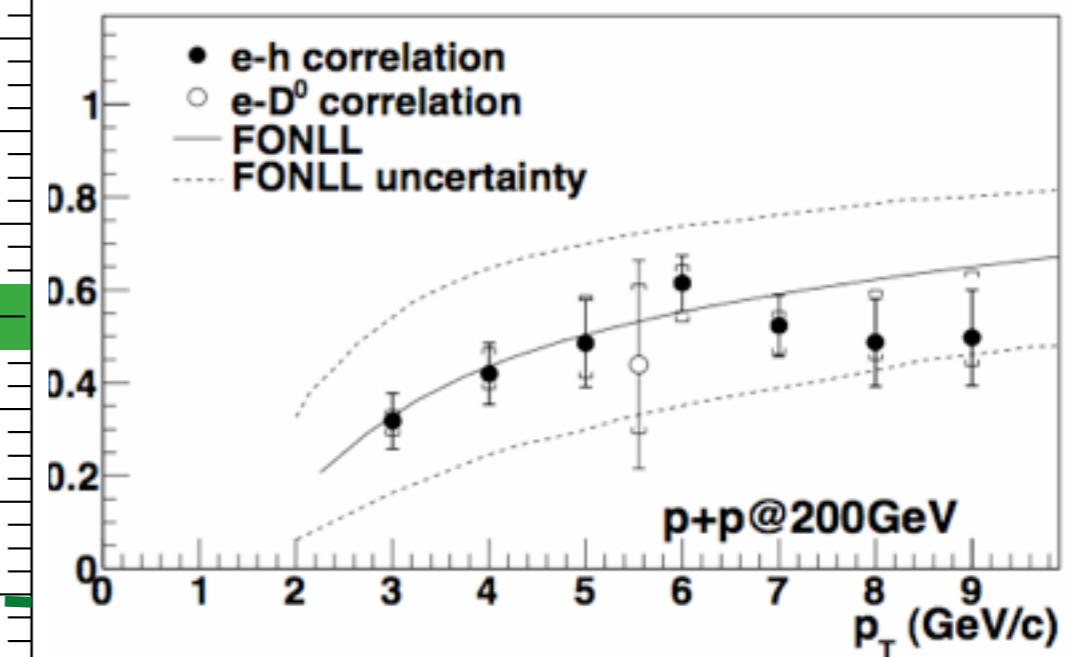
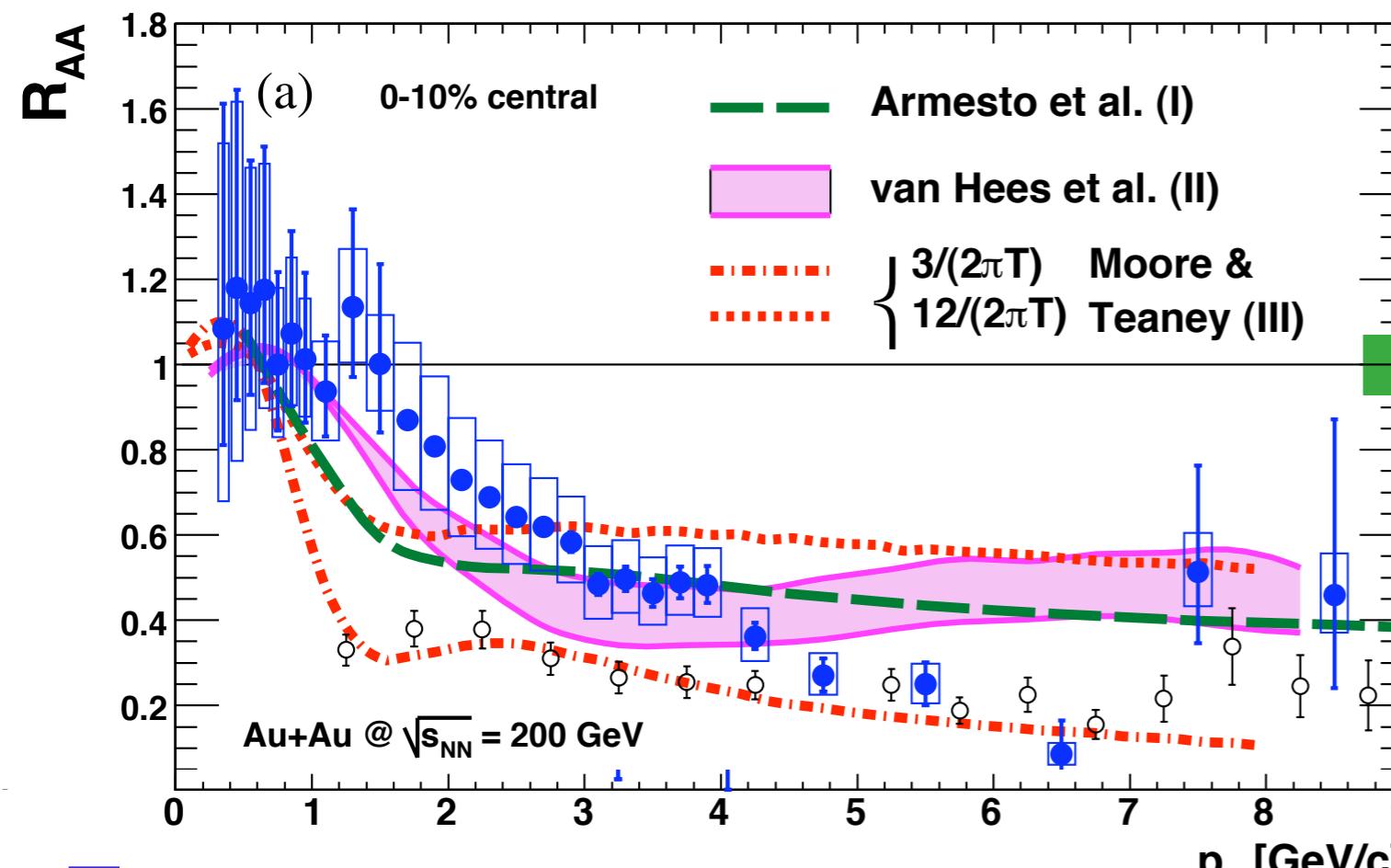
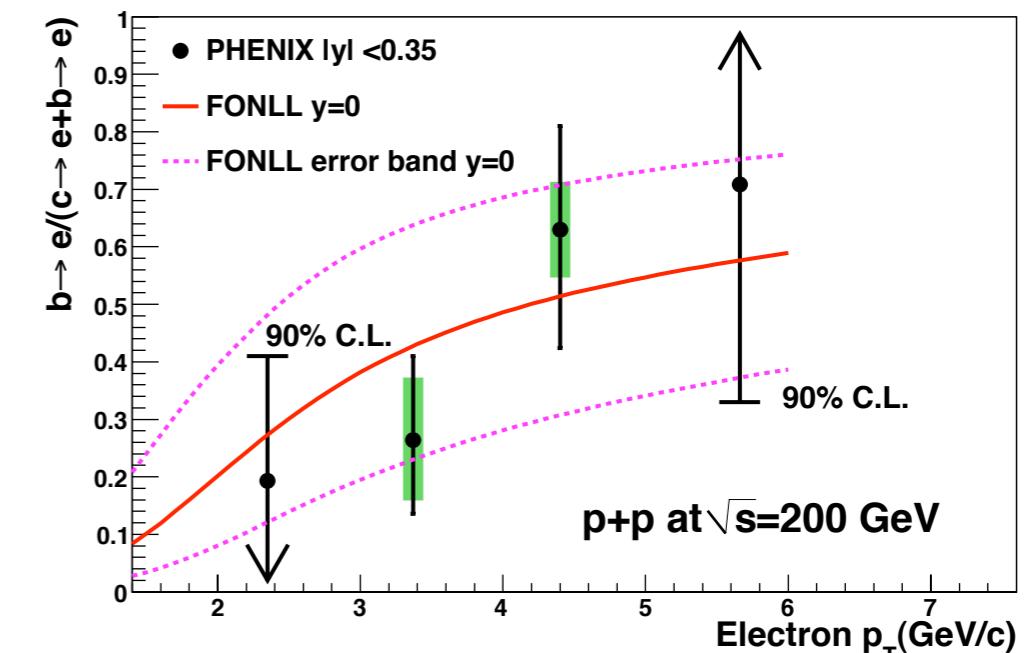
charm vs. bottom: experiment



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charm vs. bottom: experiment

- suppression large even as electrons become dominated by bottom at high p_T
- b fraction well described by FONLL

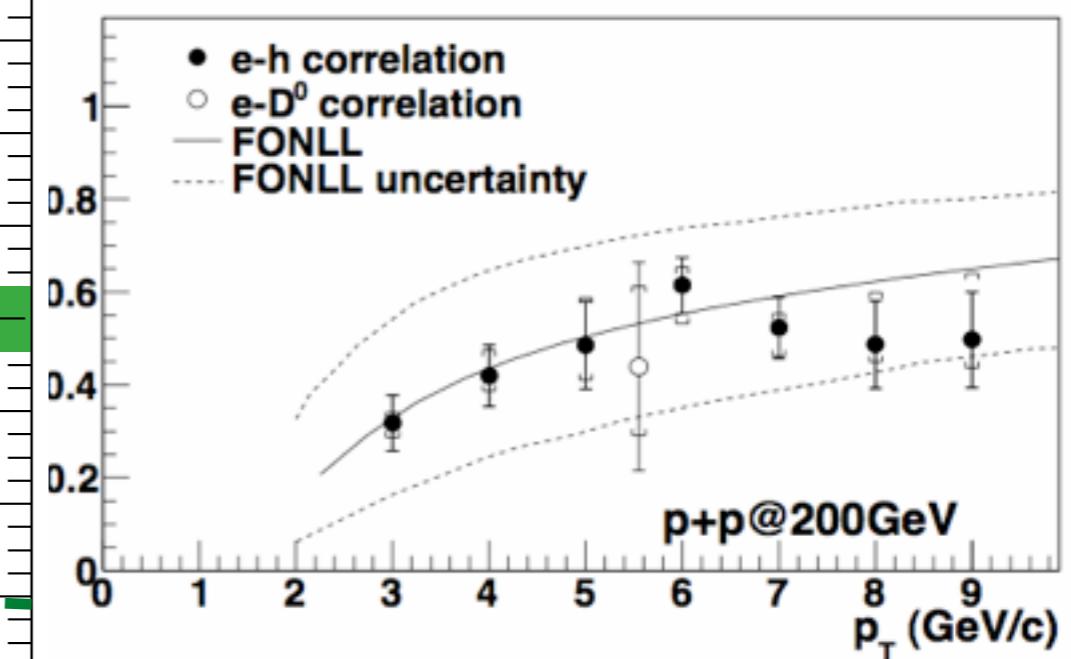
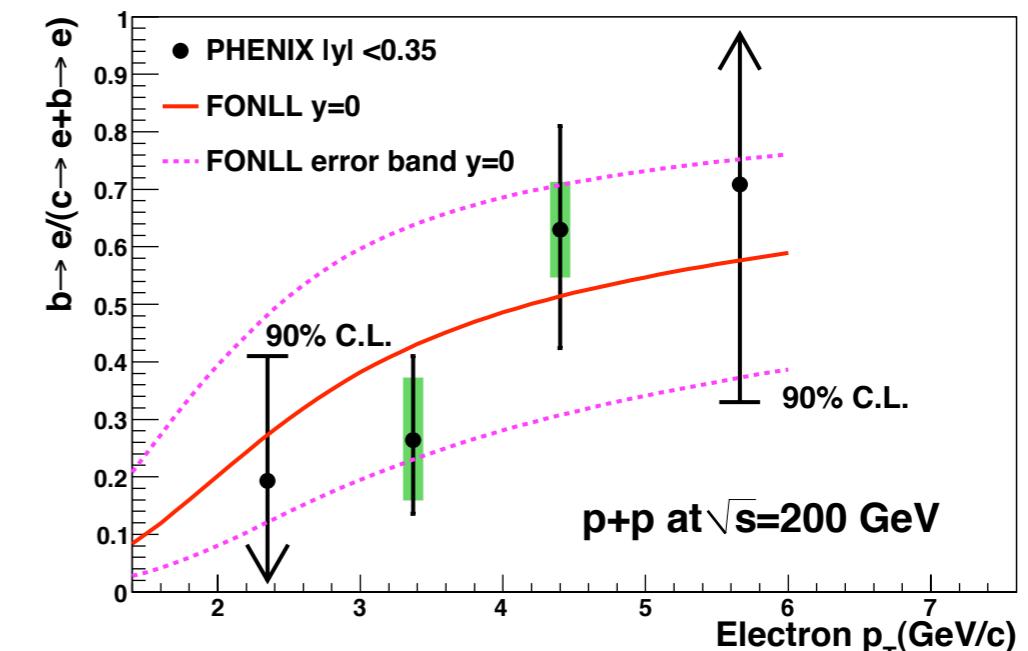
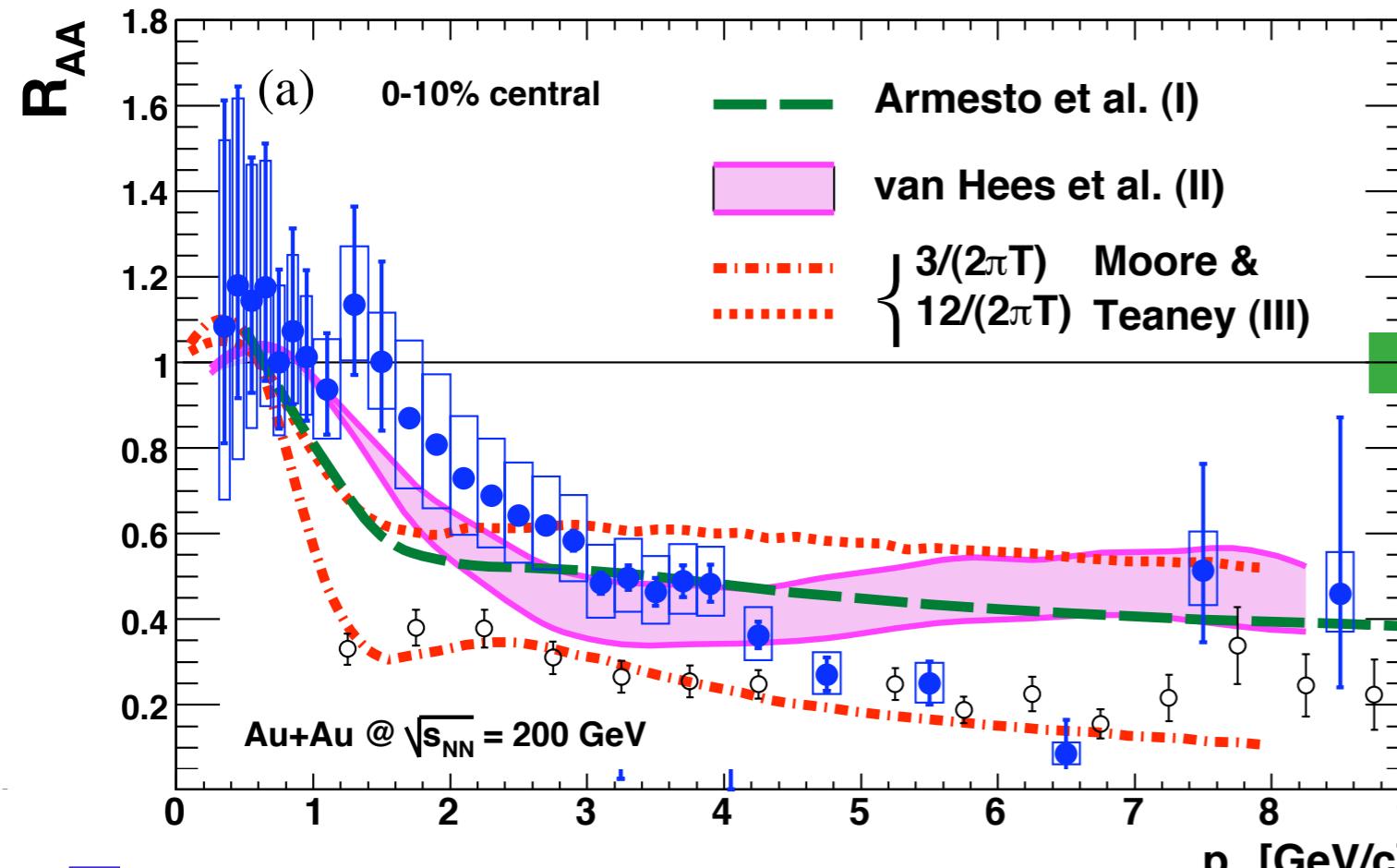


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 STAR: PRL 105 202301 (2010)

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$$R_{AA}^{\text{HF}} = (1 - r_B) R_{AA}^{e_D} + r_B R_{AA}^{e_B}$$

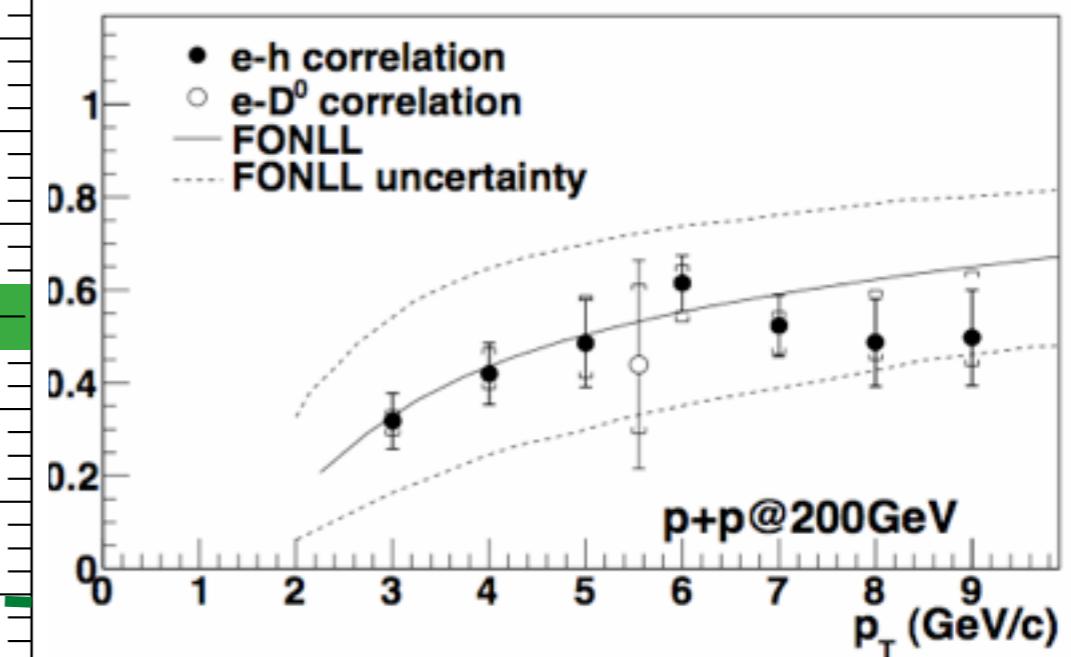
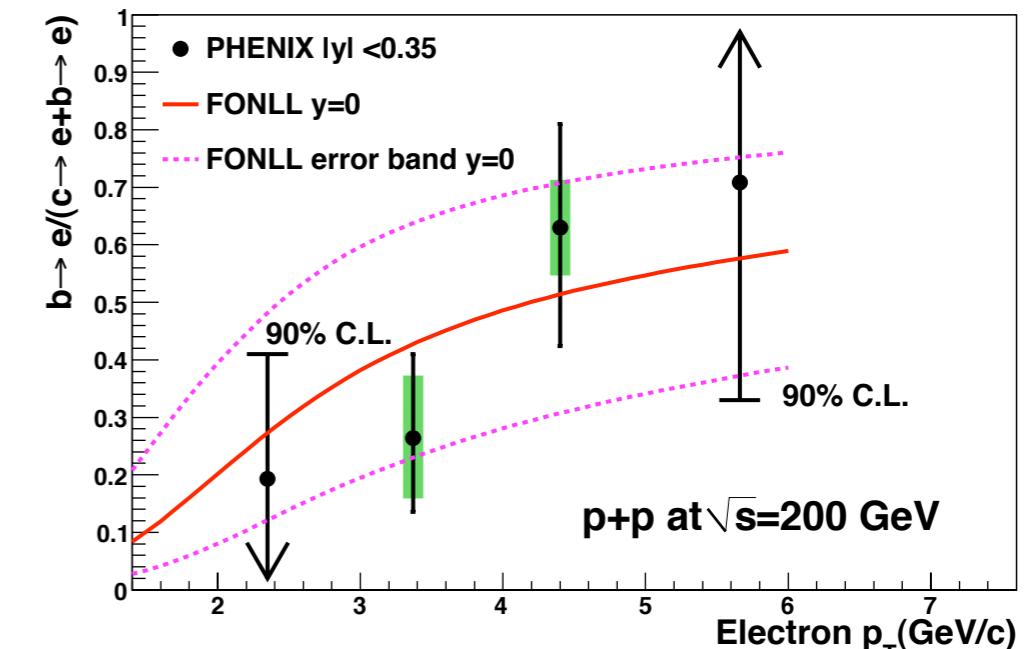
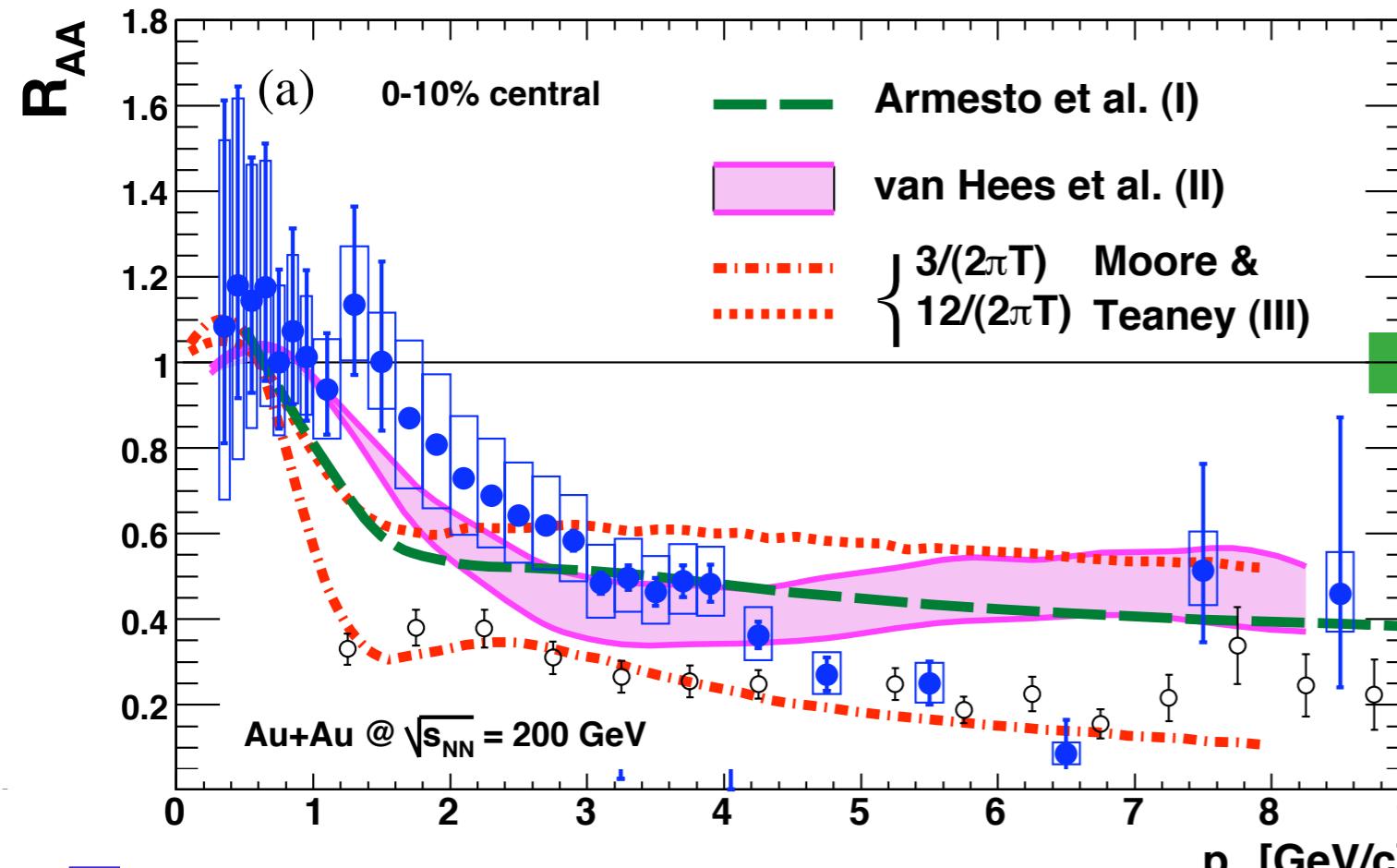


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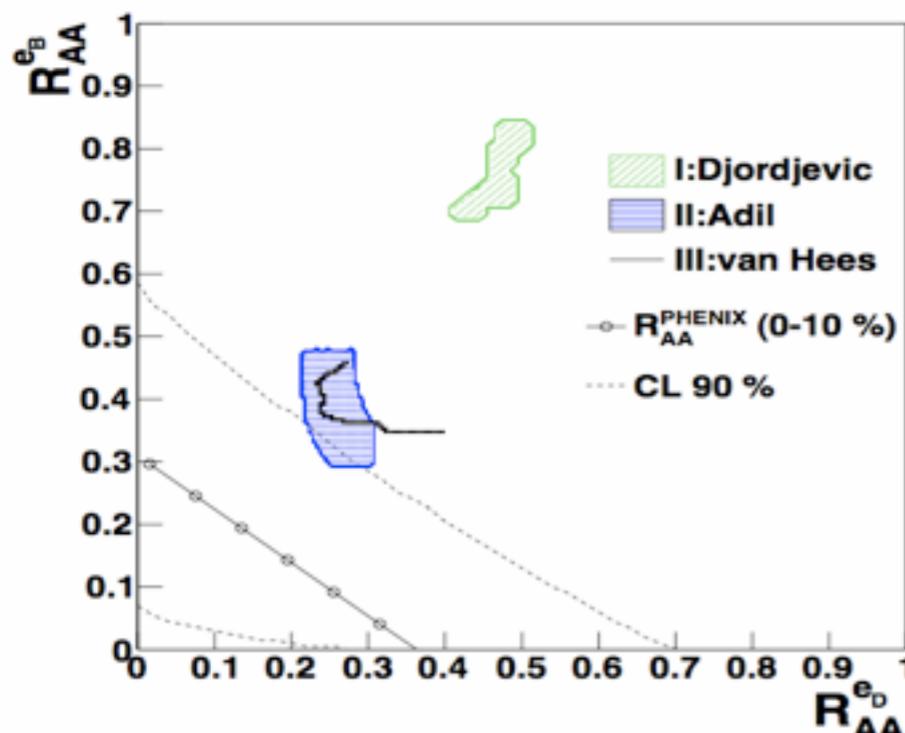


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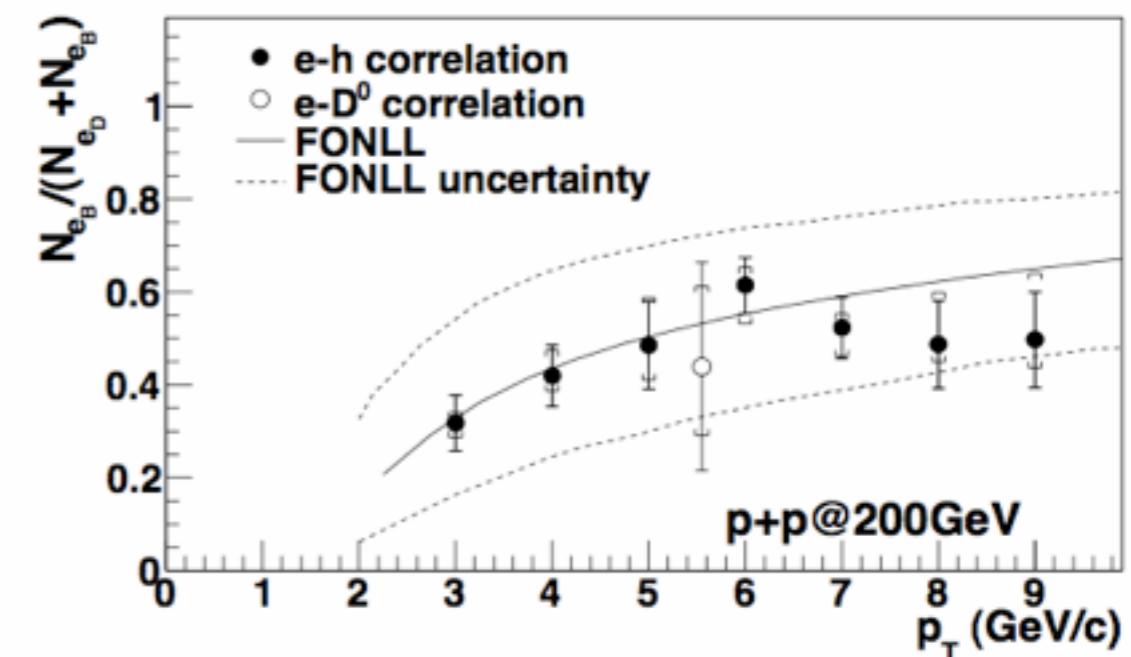
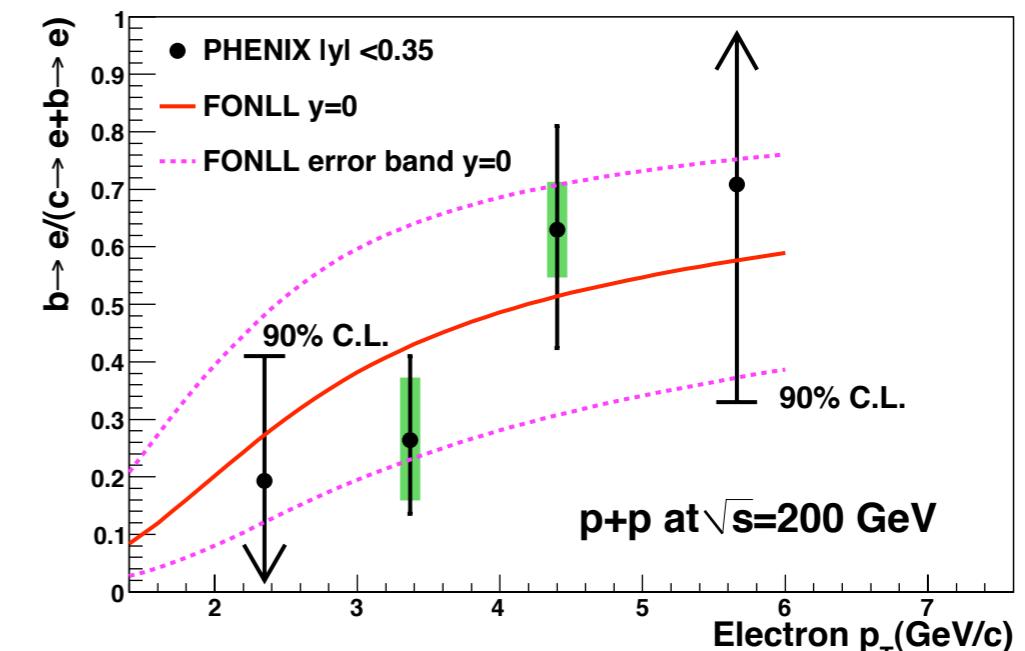
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$$R_{AA}^{\text{HF}} = (1 - r_B) R_{AA}^{e_D} + r_B R_{AA}^{e_B}$$



bottom is suppressed!



PHENIX PRL 103 082002 (2009)
STAR: PRL 105 202301 (2010)

A Roadmap for Hard Probes

A Roadmap for Hard Probes

$\pi^0 R_{AA}$
 $\pi^0 I_{AA}$

A Roadmap for Hard Probes

$\pi^0 R_{AA}$
 $\pi^0 I_{AA}$

→
***control
geometry***

$\pi^0 R_{AA}(\phi)$
 $\pi^0 I_{AA}(\phi)$

A Roadmap for Hard Probes

$\pi^0 R_{AA}$
 $\pi^0 I_{AA}$

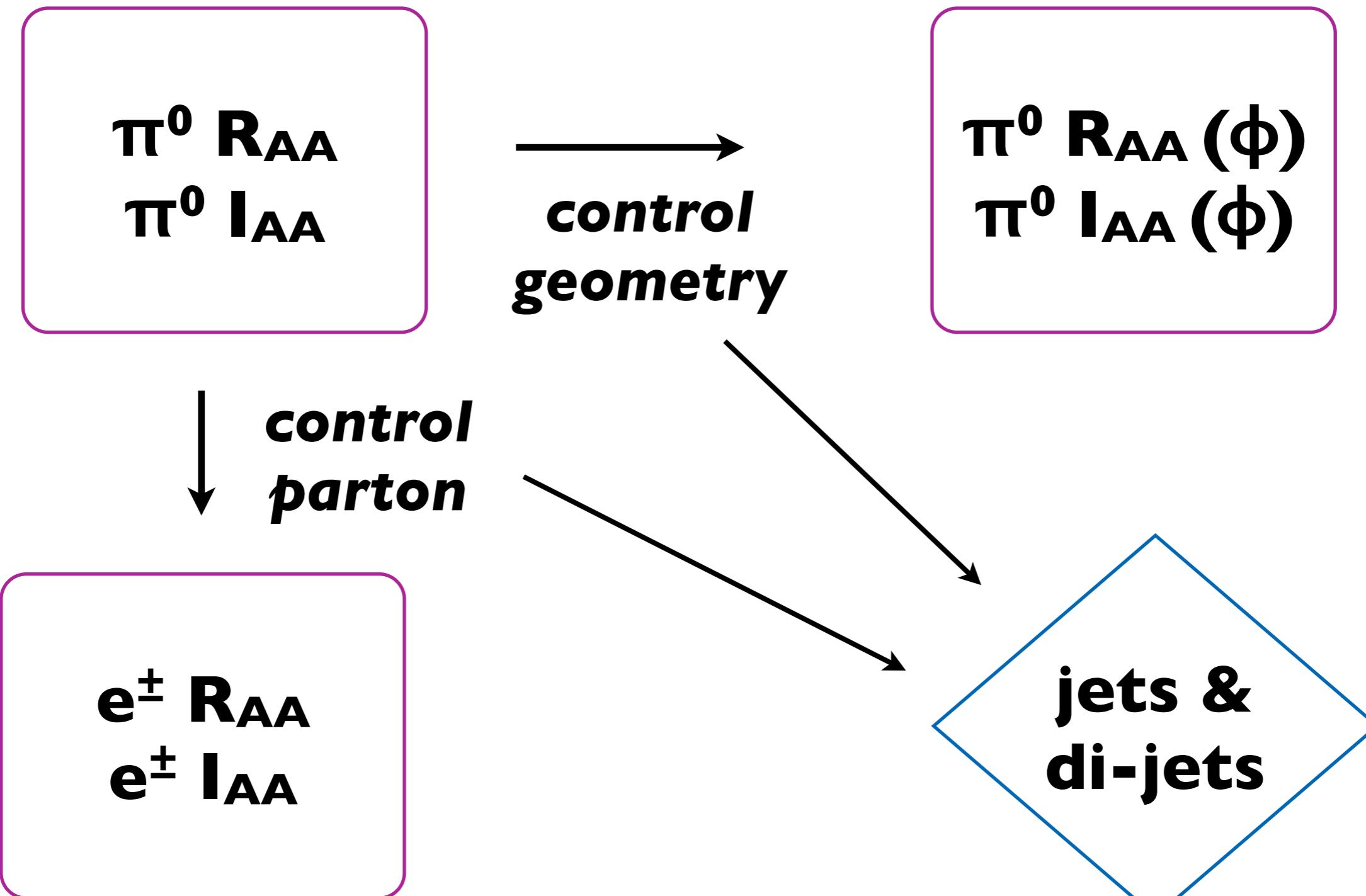
→
***control
geometry***

$\pi^0 R_{AA}(\phi)$
 $\pi^0 I_{AA}(\phi)$

↓
***control
parton***

$e^\pm R_{AA}$
 $e^\pm I_{AA}$

A Roadmap for Hard Probes



A Roadmap for Hard Probes

$\pi^0 R_{AA}$
 $\pi^0 I_{AA}$

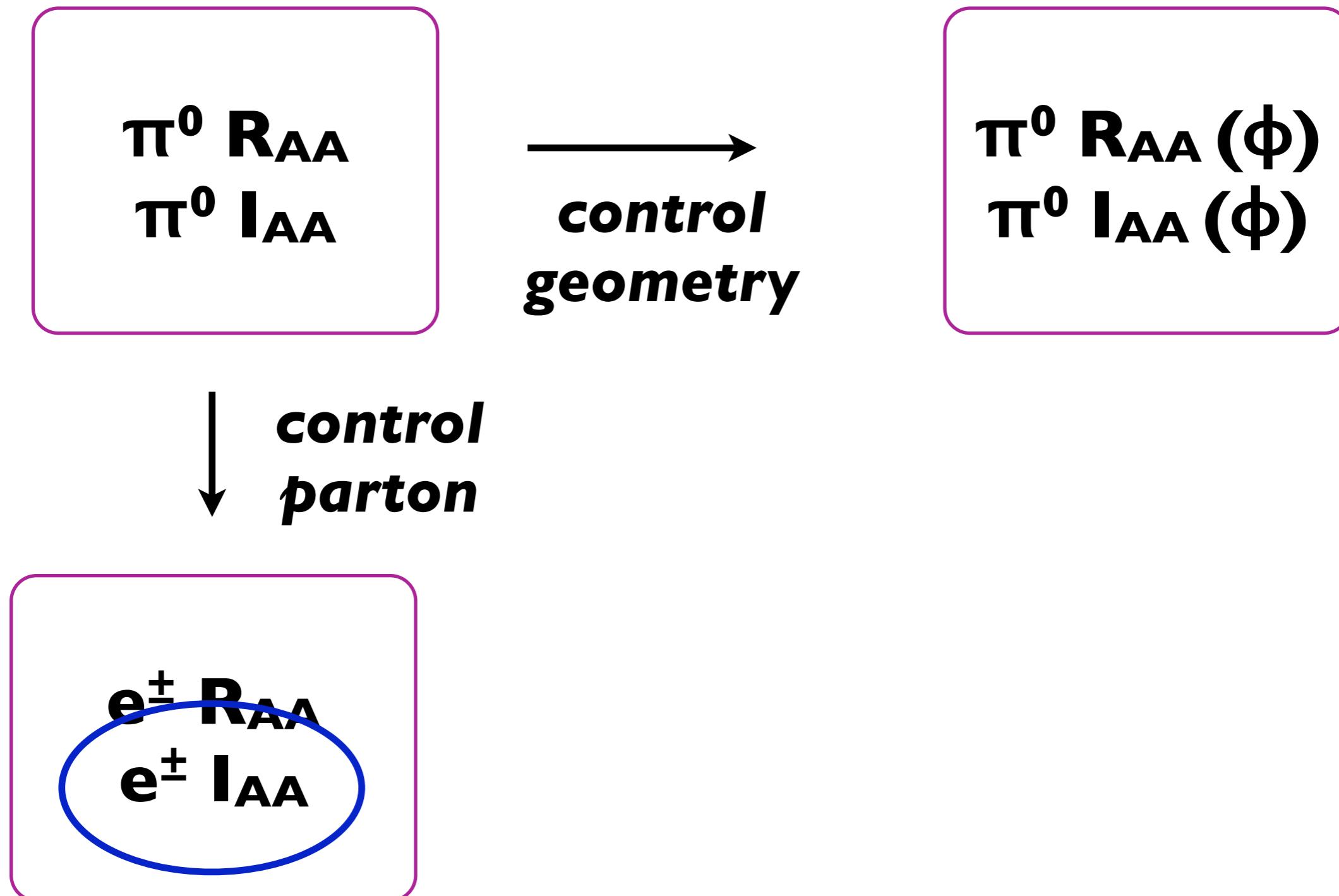
→
***control
geometry***

$\pi^0 R_{AA}(\phi)$
 $\pi^0 I_{AA}(\phi)$

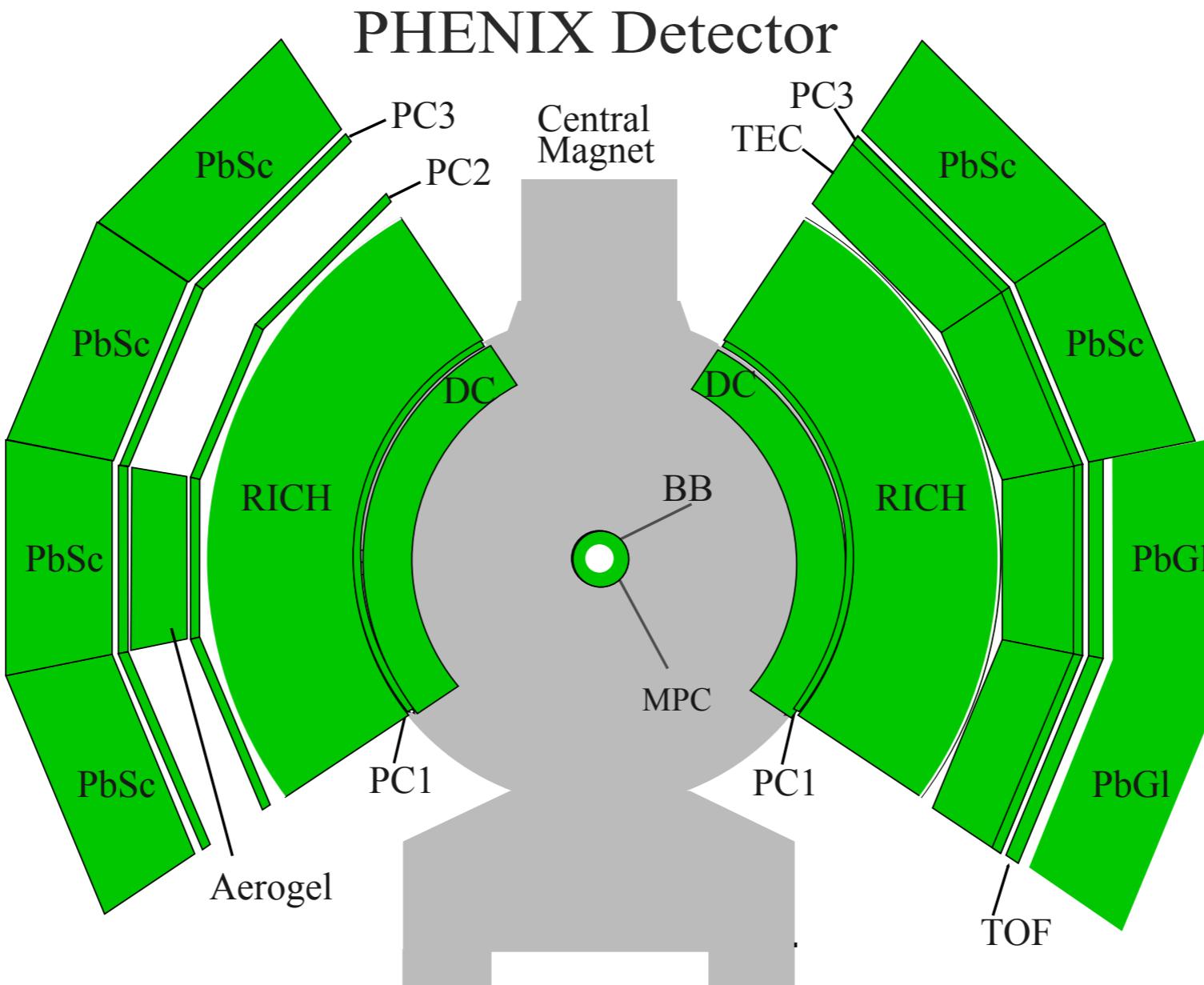
↓
***control
parton***

$e^\pm R_{AA}$
 $e^\pm I_{AA}$

A Roadmap for Hard Probes



Electron Measurement

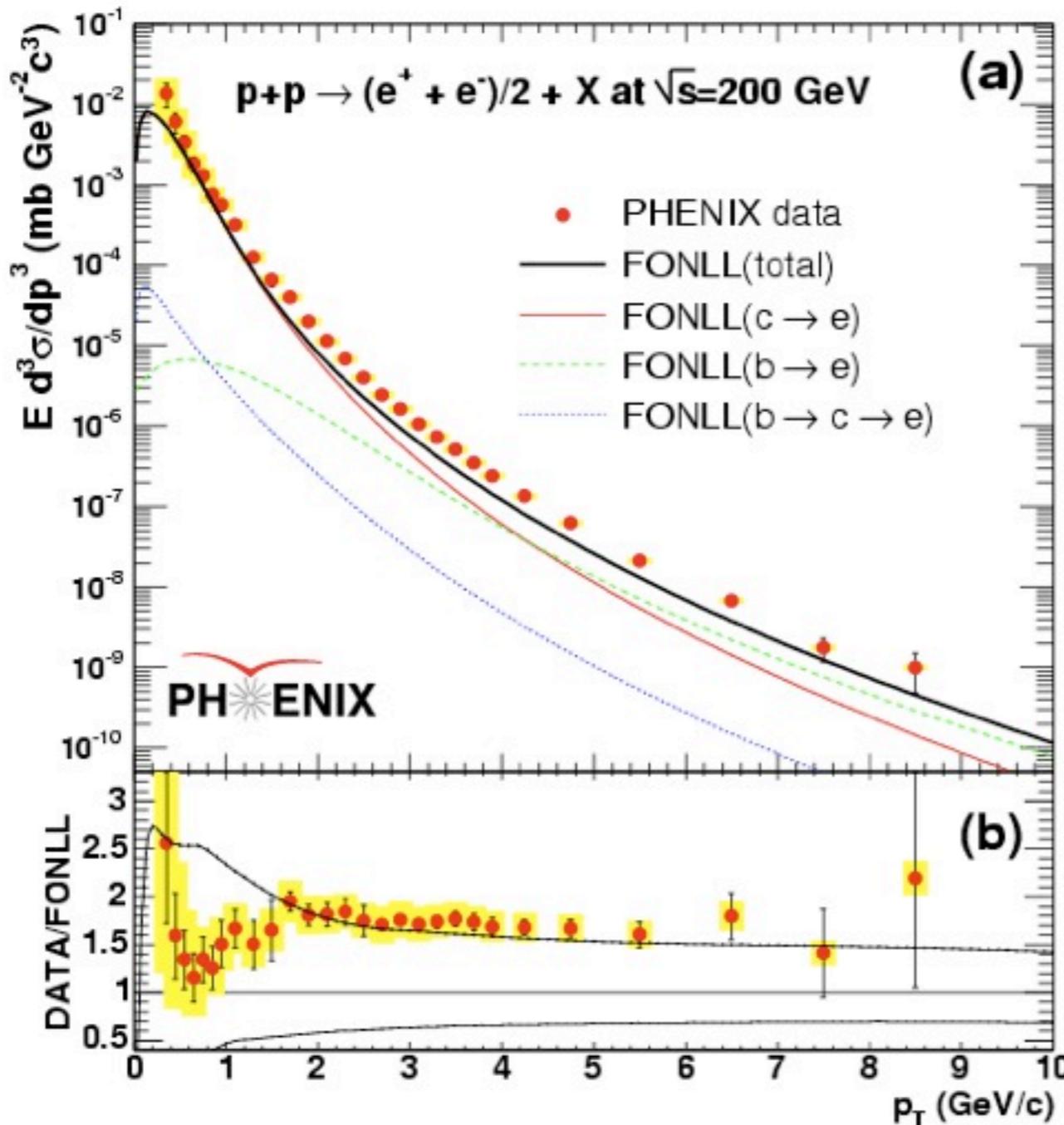


- **electron identification via RICH and EMCal**
- **residual hadron contamination: <1% p+p, <3% Au+Au**

two types of electrons

two types of electrons

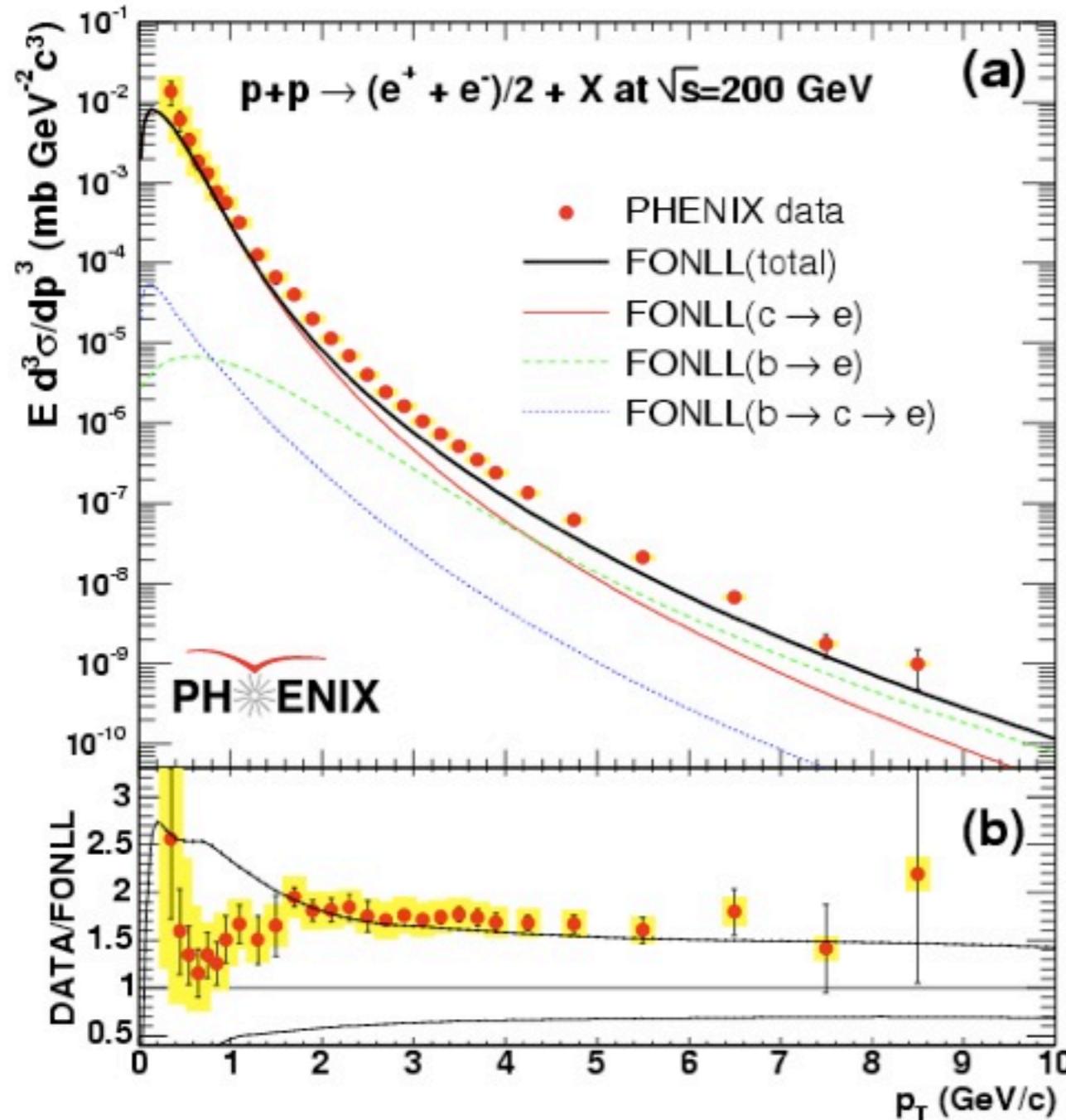
Heavy Flavor



PHENIX, PRL 97 252002 (2006)

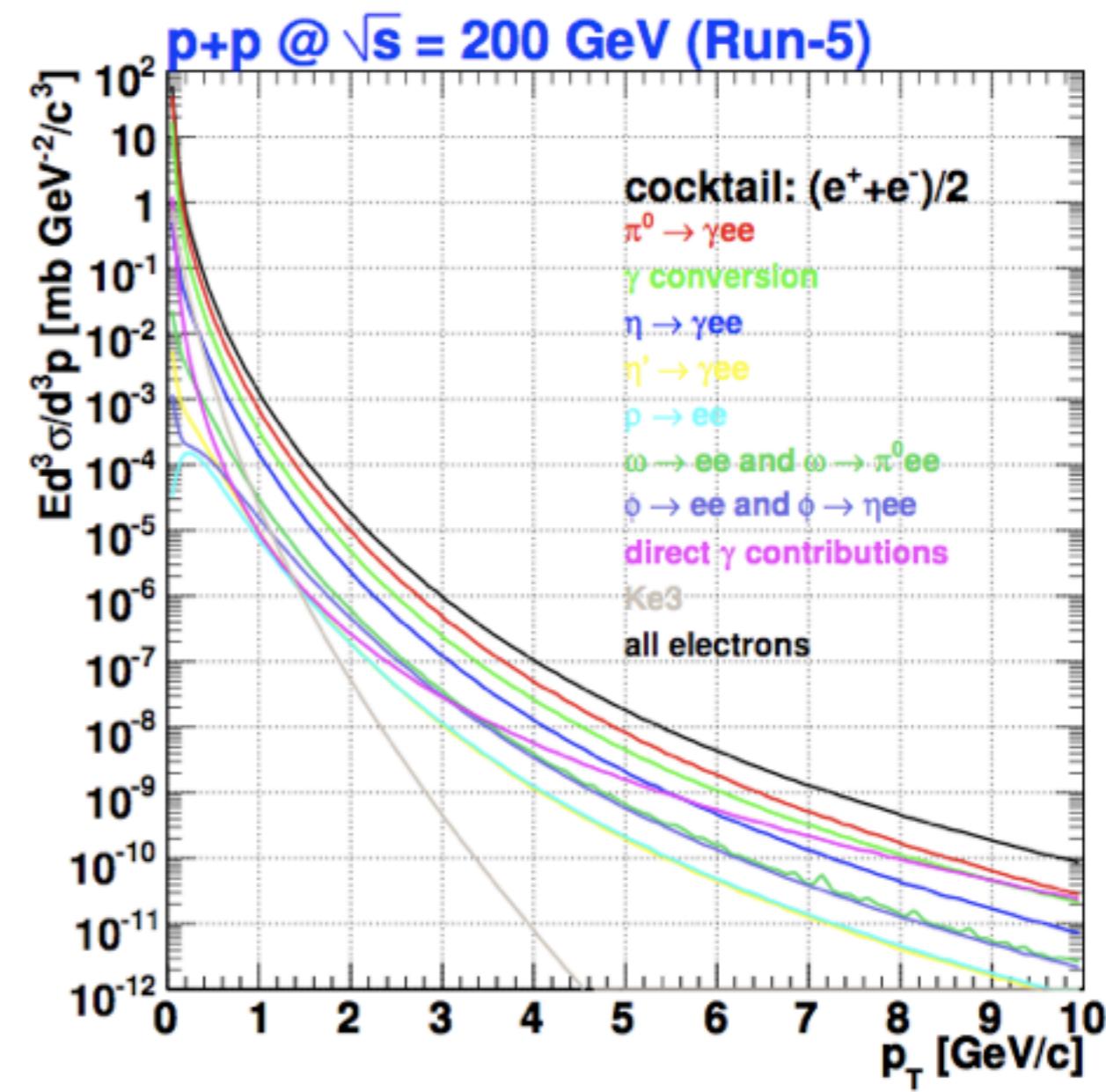
two types of electrons

Heavy Flavor



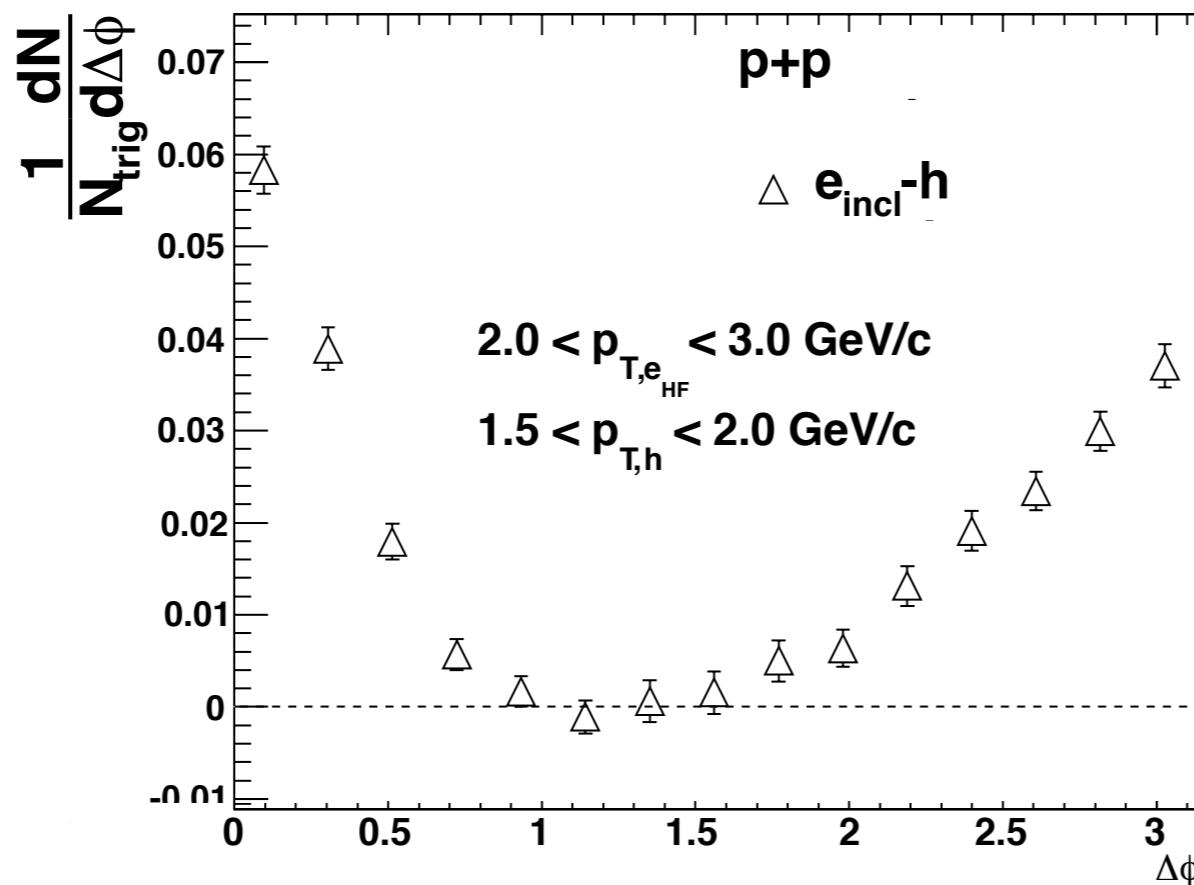
PHENIX, PRL 97 252002 (2006)

Photonic Electrons



inclusive electron correlations

$\gamma_{e_{\text{incl}}-h}$



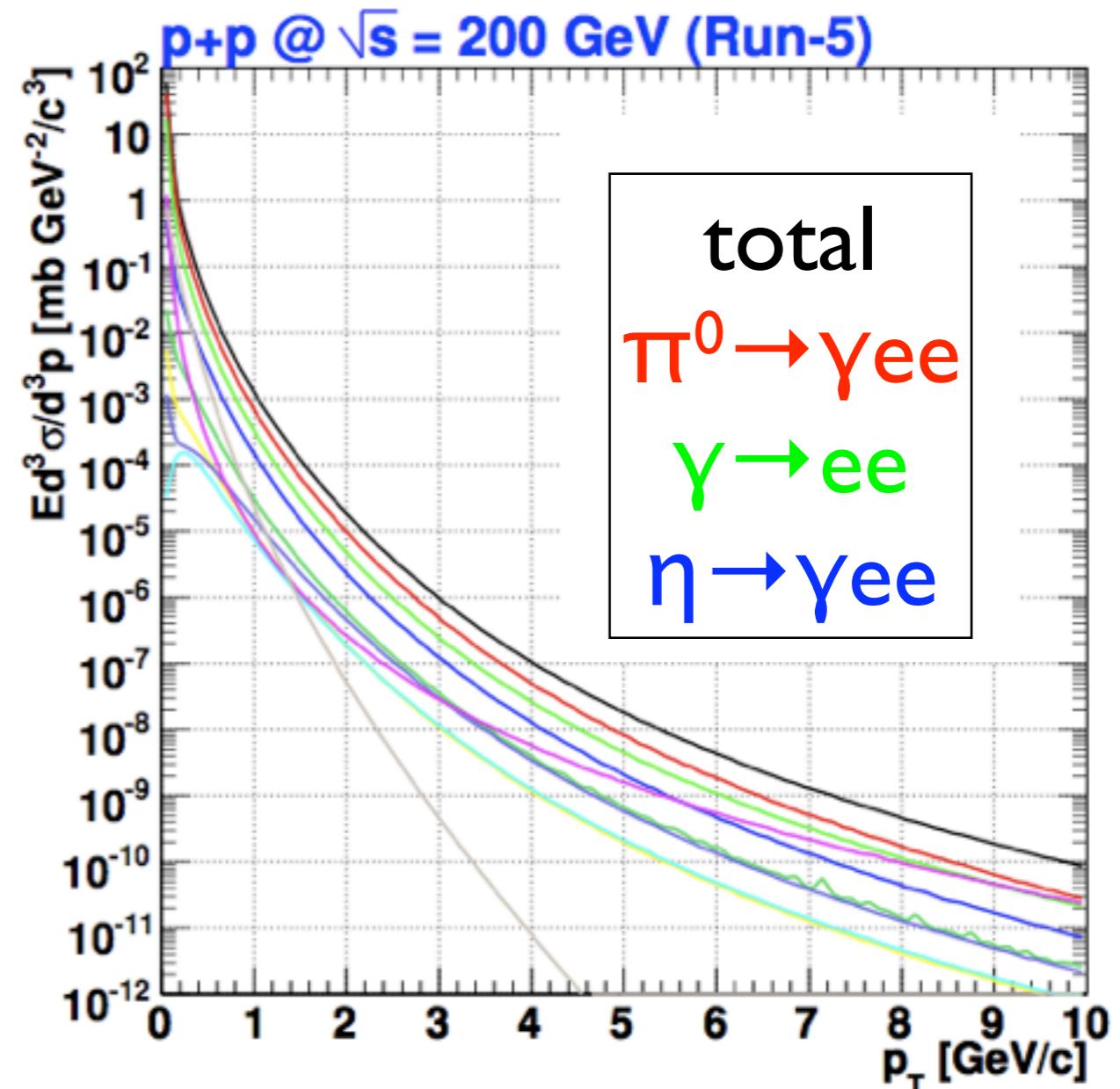
arXiv:1011.1477

photonic electrons

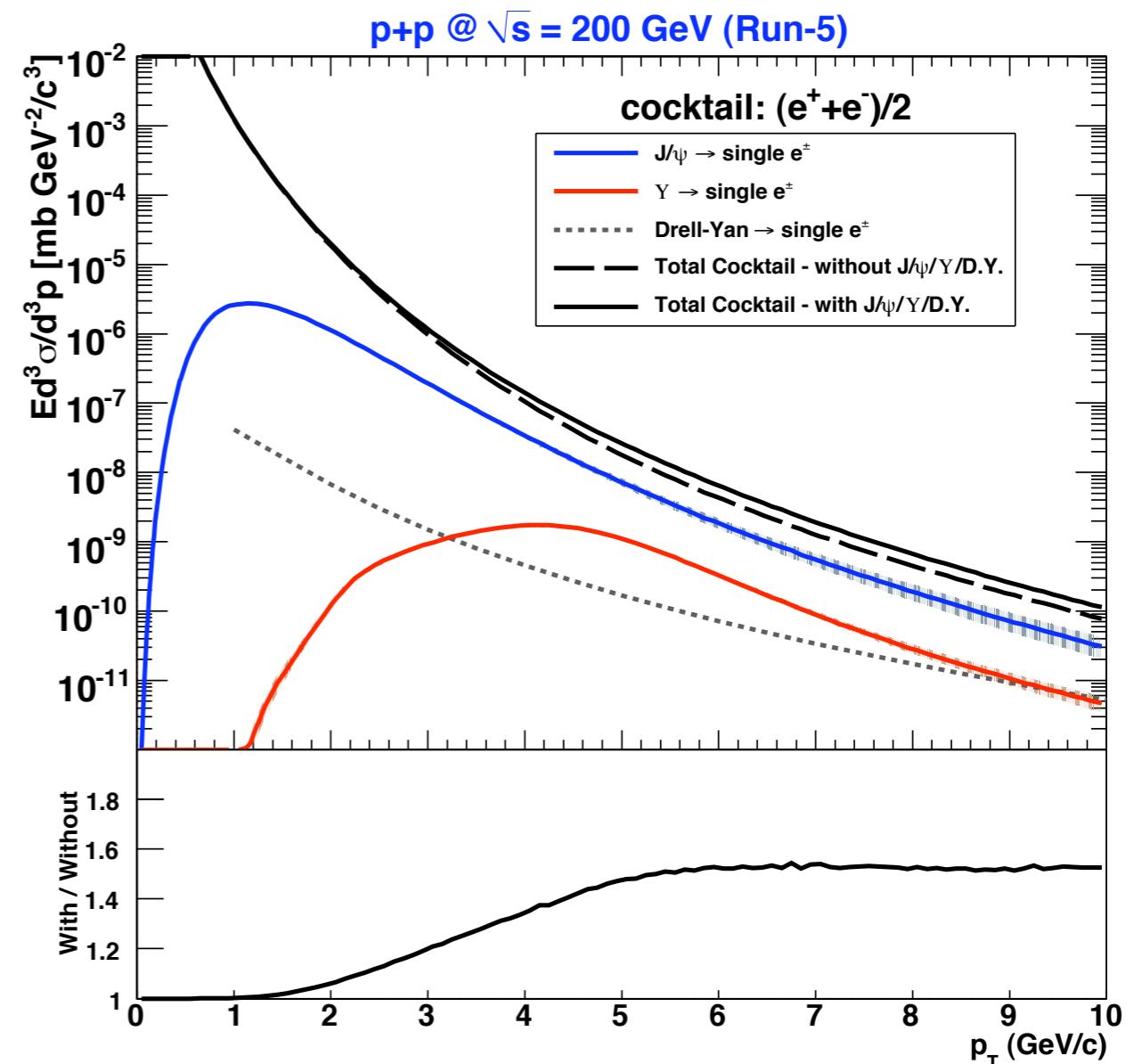
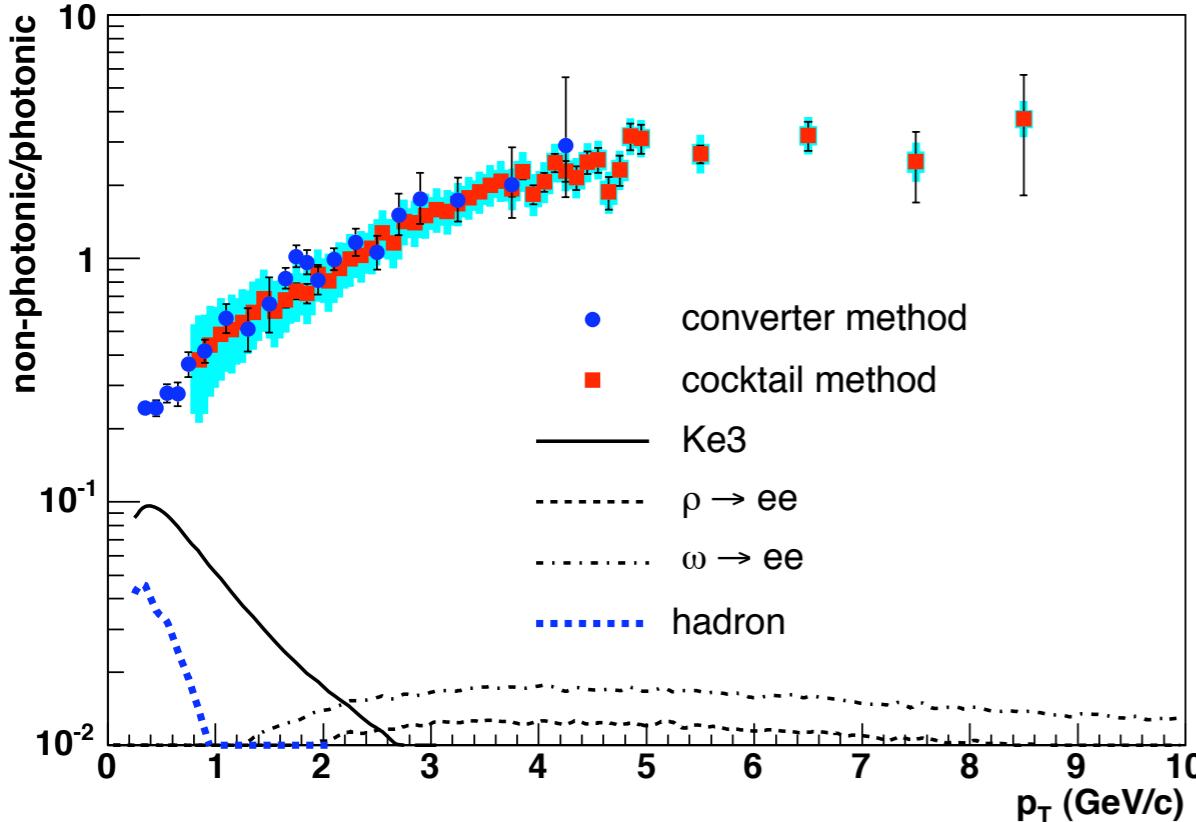
- $p_T < 5 \text{ GeV}/c$:
 - → dominantly from π^0 s
 - measure *photon-h* correlations
 - also dominantly from π^0 s
 - use MC to map between $e_{\text{phot}}(p_T)$ & $\gamma_{\text{inc}}(p_T)$



$$\gamma_{e_{\text{phot}}-h}$$



relative contributions

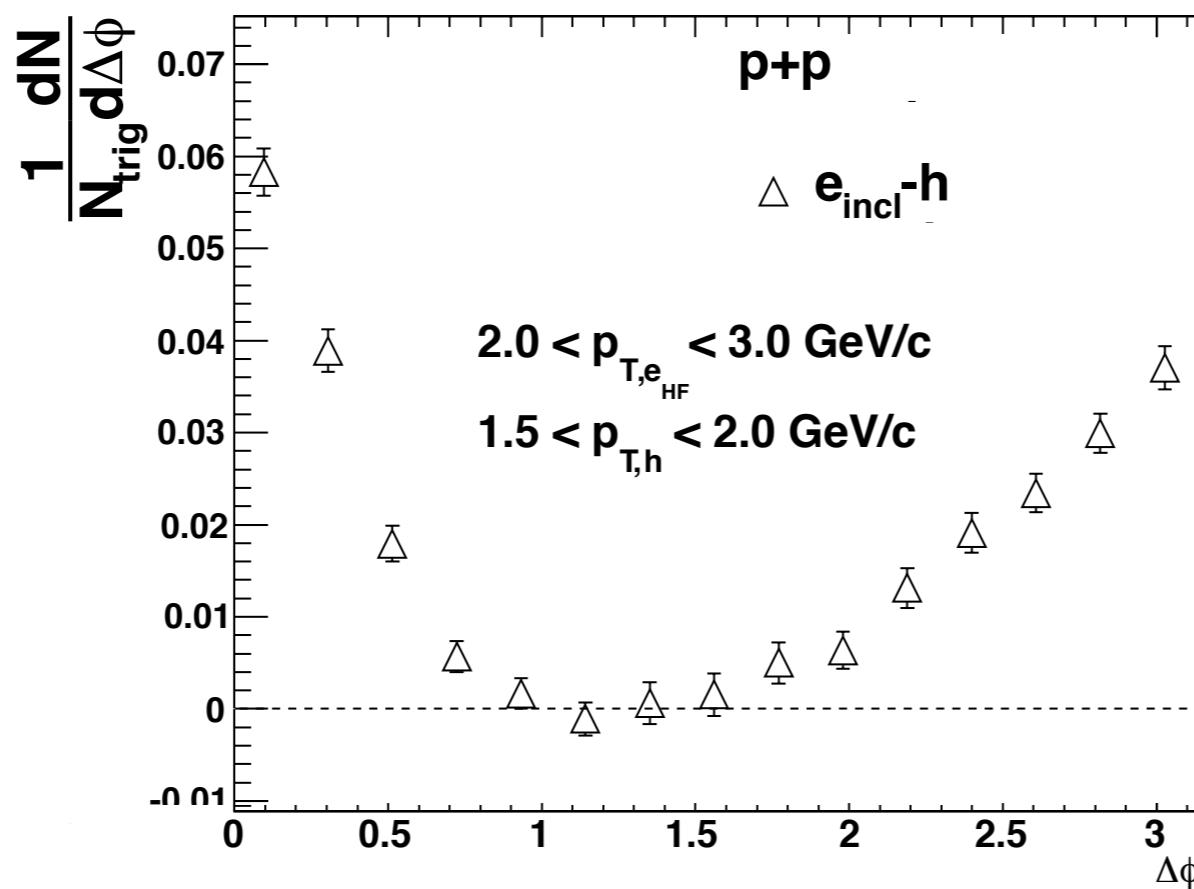


- S/B ~ 1 in the p_T range of interest
- J/ψ contributions also significant toward high p_T

PHENIX PRL 97 252002 (2006)
1005.1627[nucl-ex]

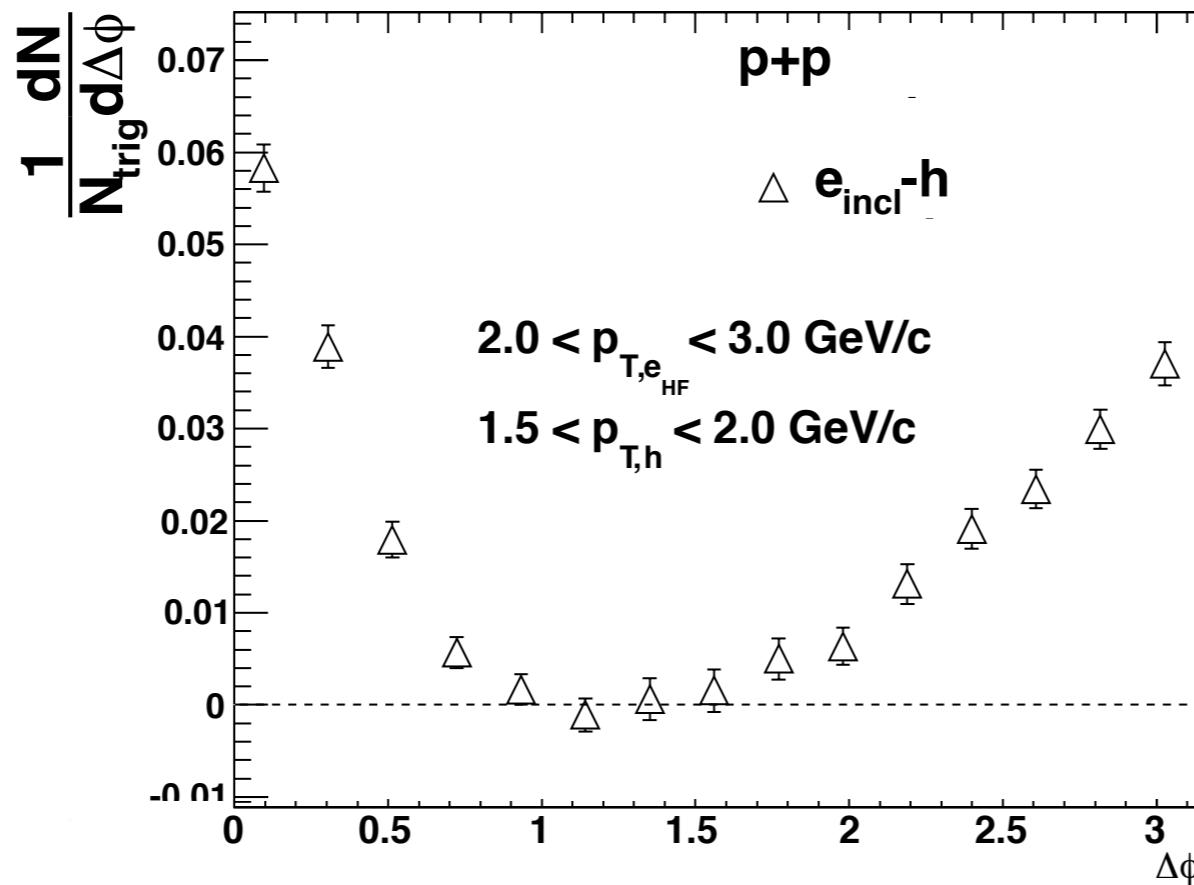
inclusive electron correlations

$\gamma_{e_{incl}-h}$



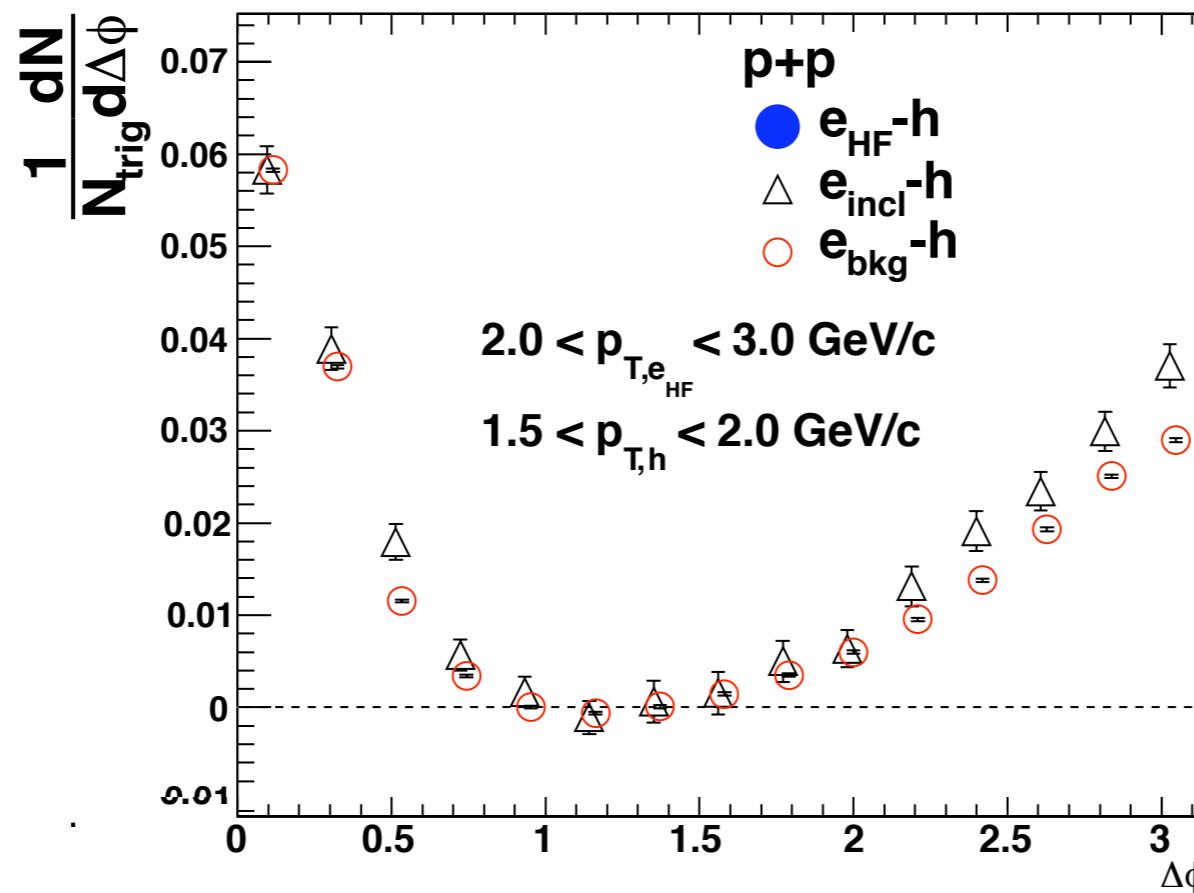
inclusive electron correlations

$$\Upsilon_{e_{incl}-h} = \frac{N_{e_{HF}} \Upsilon_{e_{HF}-h} + N_{e_{bkg}} \Upsilon_{e_{bkg}-h}}{N_{e_{HF}} + N_{e_{bkg}}}$$



inclusive electron correlations

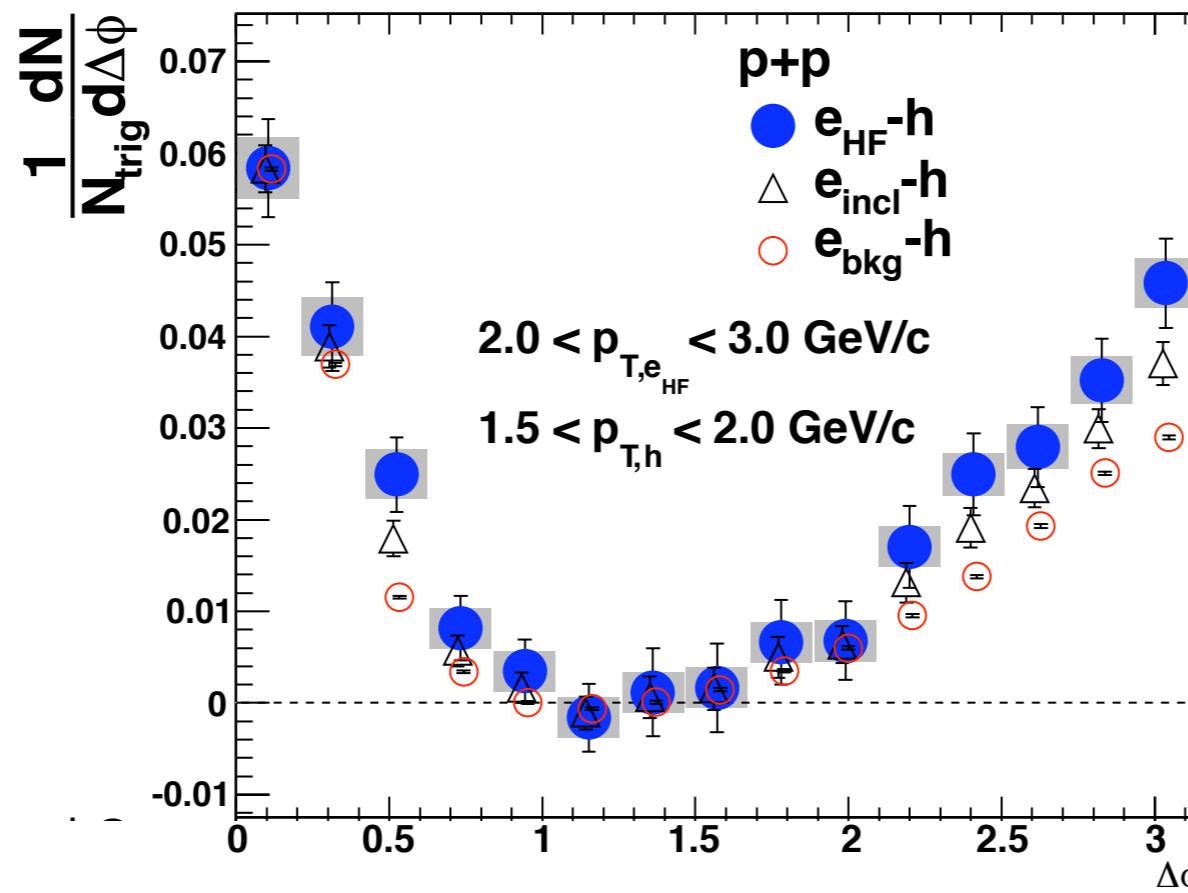
$$\Upsilon_{e_{incl}-h} = \frac{N_{e_{HF}} \Upsilon_{e_{HF}-h} + N_{e_{bkg}} \Upsilon_{e_{bkg}-h}}{N_{e_{HF}} + N_{e_{bkg}}}$$



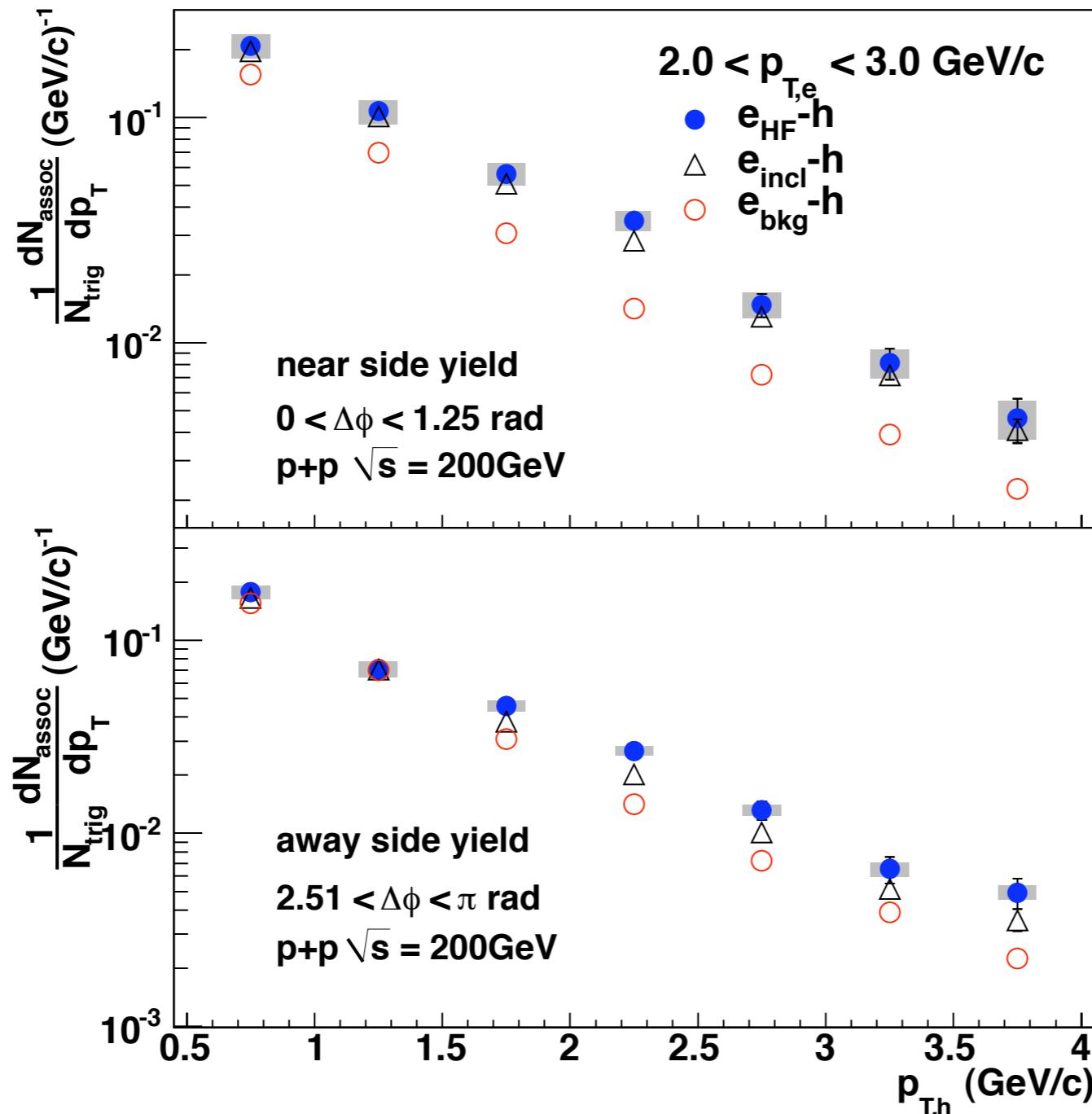
arXiv:1011.1477

inclusive electron correlations

$$\Upsilon_{e_{incl}-h} = \frac{N_{e_{HF}} \Upsilon_{e_{HF}-h} + N_{e_{bkg}} \Upsilon_{e_{bkg}-h}}{N_{e_{HF}} + N_{e_{bkg}}}$$

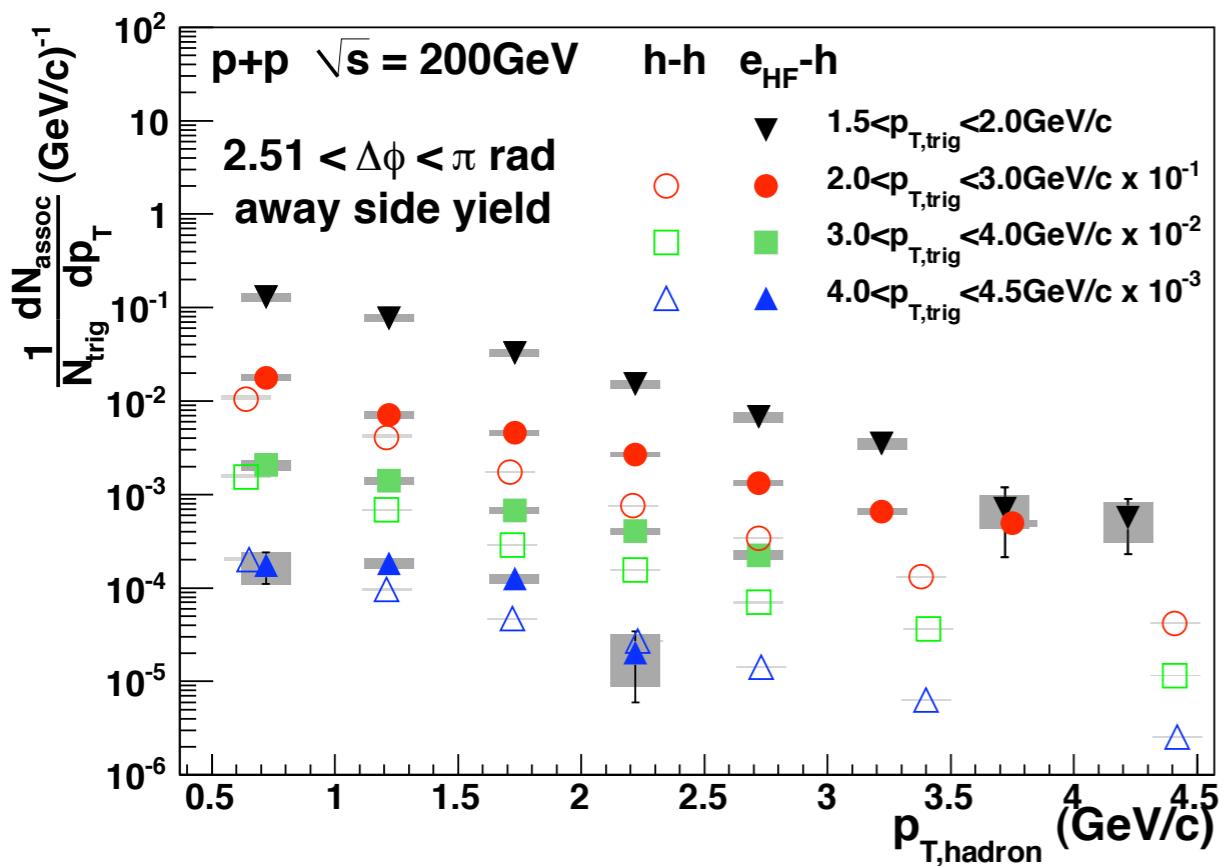


jet-like correlations

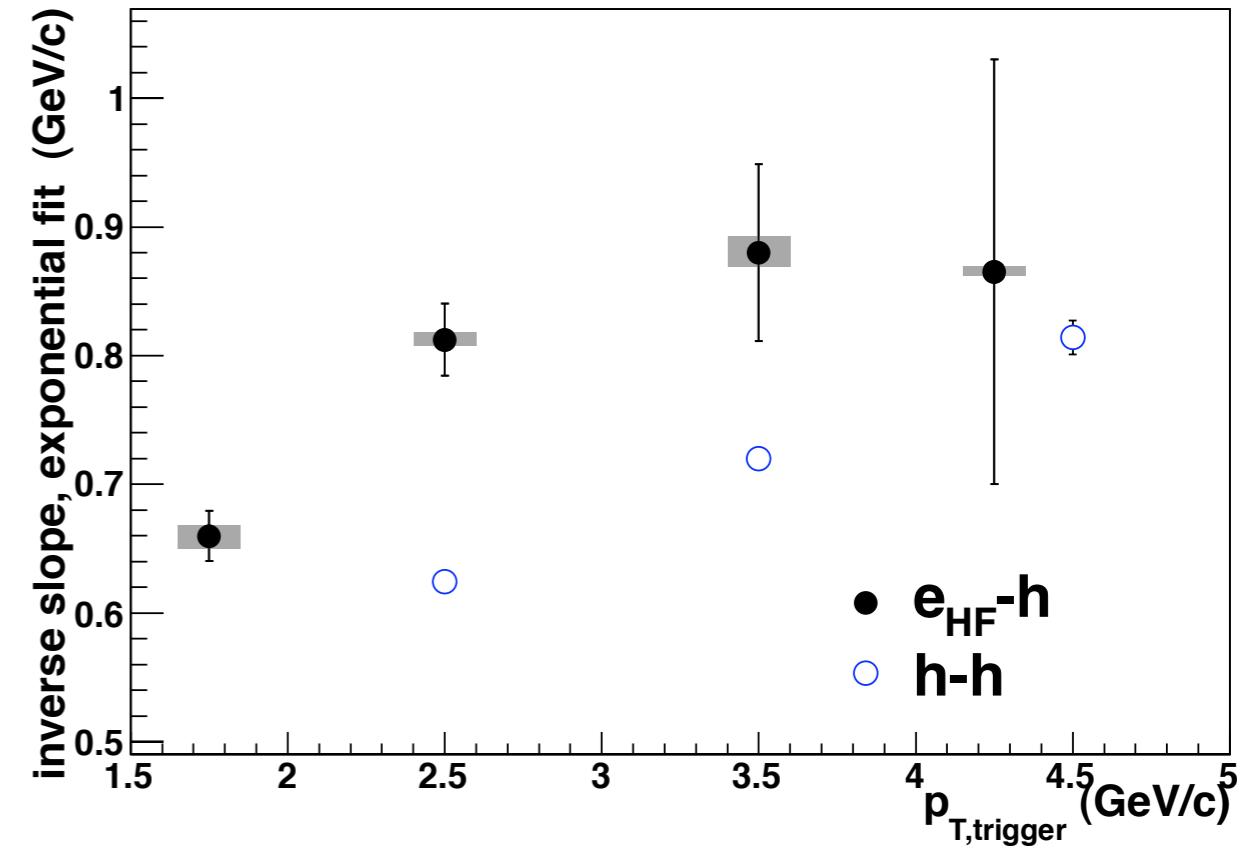
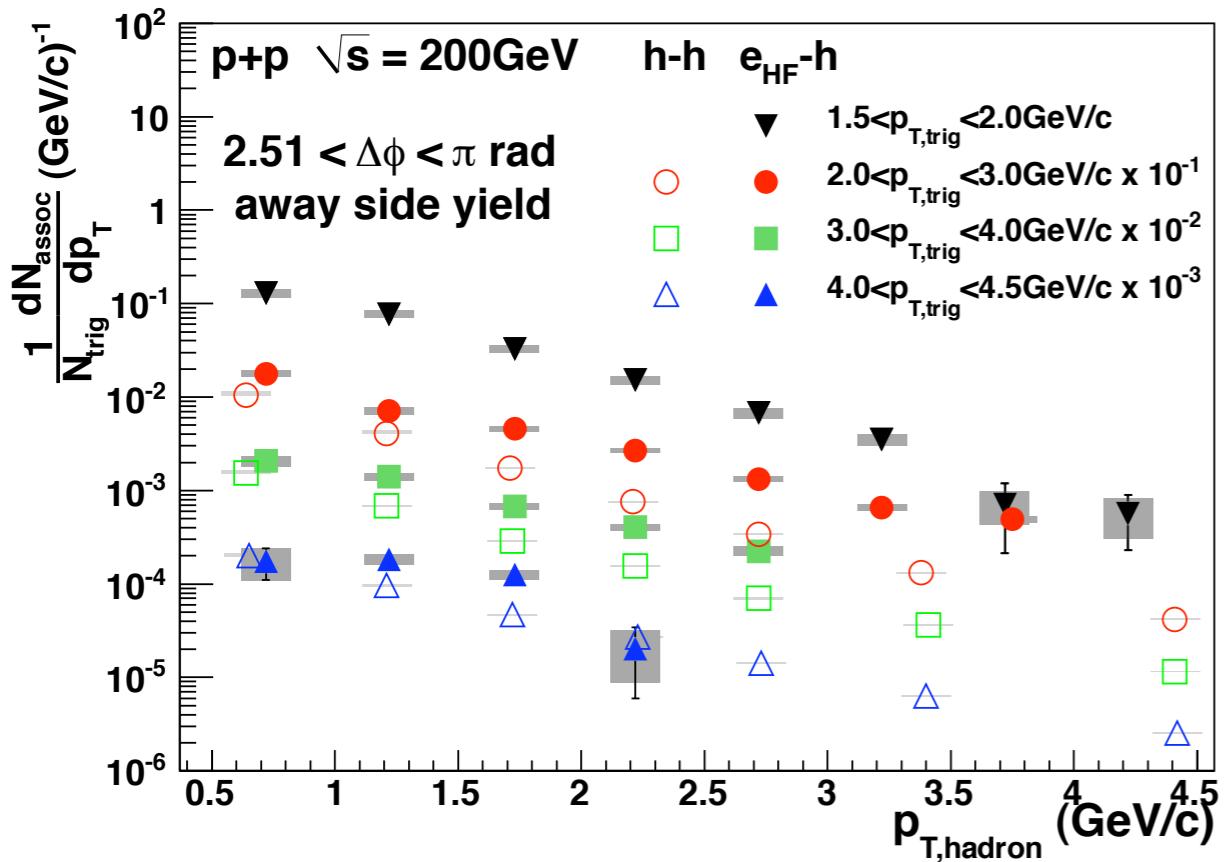


PHENIX: 1011.1477

p+p alone...



p+p alone...



p+p alone...

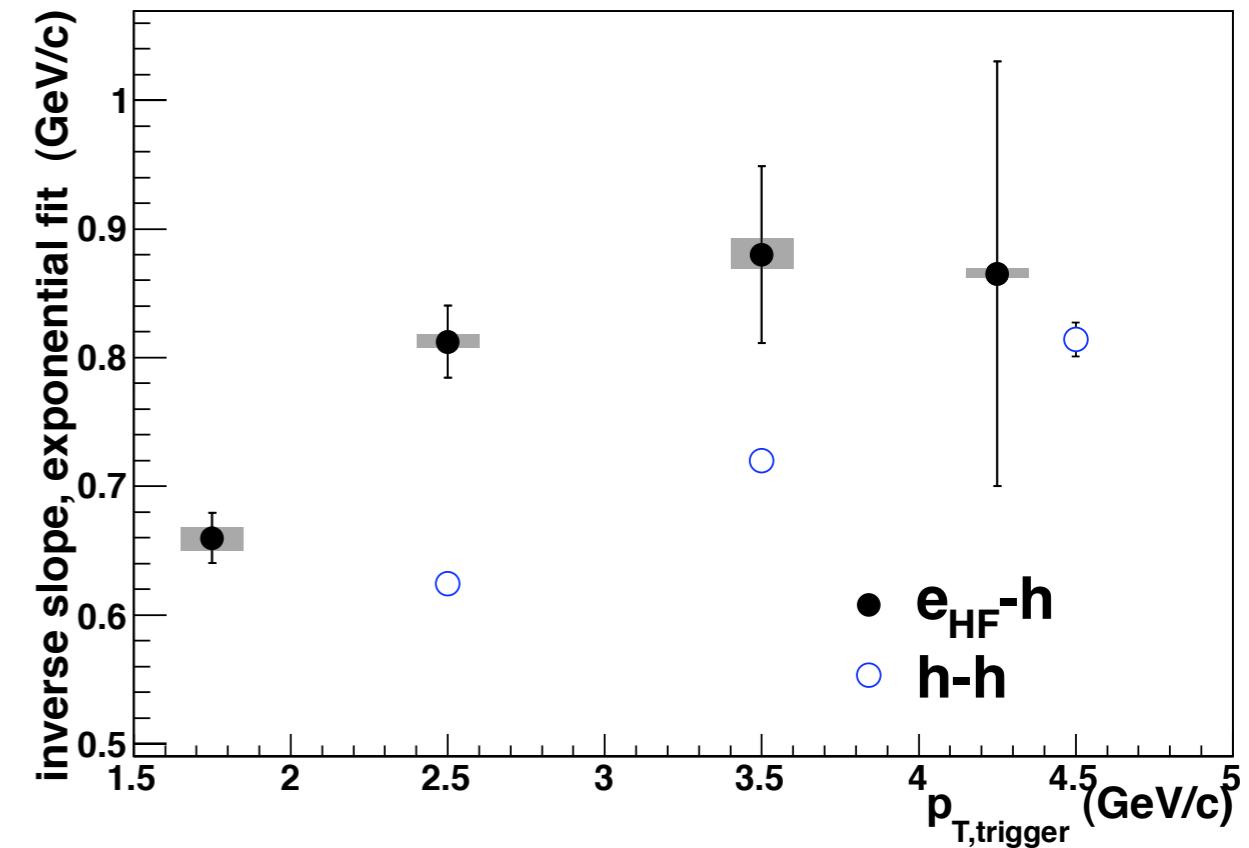
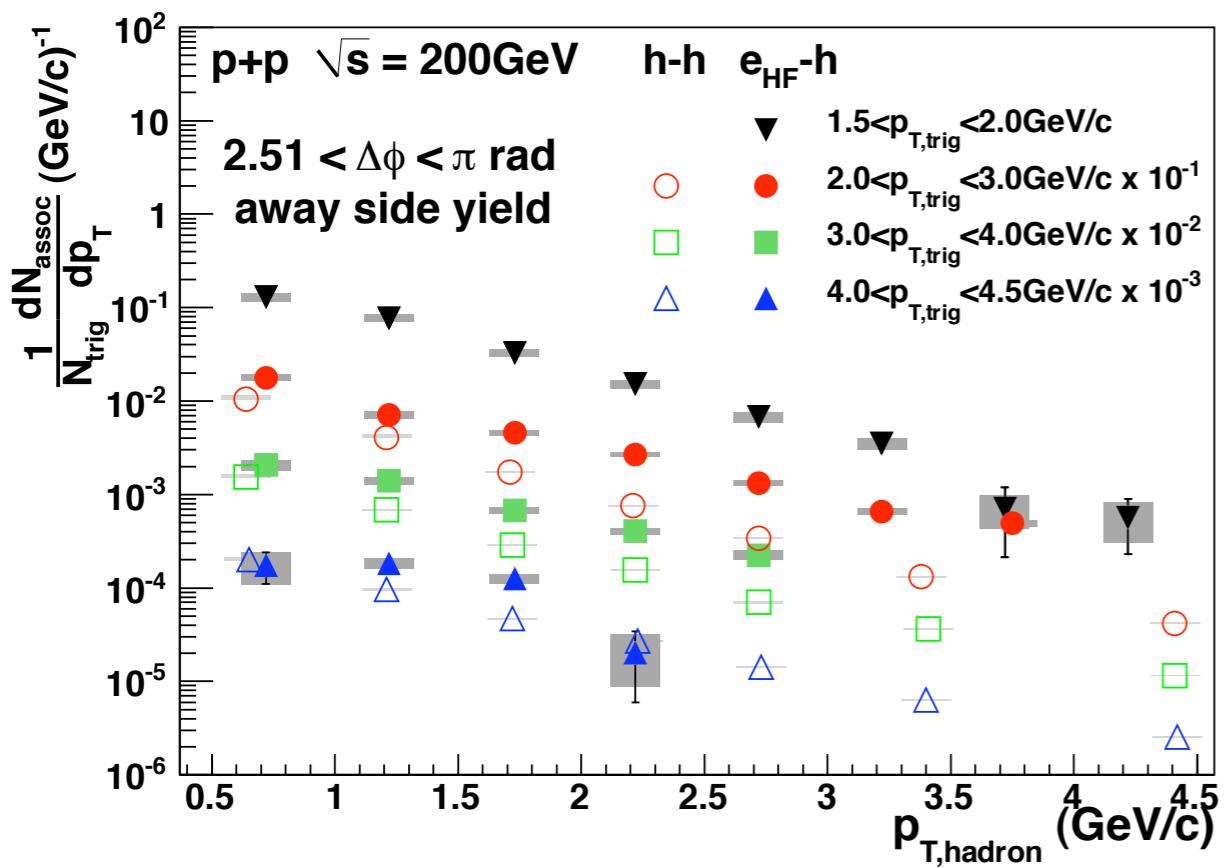


TABLE III: Mean transverse momentum of the parent D and B mesons contributing to the heavy-flavor electron p_T bins used here. They are combined according to the fraction of heavy-flavor electrons from b quarks, $\frac{b \rightarrow e}{(c \rightarrow e + b \rightarrow e)}$ according to the FONLL calculations [31] (as shown in Ref. [29]) to determine the mean heavy meson transverse momentum.

$p_{T,e}$ (GeV/c)	$\langle p_T \rangle_D$ (GeV/c)	$\langle p_T \rangle_B$ (GeV/c)	$\frac{b \rightarrow e}{(c \rightarrow e + b \rightarrow e)}$	$\langle p_T \rangle_{\text{meson}}$ (GeV/c)
1.5-2.0	3.4	4.4	0.15	3.6
2.0-3.0	4.1	4.7	0.26	4.3
3.0-4.0	5.6	5.6	0.42	5.6

p+p alone...

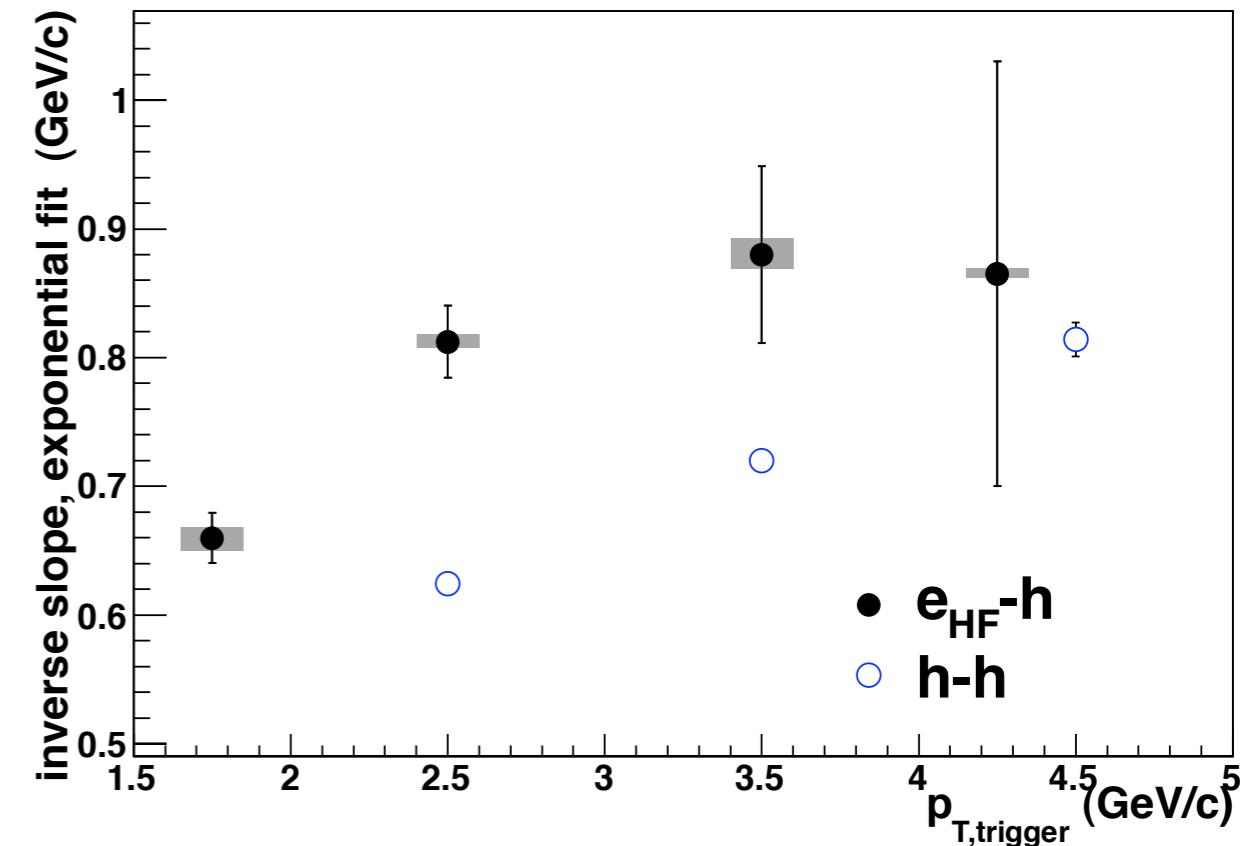
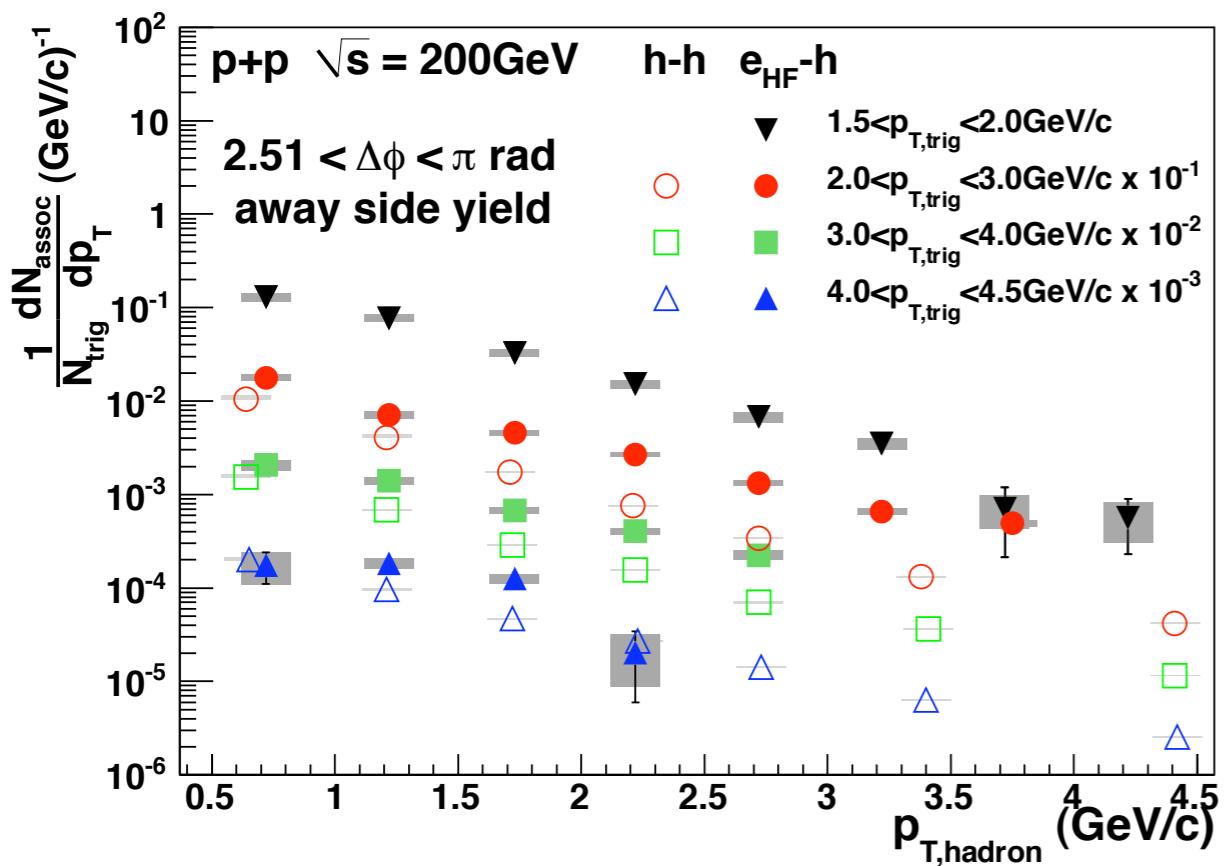
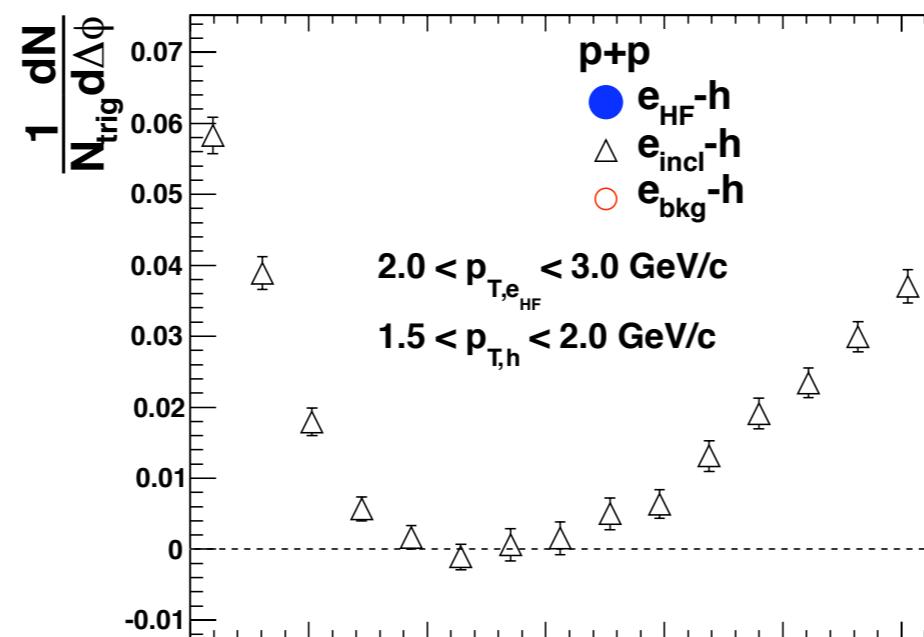
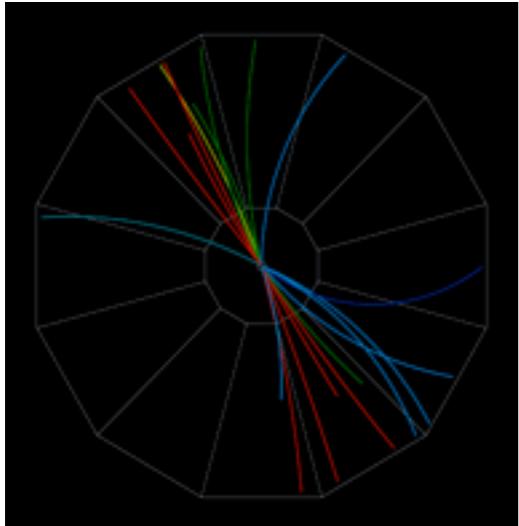


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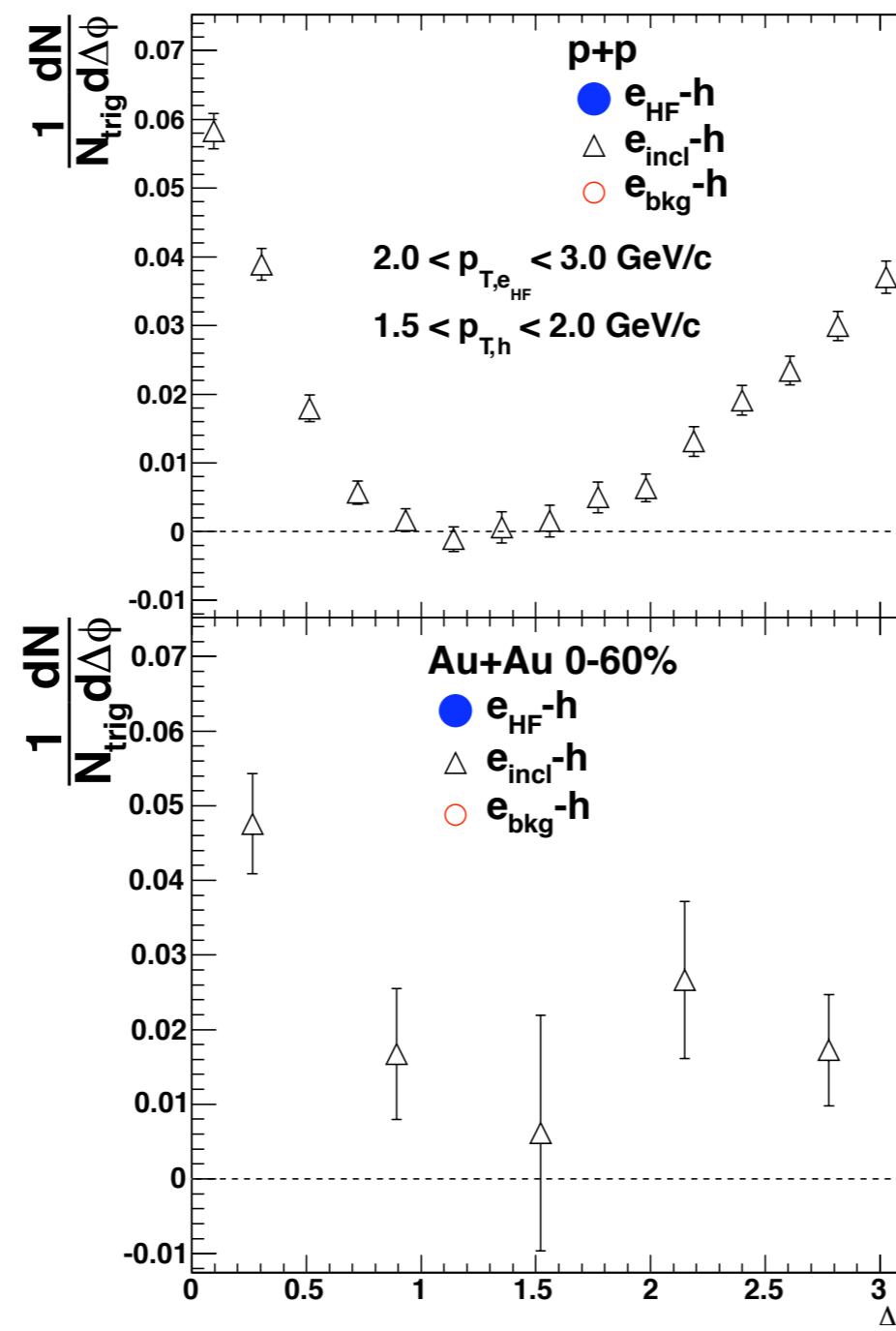
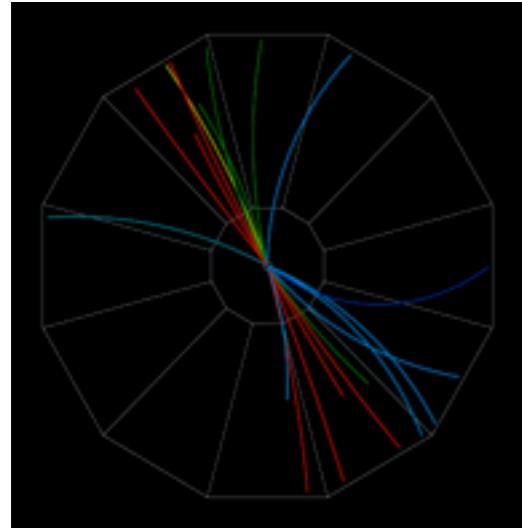
$p_{T,e}$ (GeV/c)	$\langle p_T \rangle_D$ (GeV/c)	$\langle p_T \rangle_B$ (GeV/c)	$\frac{b \rightarrow e}{(c \rightarrow e + b \rightarrow e)}$	$\langle p_T \rangle_{meson}$ (GeV/c)
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2.0-3.0	4.1	4.7	0.26	4.3
3.0-4.0	5.6	5.6	0.42	5.6

combinatorial background



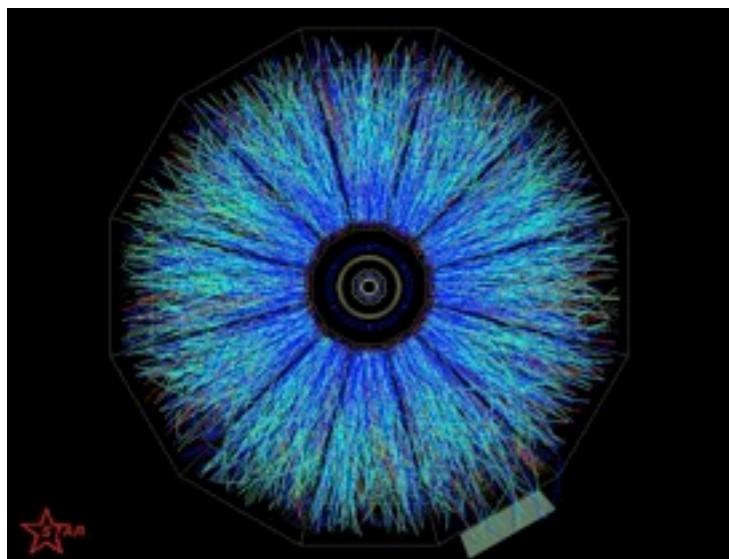
jet S/B > 1

combinatorial background



jet S/B > 1

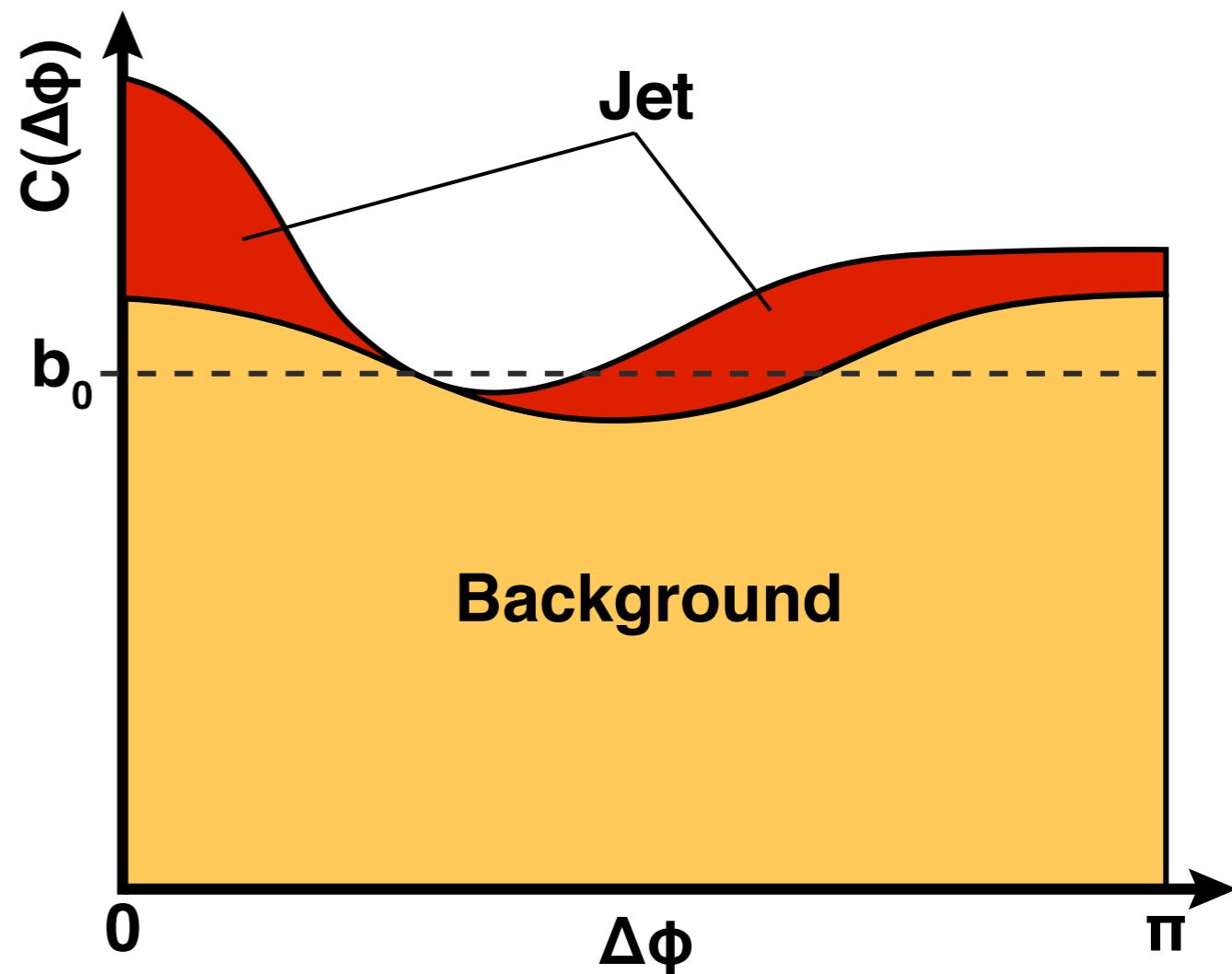
jet S/B ~ 1%



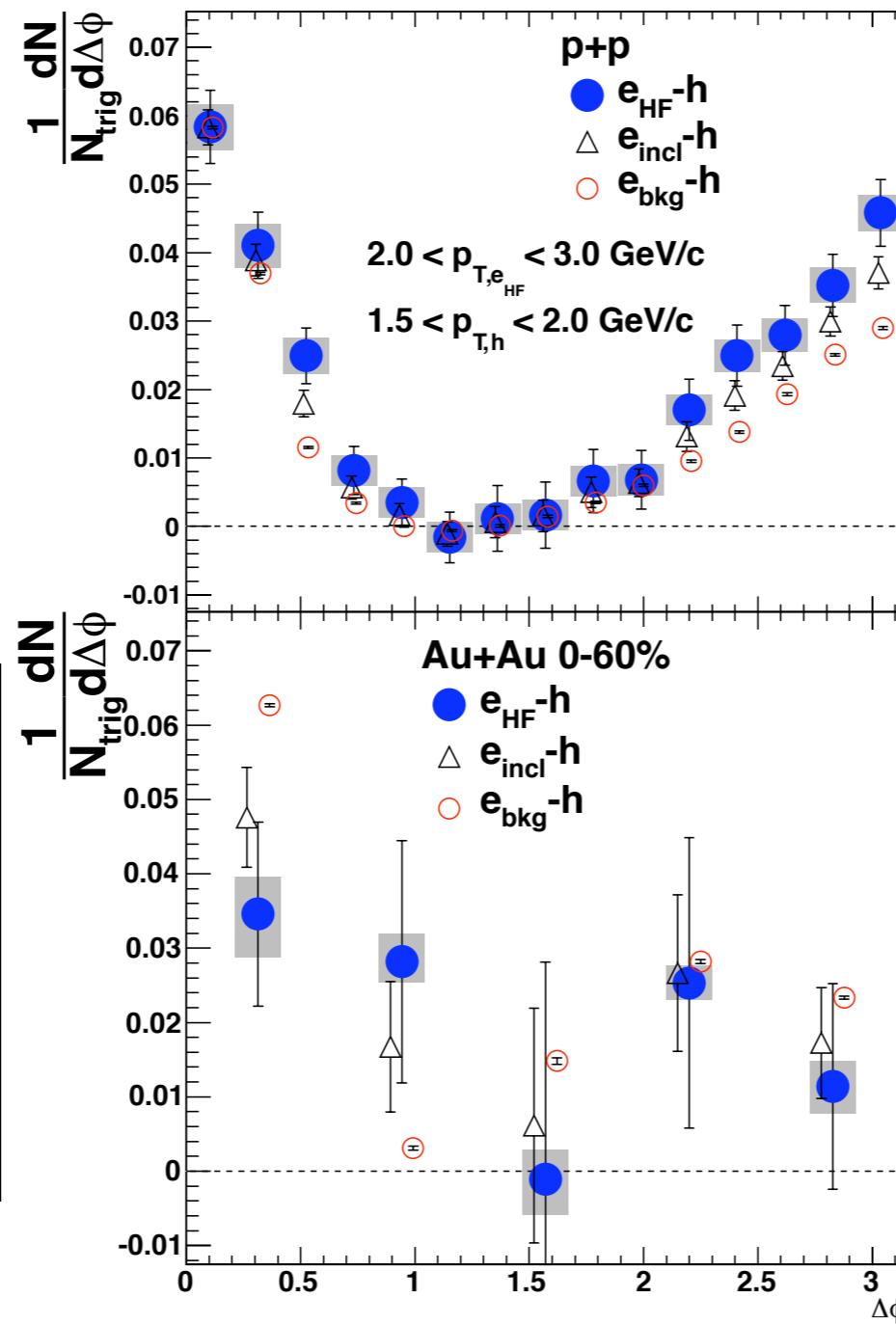
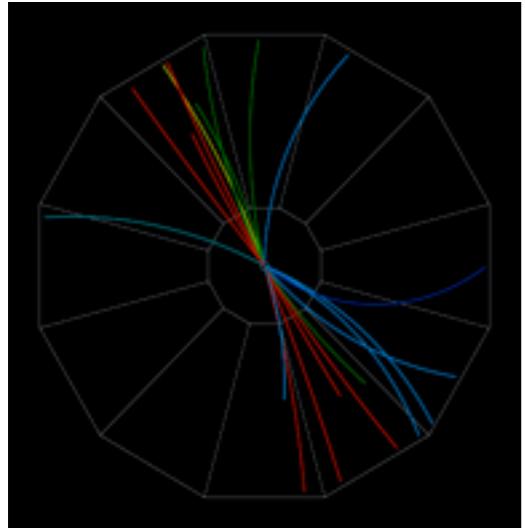
absolute background subtraction

$$\text{combinatorial background} = b_0(1 + 2v_2 A v_2 B \cos(2\Delta\phi))$$

- b_0 can be calculated in HI collisions (no fudge factors) w/ negligible statistical errors
 - depends on the centrality fluctuations
- generally very close to ZYAM, however some significant advantages
 - wide jets
 - poor statistics

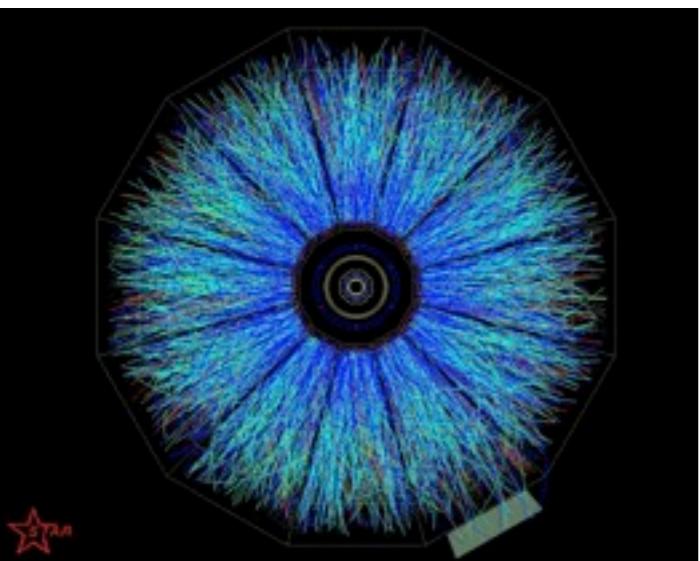


combinatorial background

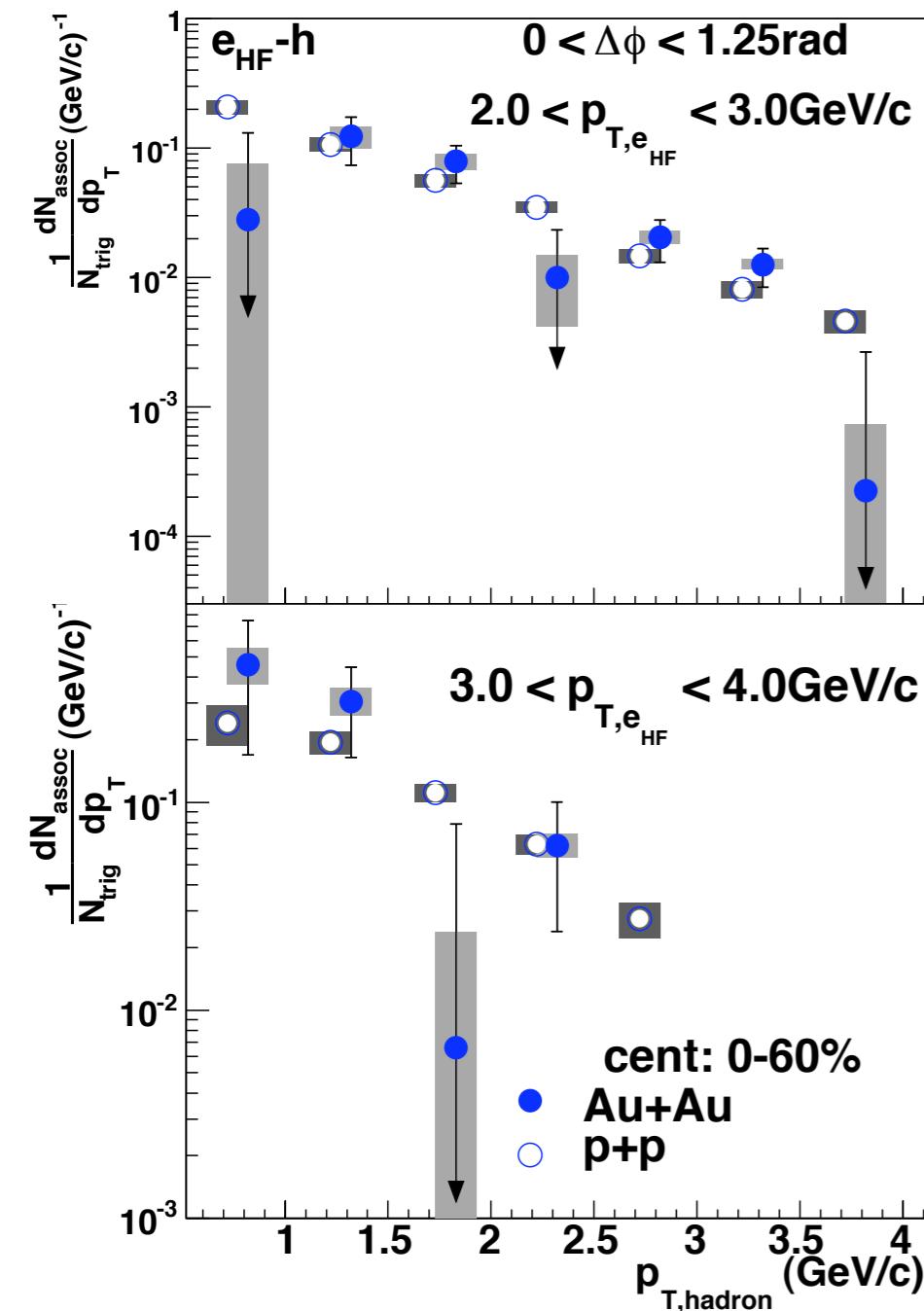


jet S/B > 1

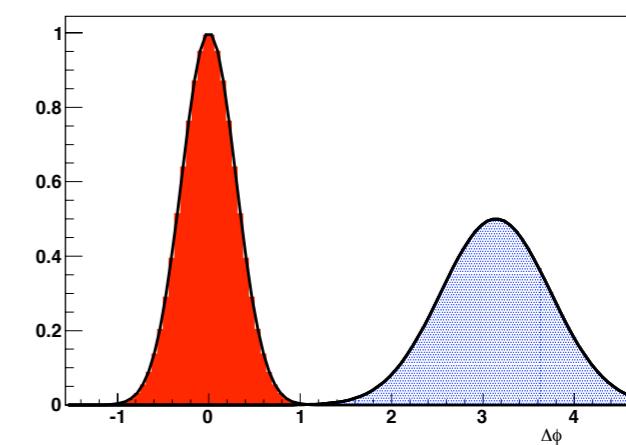
jet S/B ~ 1%



e-h: same side correlations

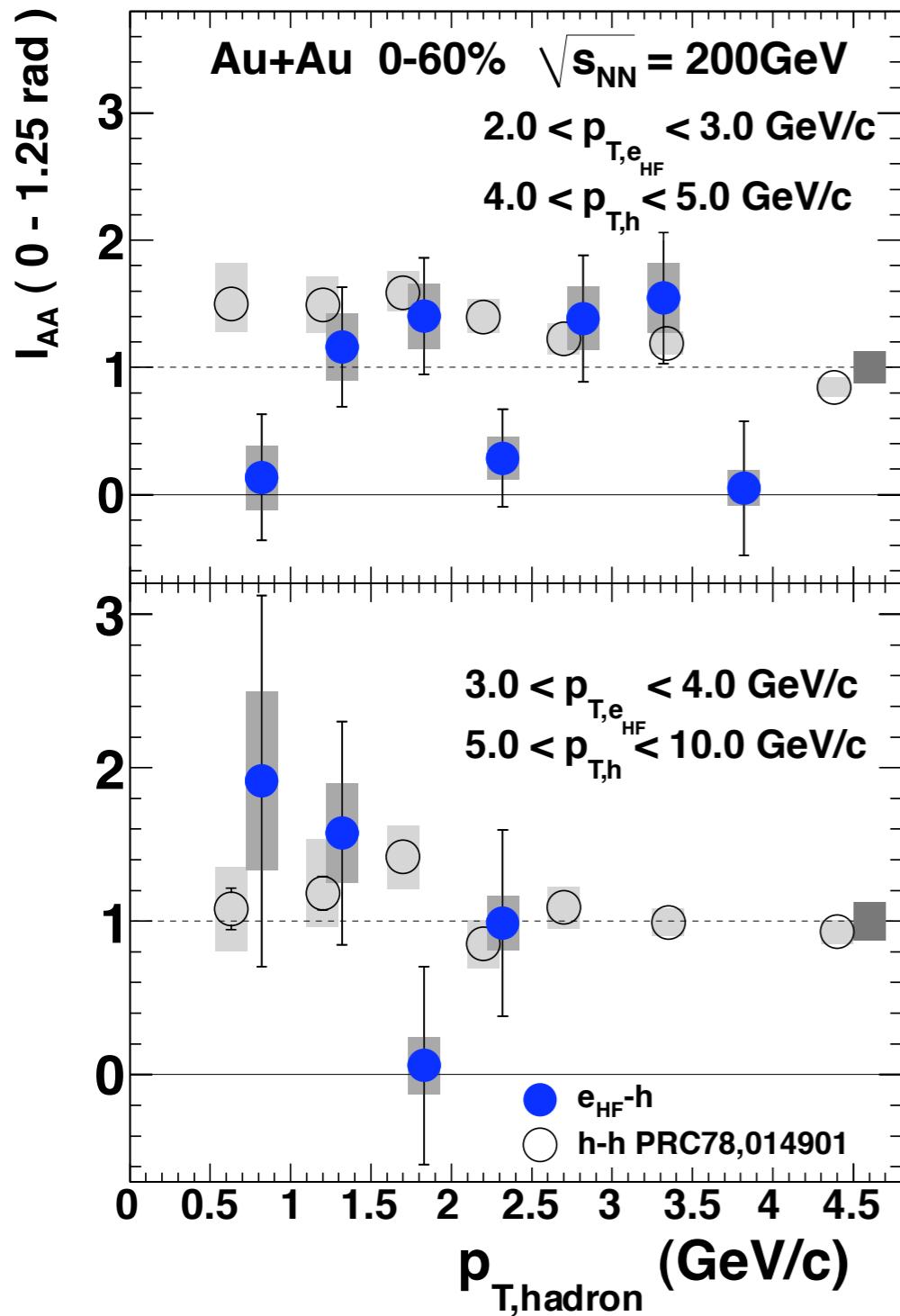


- no evidence for any modification
- consistent with hadron triggered

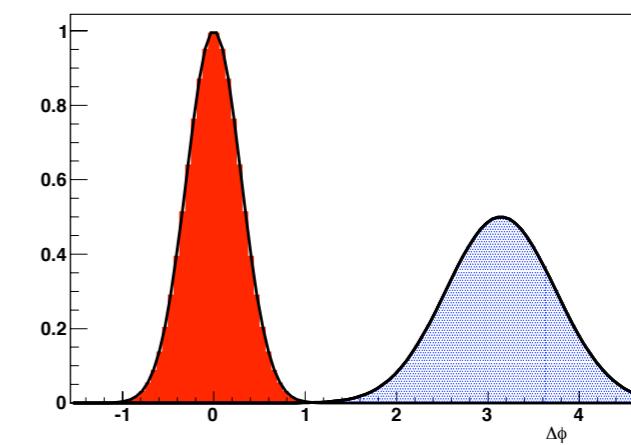


PHENIX: 1011.1477

e-h: same side correlations

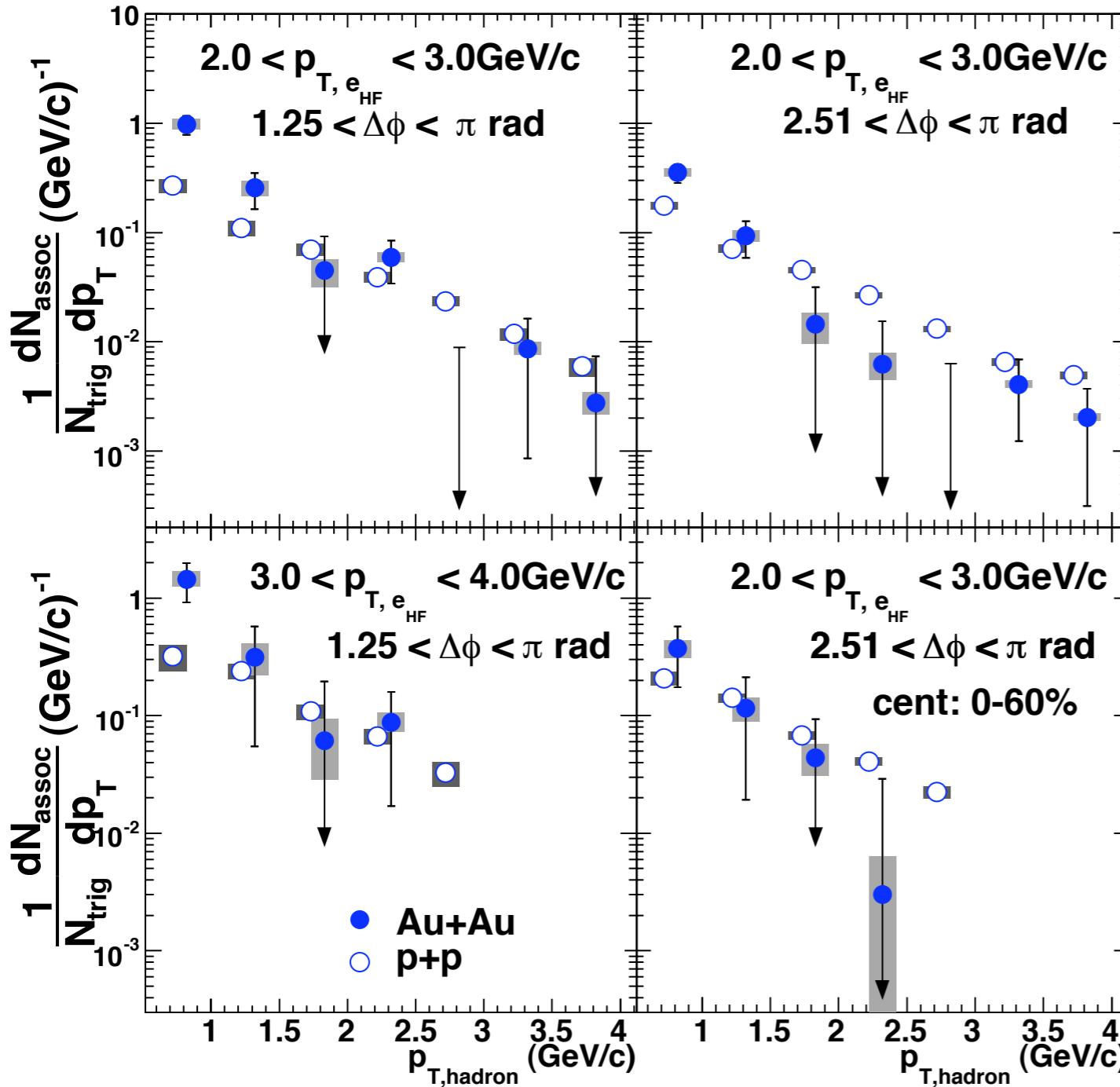


- no evidence for any modification
- consistent with hadron triggered



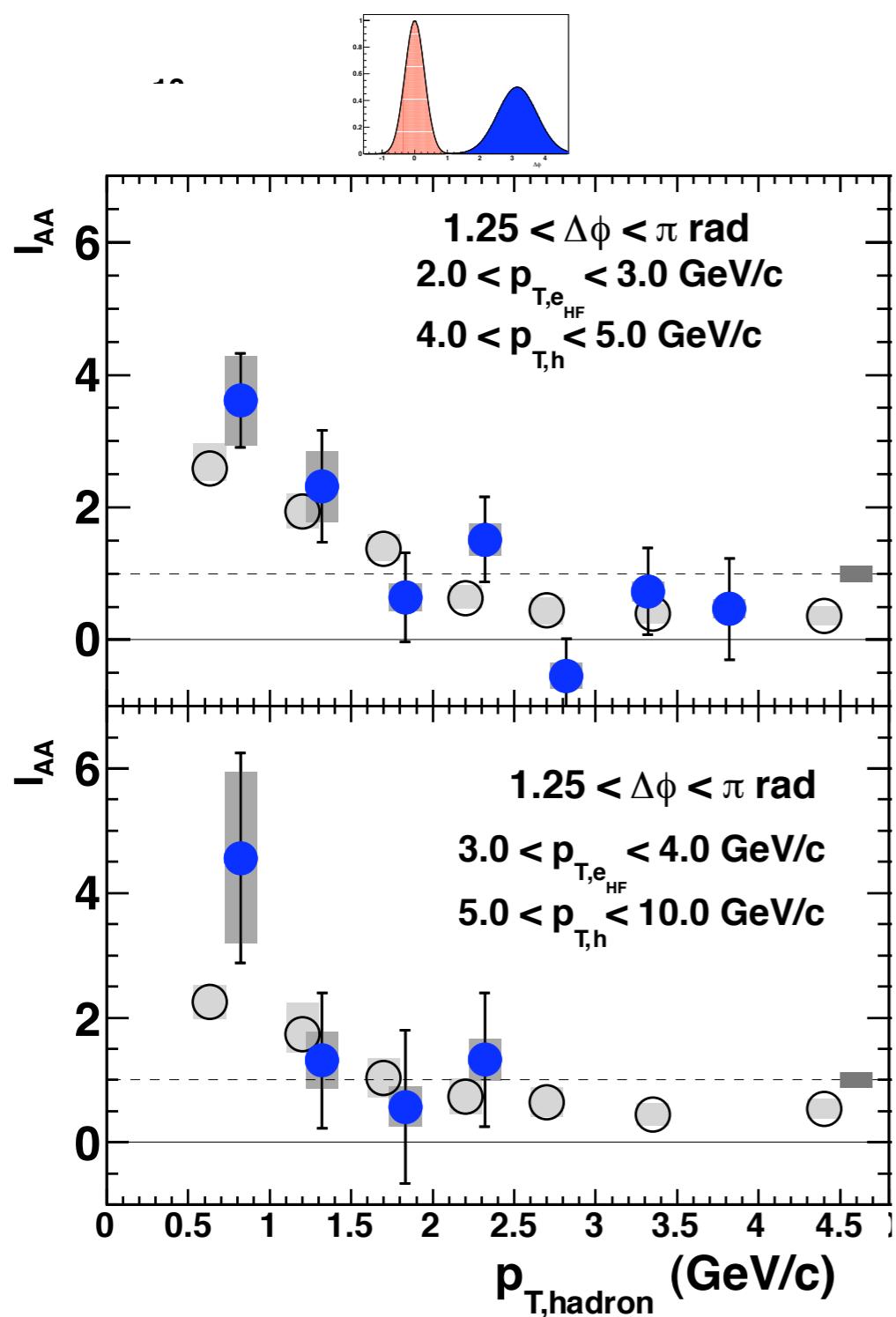
PHENIX: 1011.1477

e-h: opposite side correlations



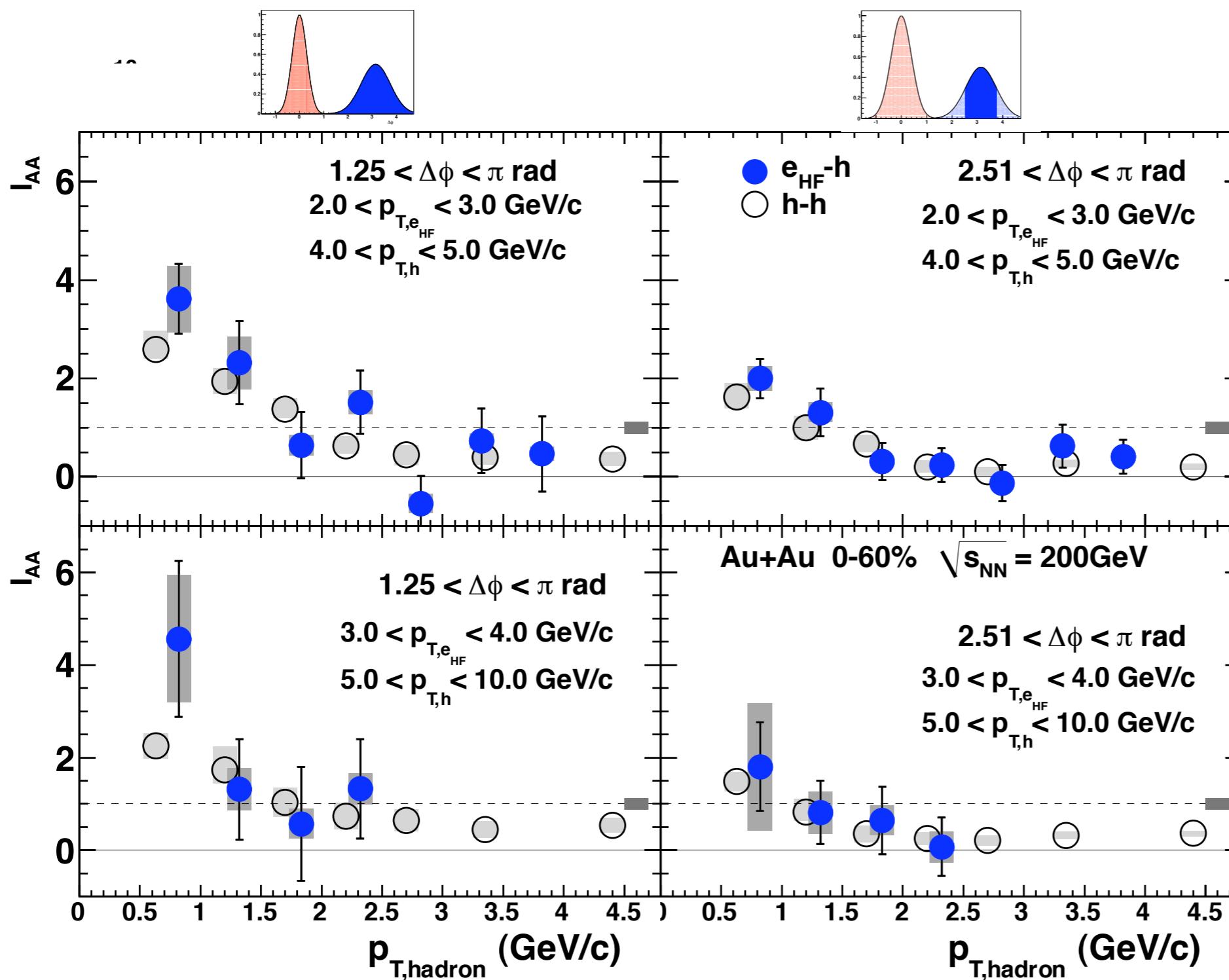
PHENIX: 1011.1477

e-h: opposite side correlations



PHENIX: 1011.1477

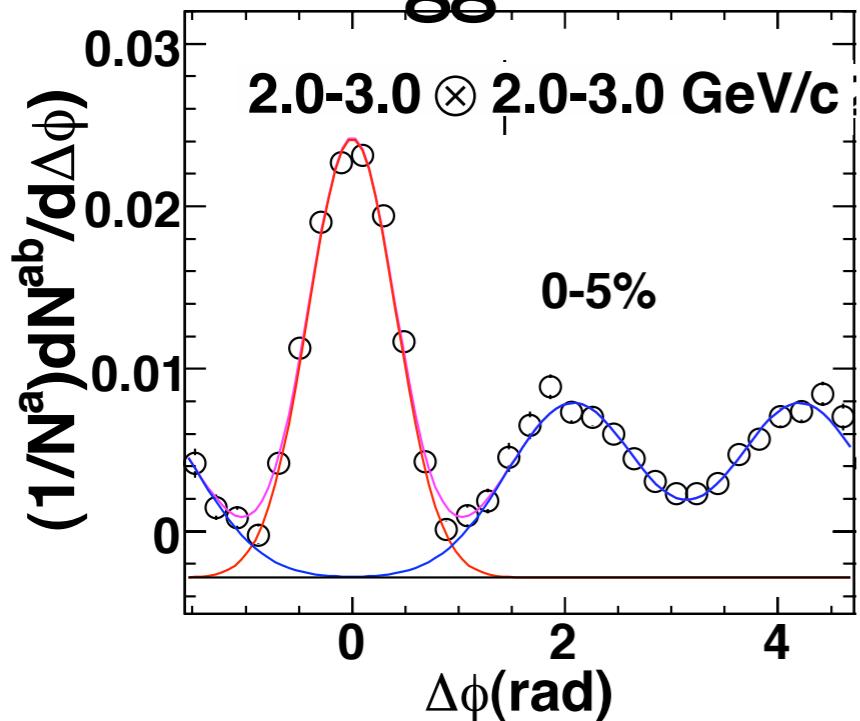
e-h: opposite side correlations



PHENIX: 1011.1477

shape modifications

hadron triggers

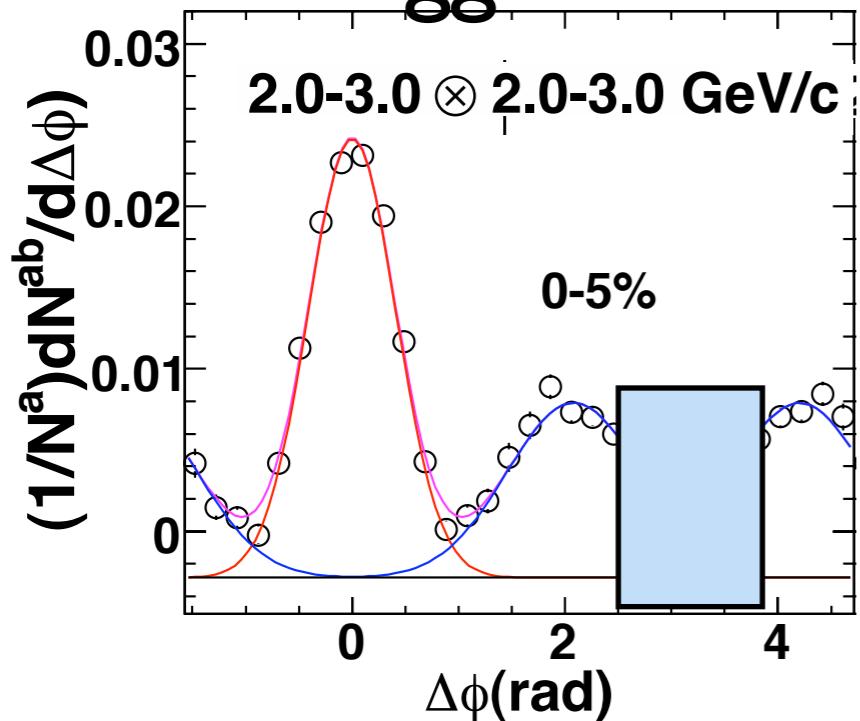


n.b. not exactly comparable
(head, shoulder definitions
slightly different)

PRC 78 014901
1011.1477[nucl-ex]

shape modifications

hadron triggers

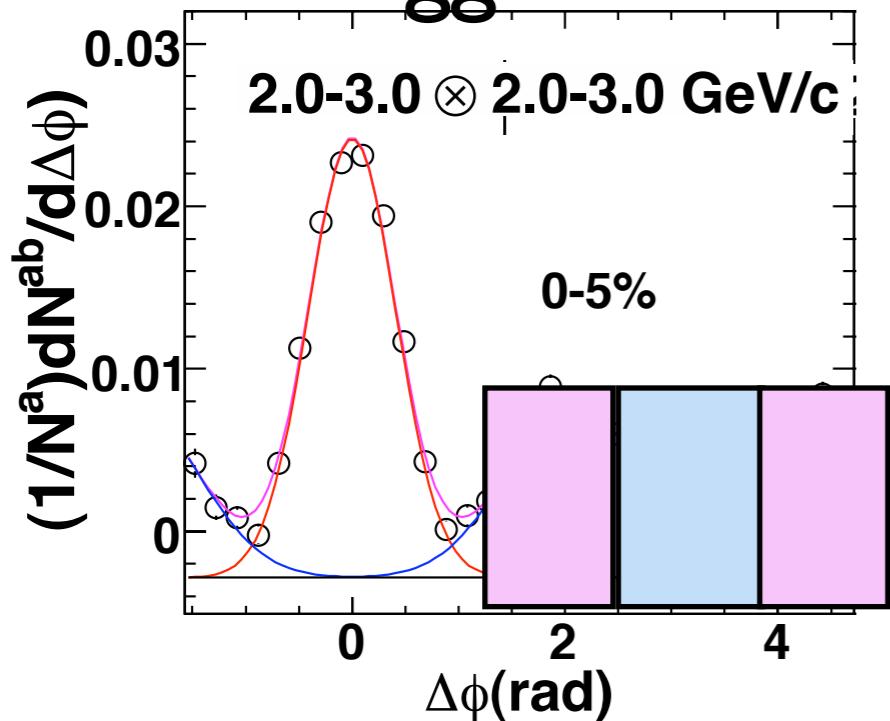


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PRC 78 014901
1011.1477[nucl-ex]

shape modifications

hadron triggers

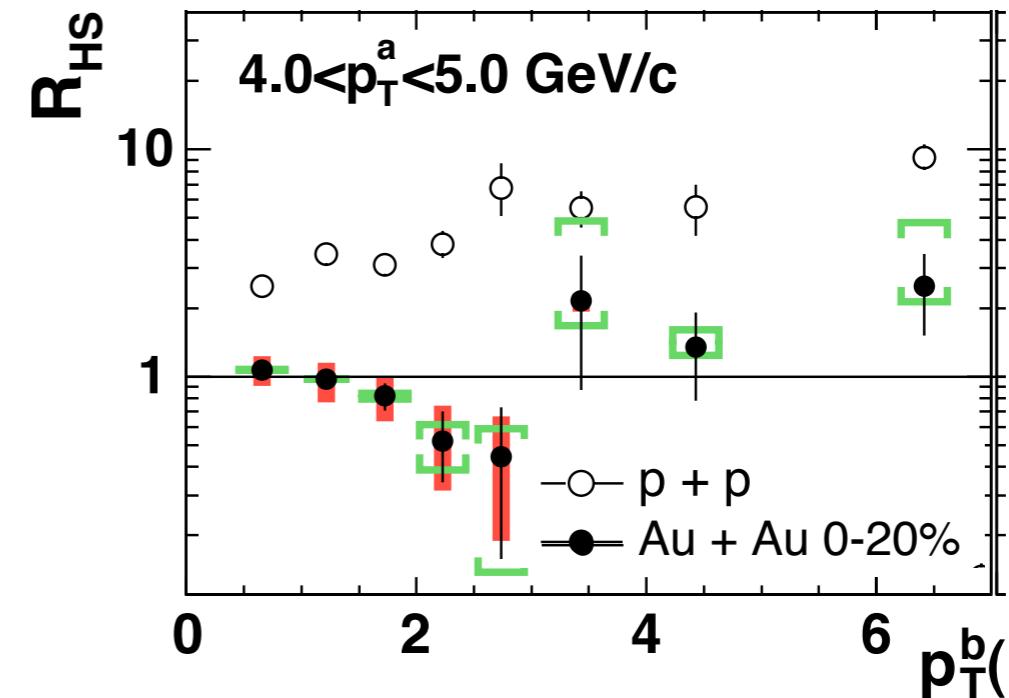
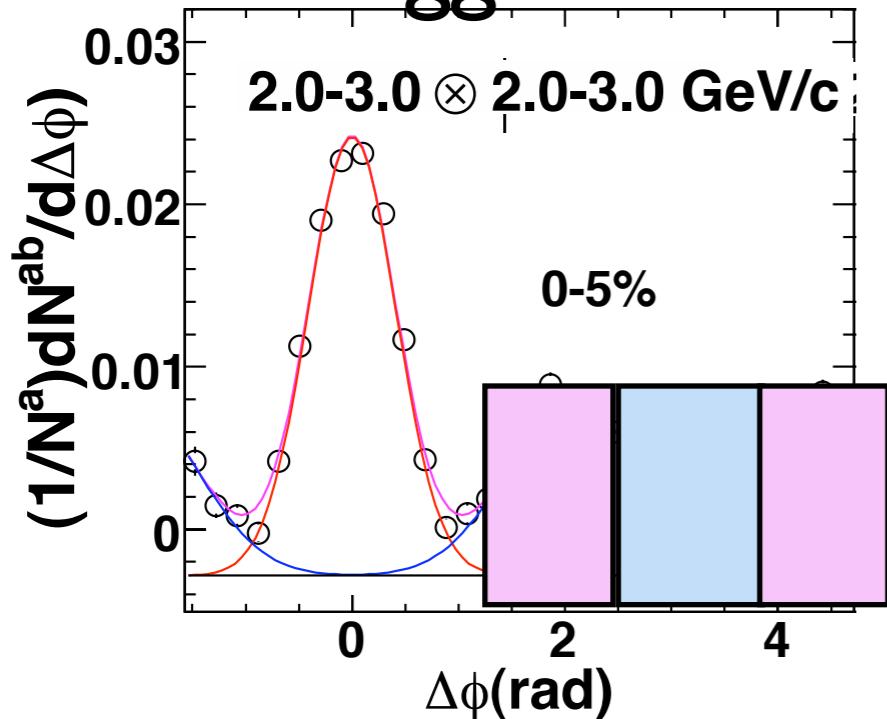


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PRC 78 014901
1011.1477[nucl-ex]

shape modifications

hadron triggers

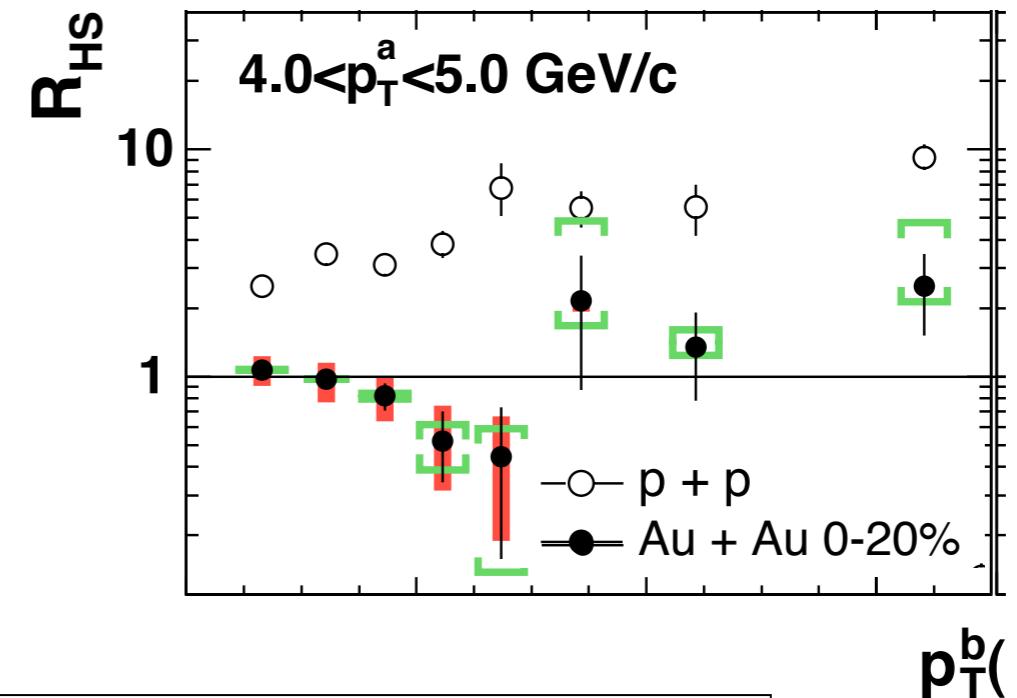
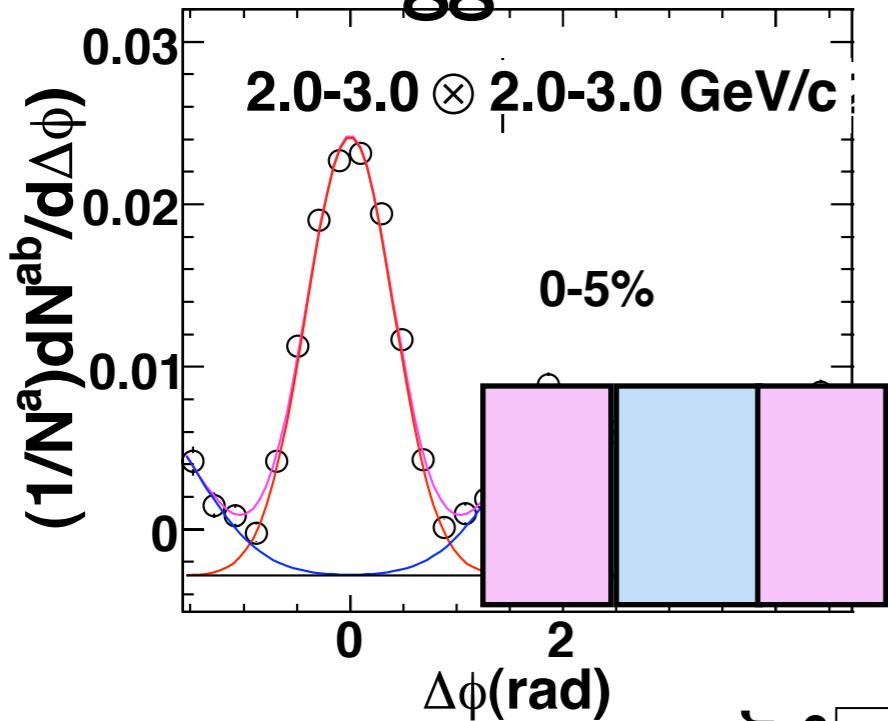


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PRC 78 014901
 1011.1477[nucl-ex]

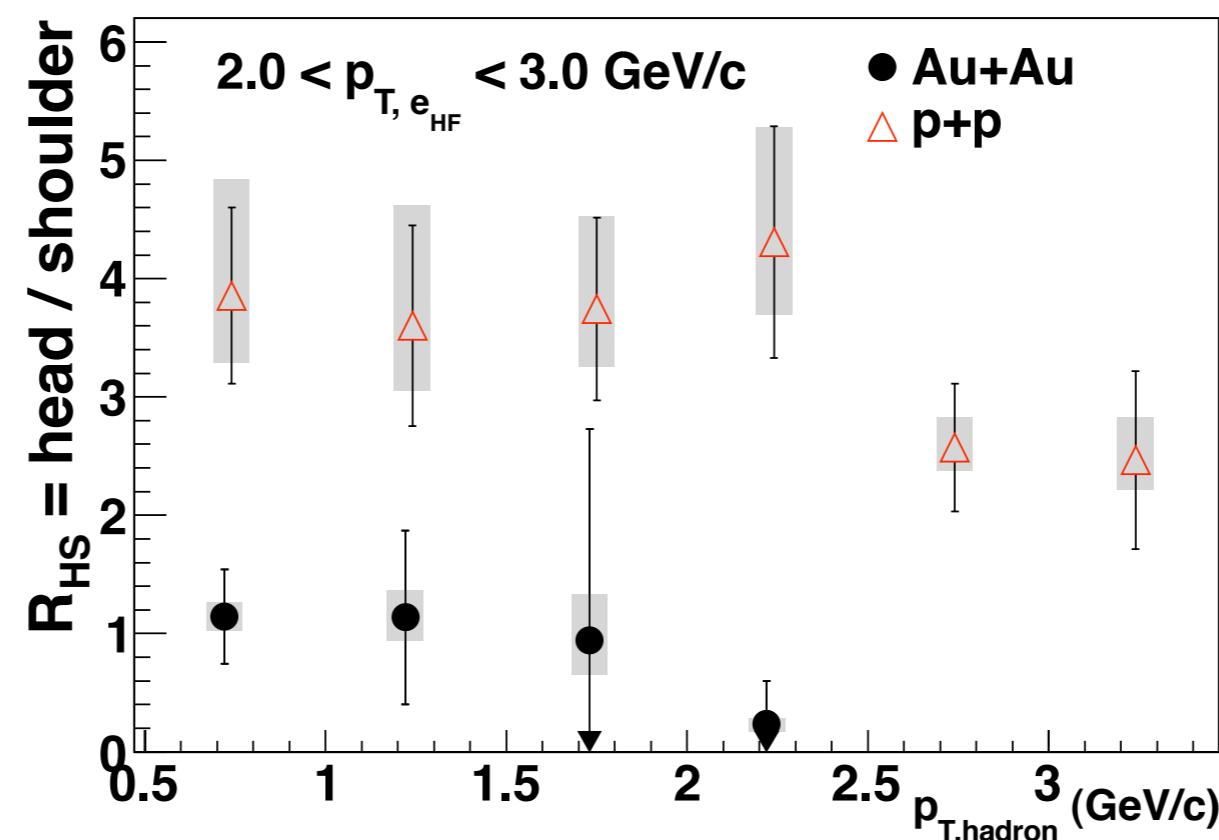
shape modifications

hadron triggers



electron triggers

n.b. not exactly comparable
(head, shoulder definitions
slightly different)



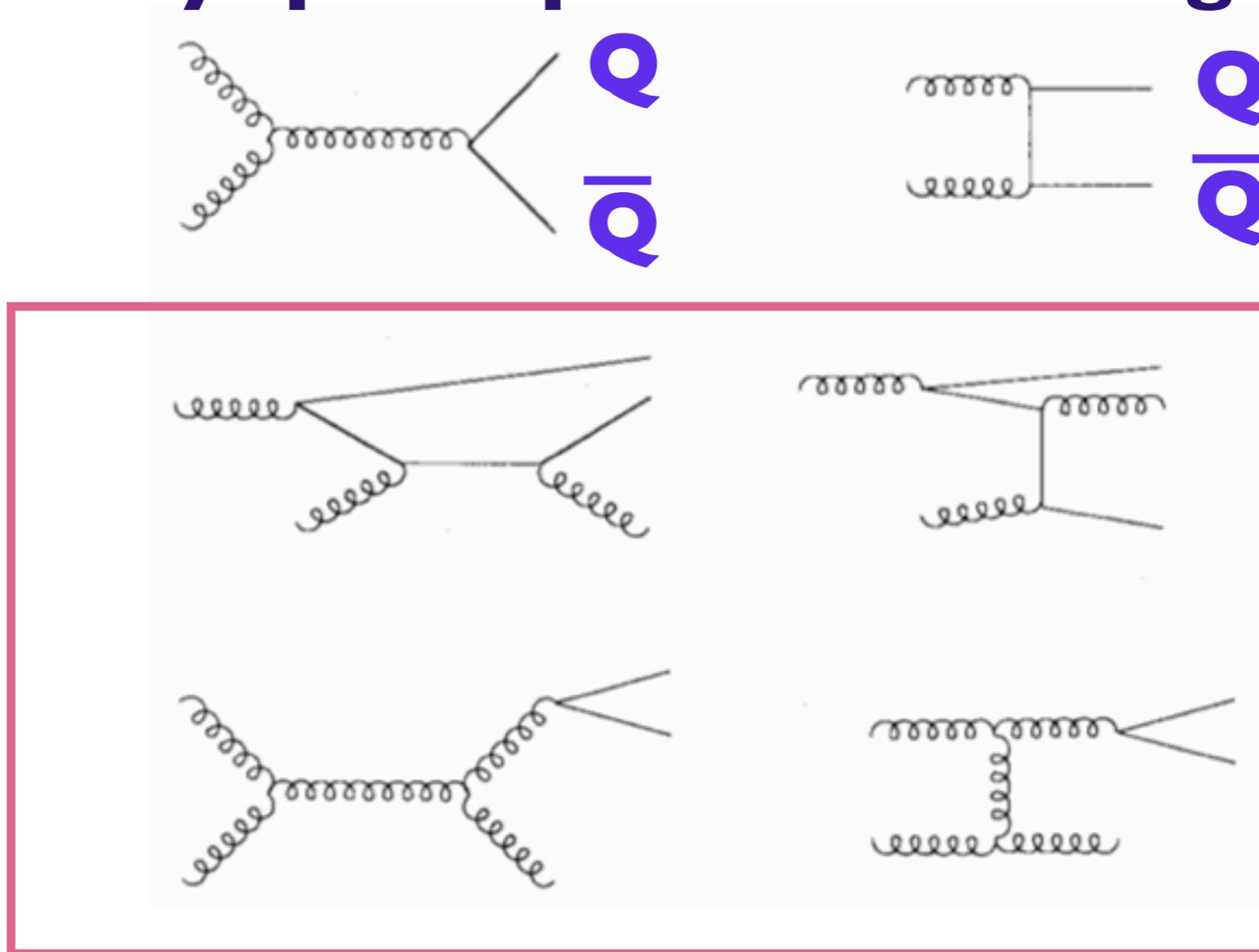
not unexpected

heavy quark production diagrams



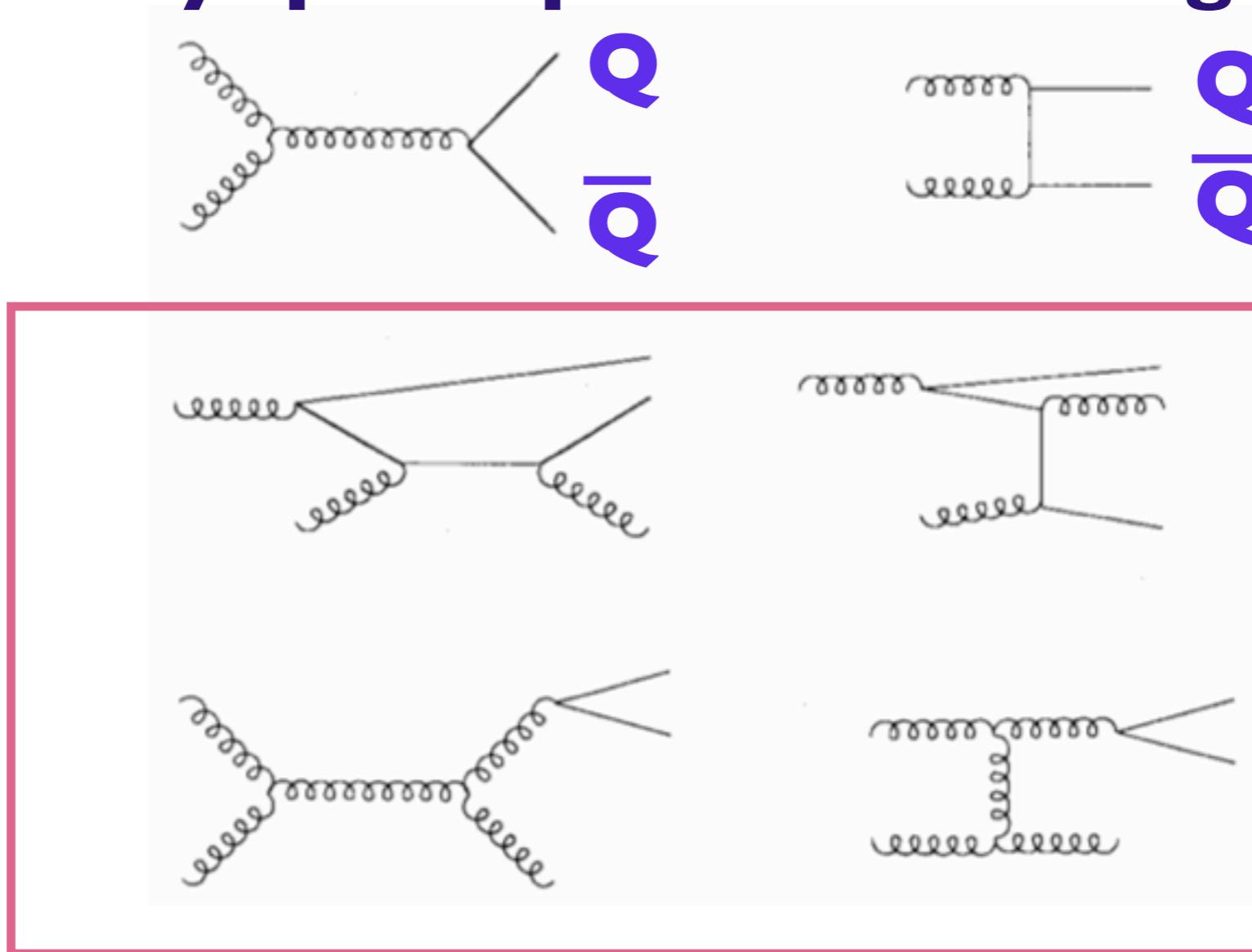
not unexpected

heavy quark production diagrams



not unexpected

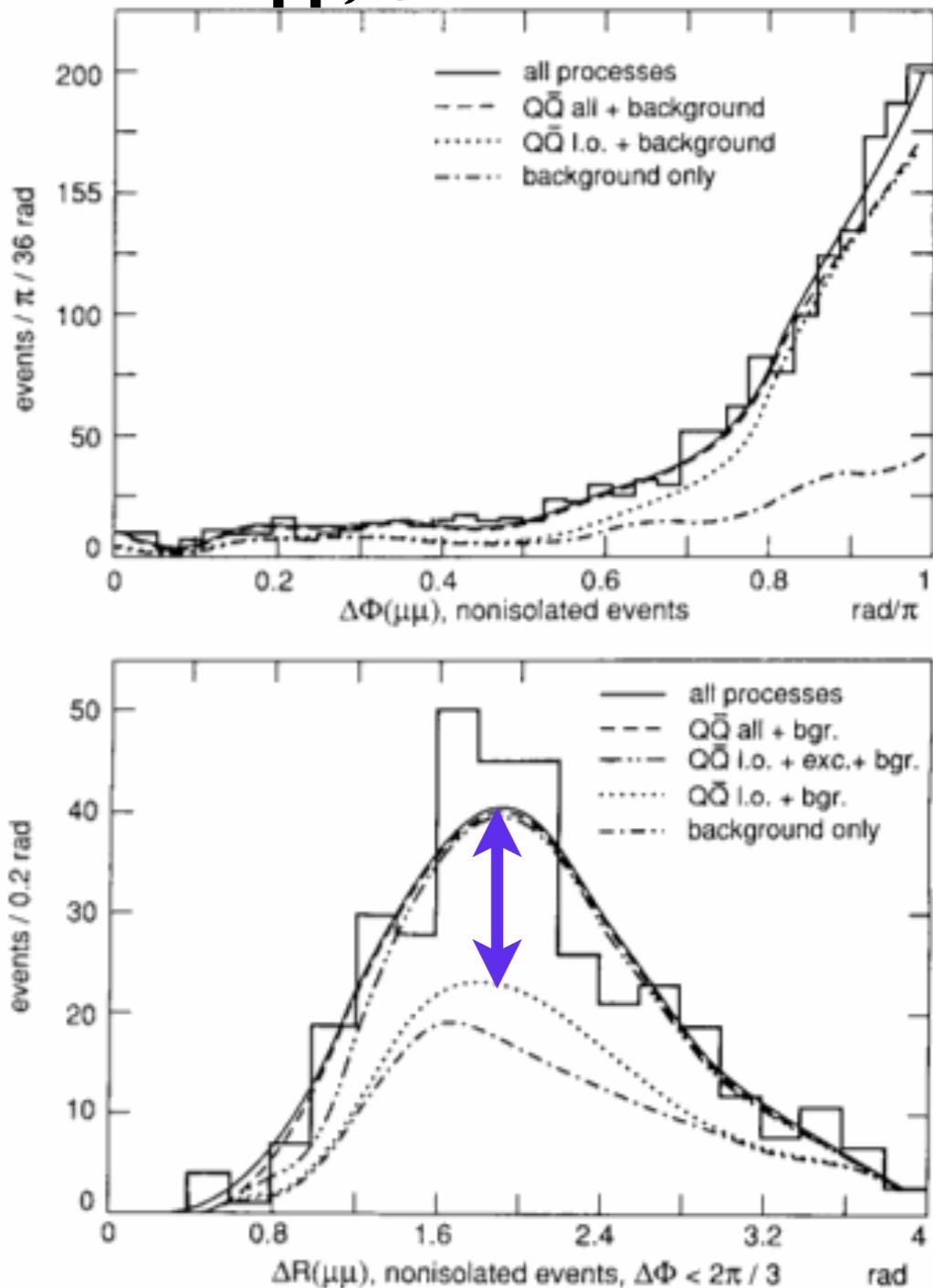
heavy quark production diagrams



sizable contributions from NLO effects

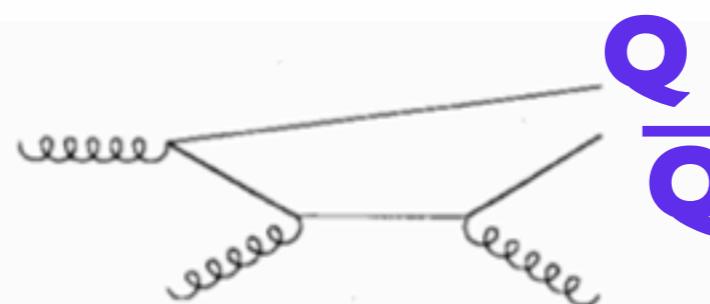
$\mu\mu$ Correlations @ ISR

pp, $\sqrt{s} = 630$ GeV



- fit with ISAJET
- 20-35% “higher order”
- similar sorts of measurements @ Tevatron

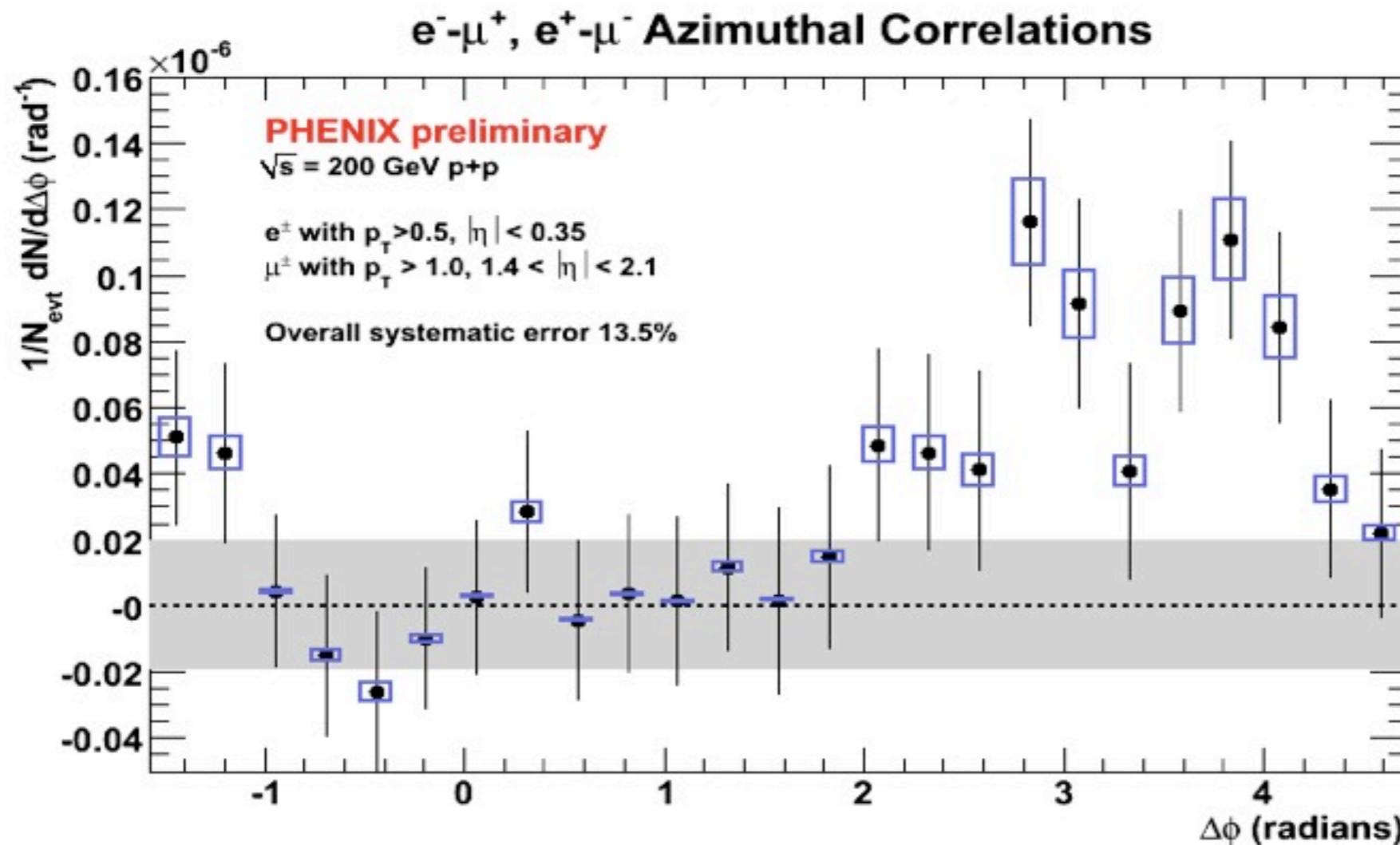
$p_{T\mu}^{\text{high}}$ range [GeV/c]	p_{Tb} range [GeV/c]	$b\bar{b}$ nonisol. $m_{\mu\mu} > 4$ GeV/c 2 [events]	‘high.ord.’ fraction [%]
All	$\gtrsim 6$	829 ± 58	26.2 ± 4.0
3-5	$\gtrsim 6$	402 ± 37	24.6 ± 8.5
5-7	$\gtrsim 8$	286 ± 23	31.2 ± 5.4
7-10	$\gtrsim 11$	103 ± 12	35.2 ± 5.1
10-20	$\gtrsim 15$	32 ± 6	21.3 ± 12.4



UA1, Z Phys C 61 41 1994

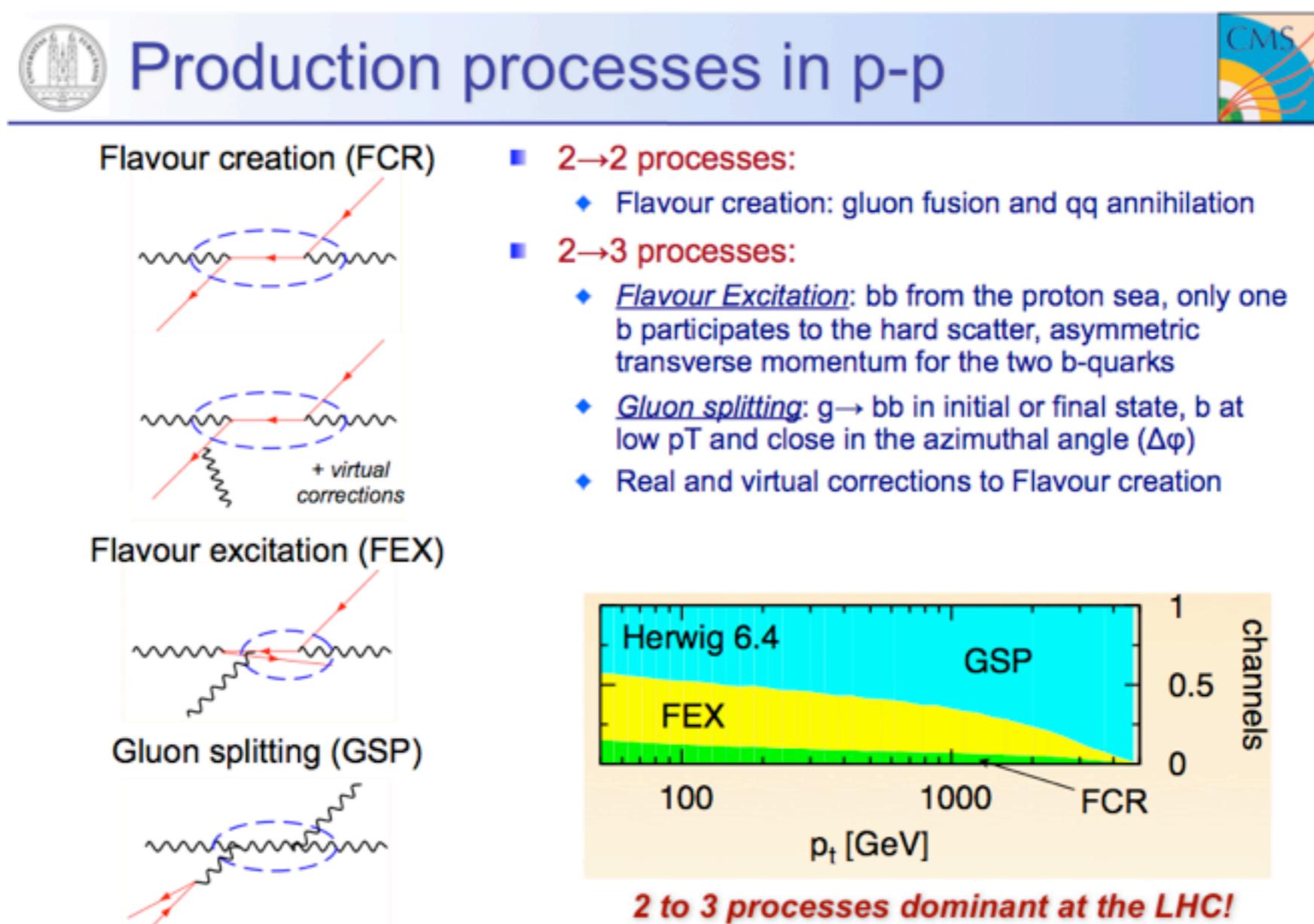
e- μ correlations

- sensitive to correlated charm, but at forward/mid-rapidity



RHIC vs. LHC

- also different production mix



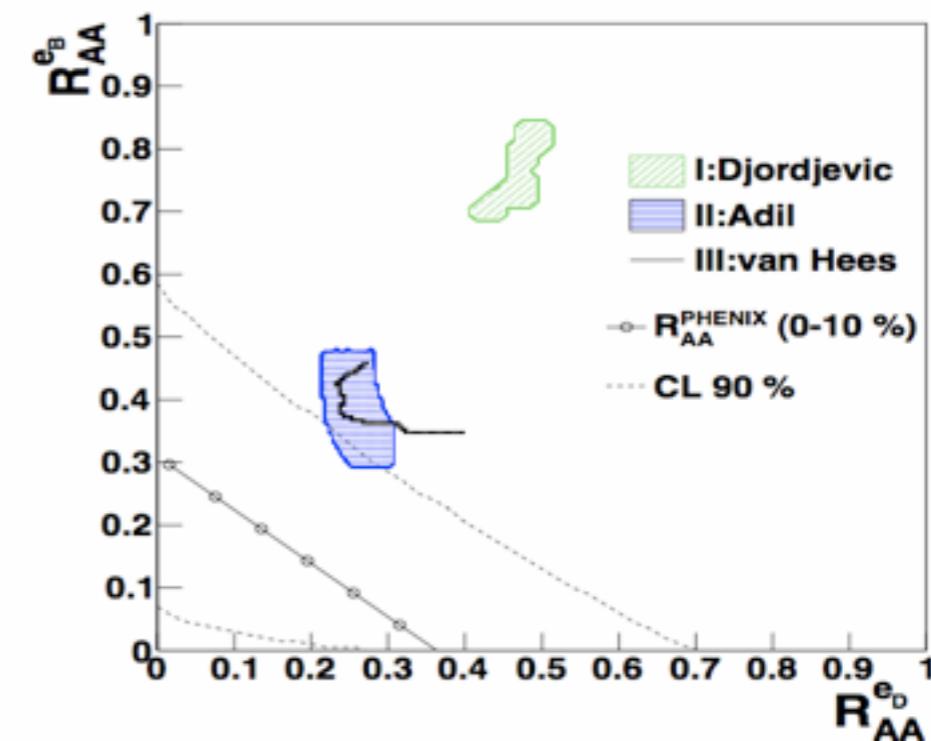
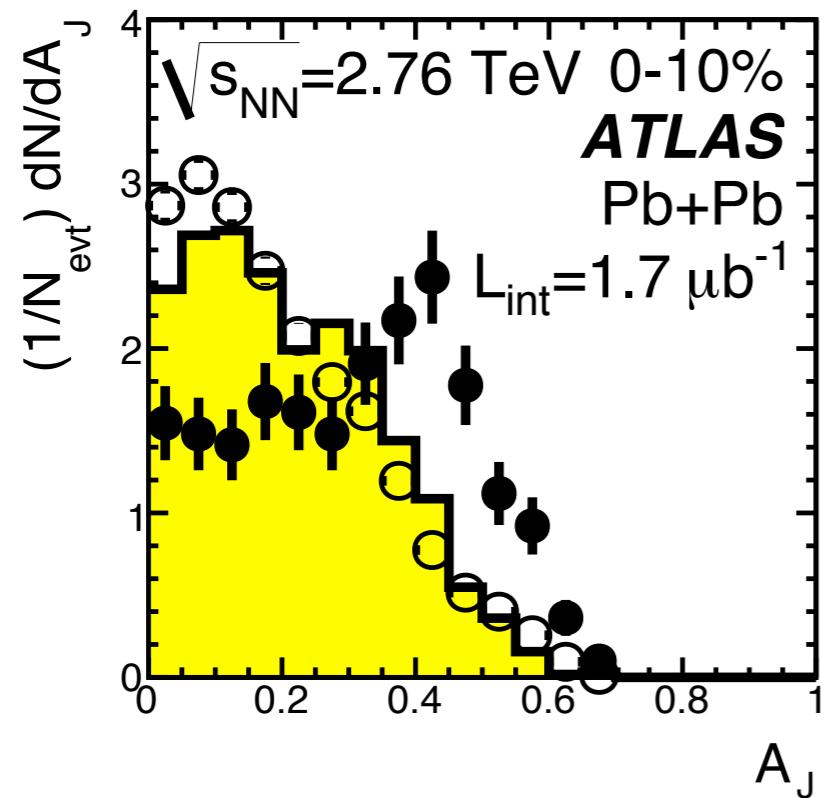
Near Term Future



- Silicon Vertex Detector
 - e-h and e-e correlations to understand HF production
 - here 500 GeV p+p data provides a good opportunity
 - increased HF cross sections and different collision energy
→ useful input for understanding HI data at 200 GeV

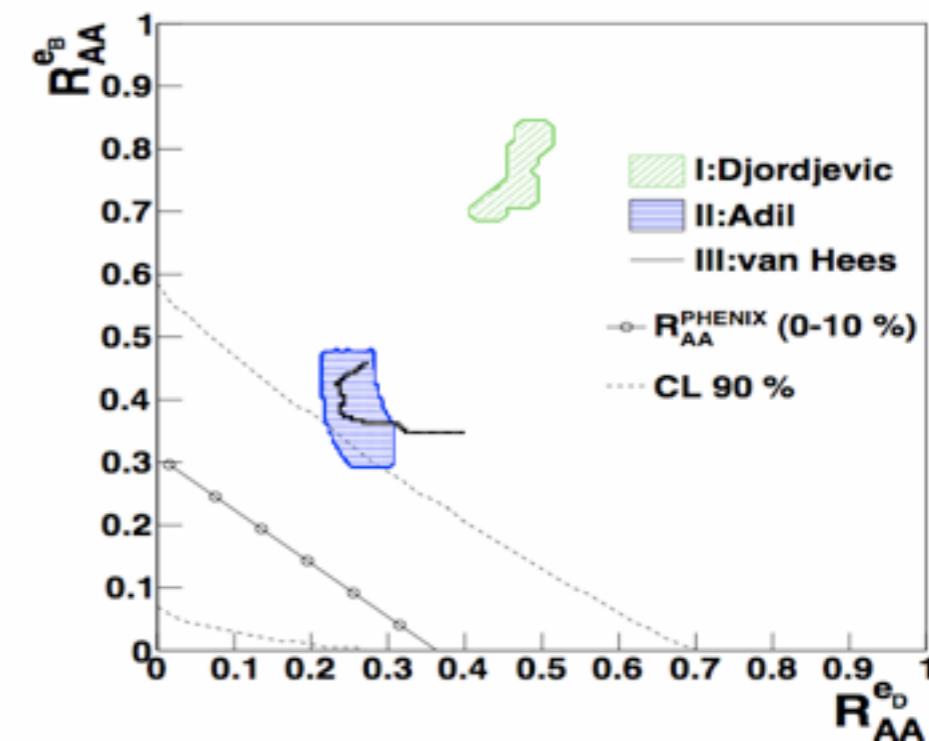
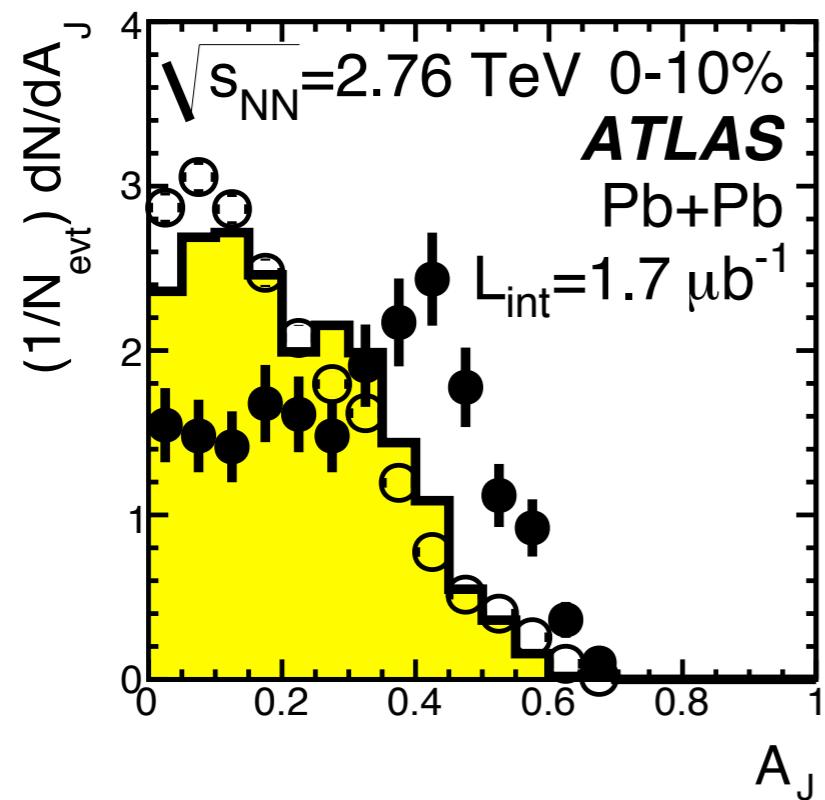
heavy flavor and the LHC

- ATLAS di-jet results and bottom suppression at RHIC both point to the strong quenching ability of the matter



heavy flavor and the LHC

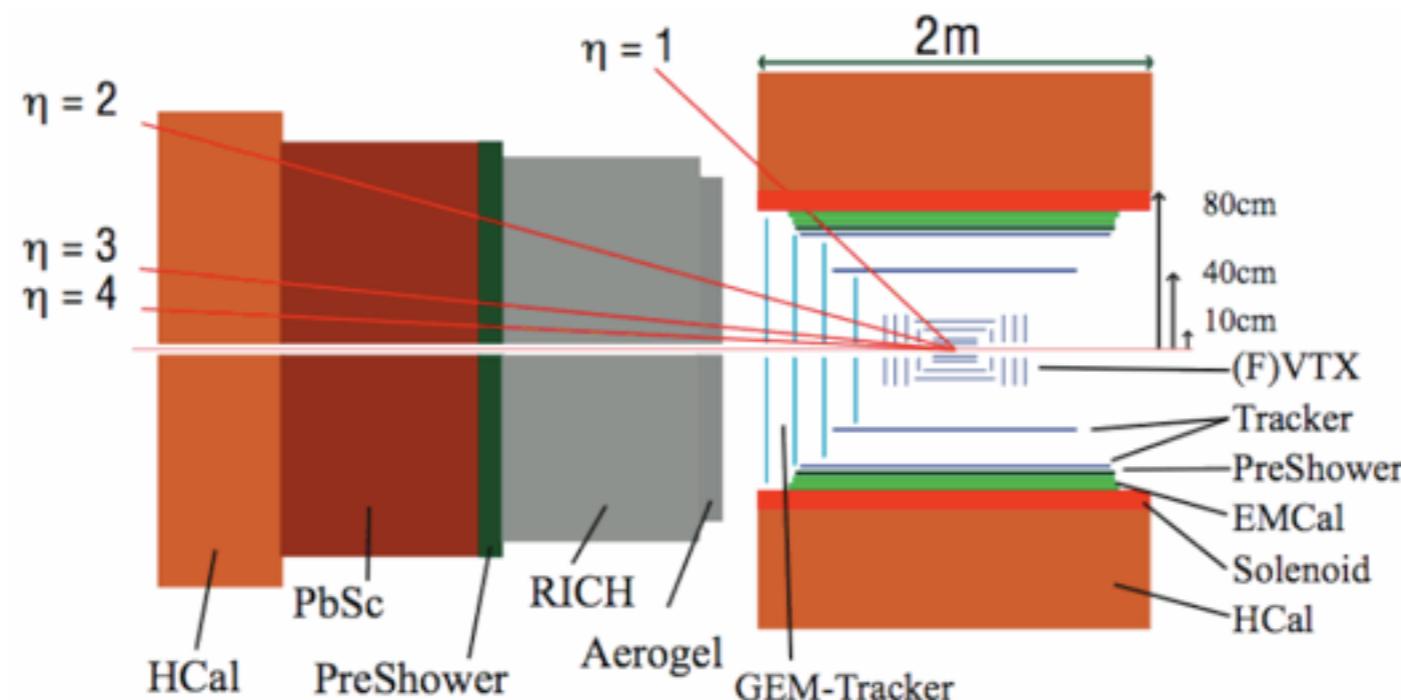
- ATLAS di-jet results and bottom suppression at RHIC both point to the strong quenching ability of the matter



what will b -jets look like at the LHC?

sPHENIX

- jets offer huge rate advantages and a reduction of biases from spectra & correlations
- however need a real jet detector for RHIC
 - high rate, hadronic calorimetry, heavy flavor tagging, large acceptance
 - suited to systematic studies (system size, energy, etc)



PHENIX Decadal Plan, Jacak HP10

outlook

outlook

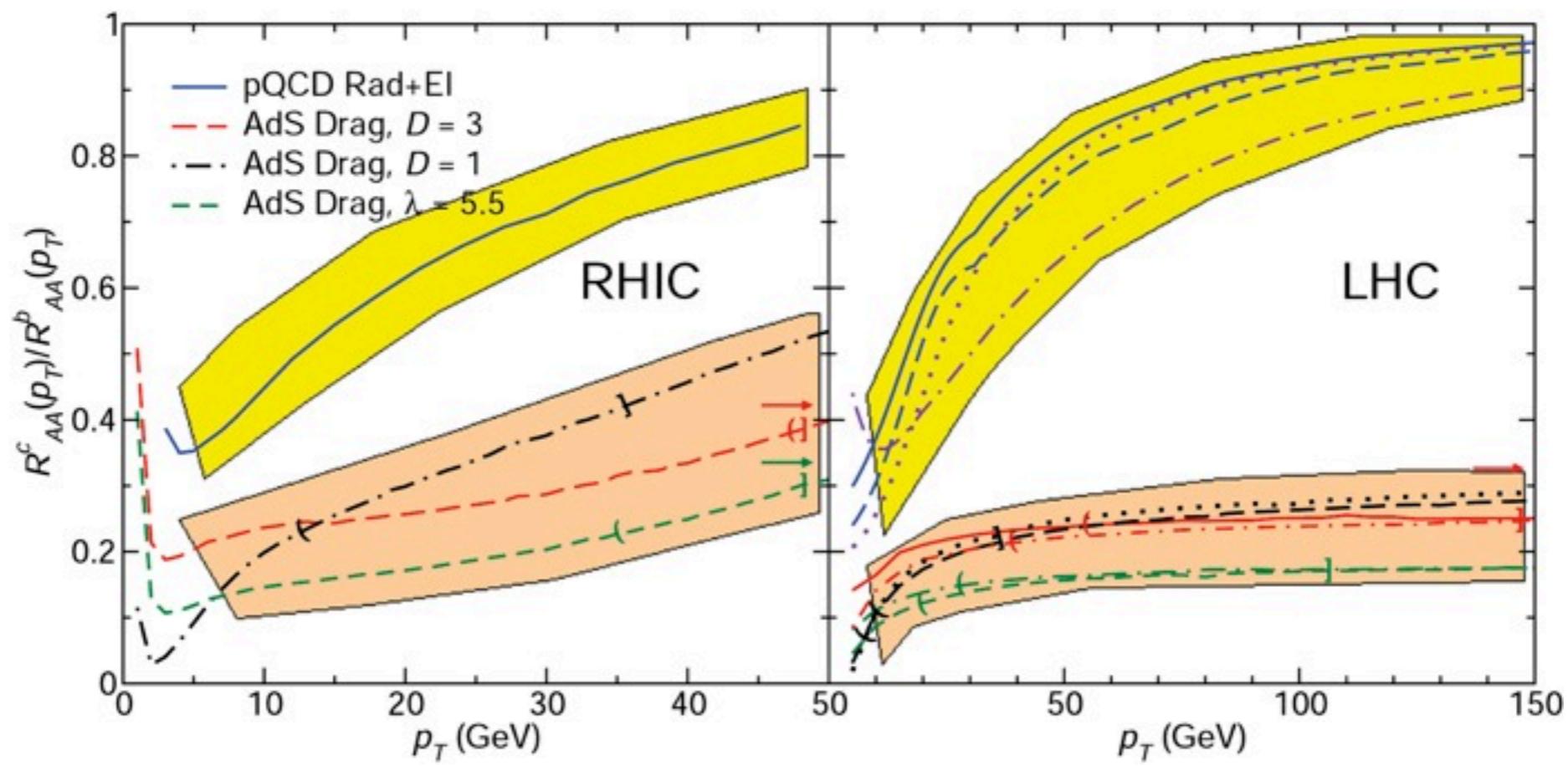
- heavy flavor is one of the best tools to understand how partons interact with the QGP

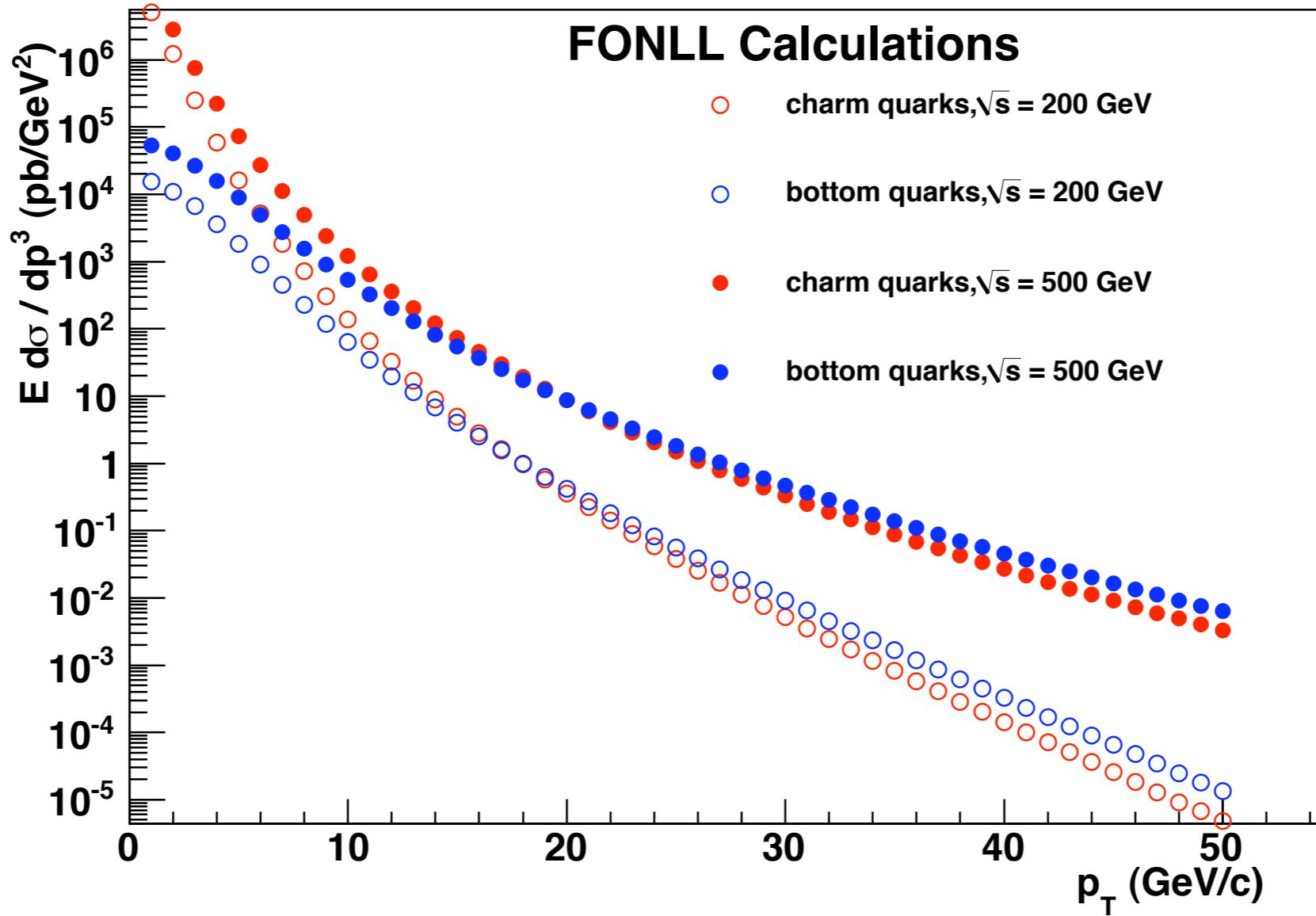
outlook

- heavy flavor is one of the best tools to understand how partons interact with the QGP
- experimentally very challenging
 - rate
 - charm & bottom mixture
 - different production configurations
 - measurement via single electrons

outlook

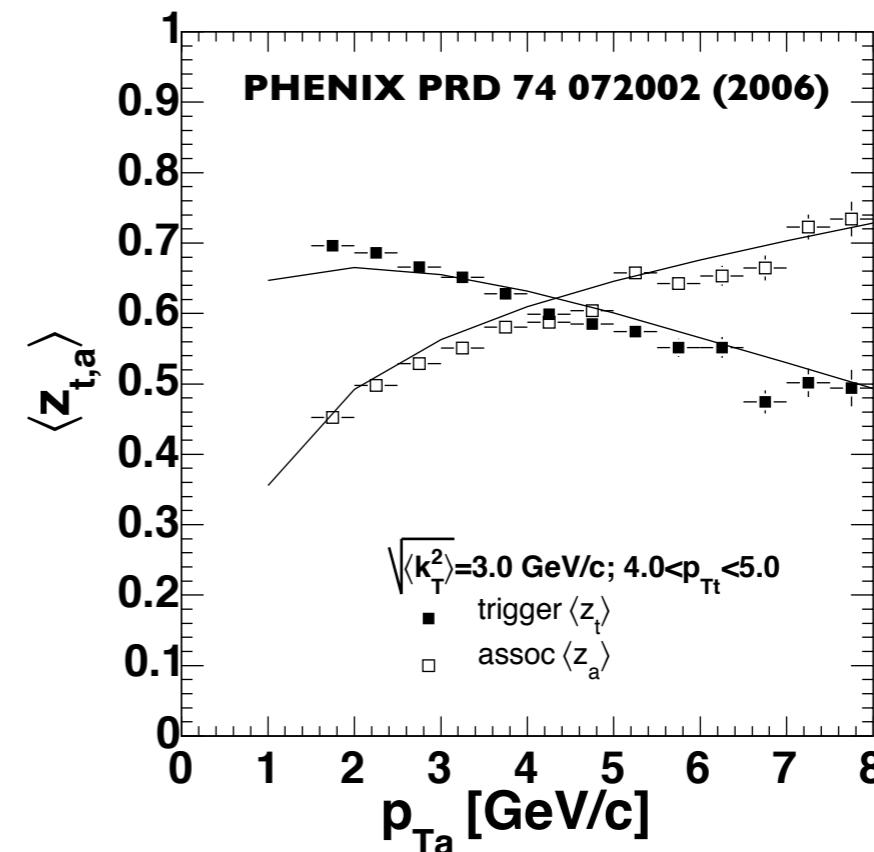
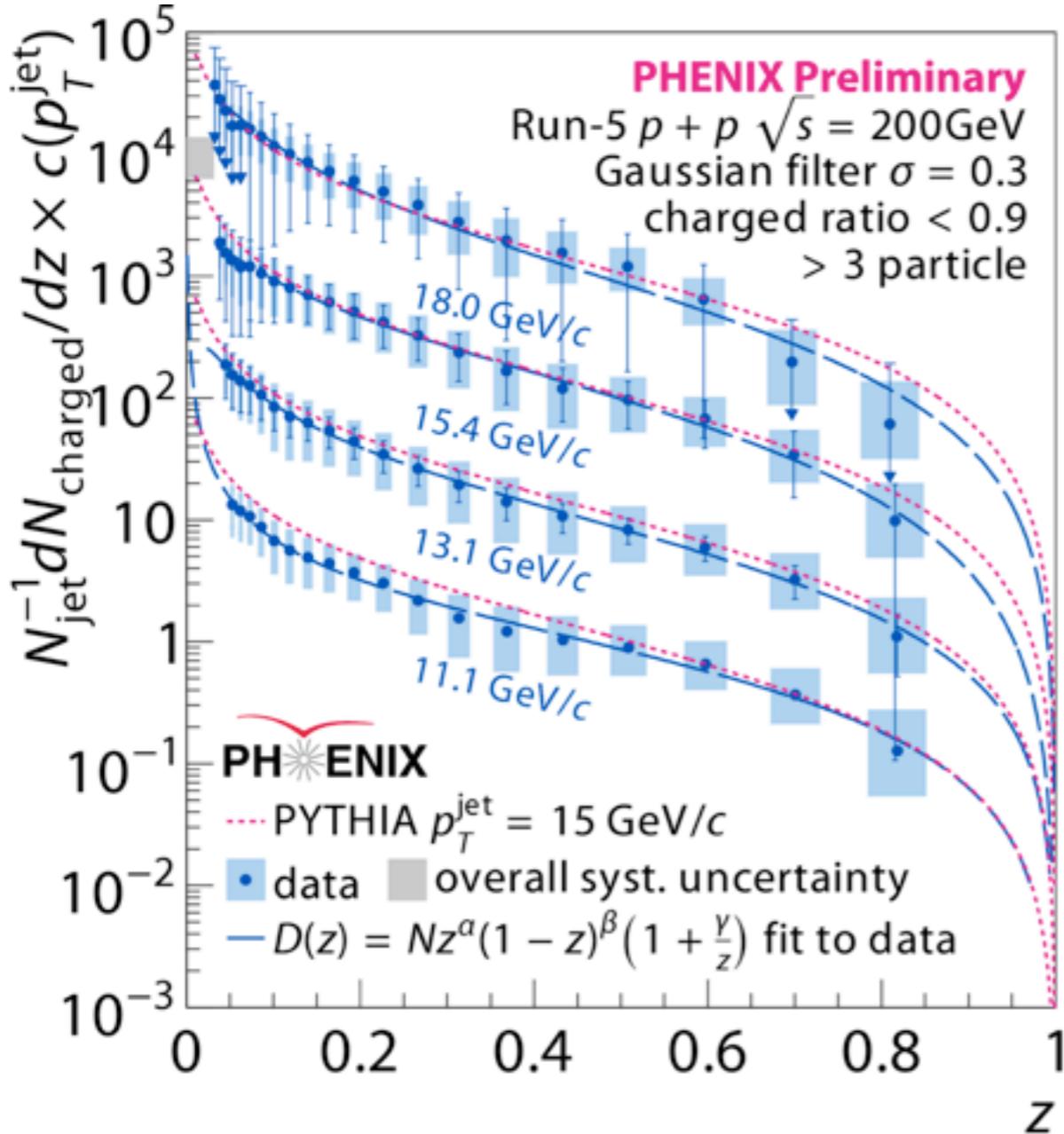
- heavy flavor is one of the best tools to understand how partons interact with the QGP
- experimentally very challenging
 - rate
 - charm & bottom mixture
 - different production configurations
 - measurement via single electrons
- investigations are still in their early stages
 - vertex upgrades at RHIC & LHC provide big improvements!
 - correlations will be key





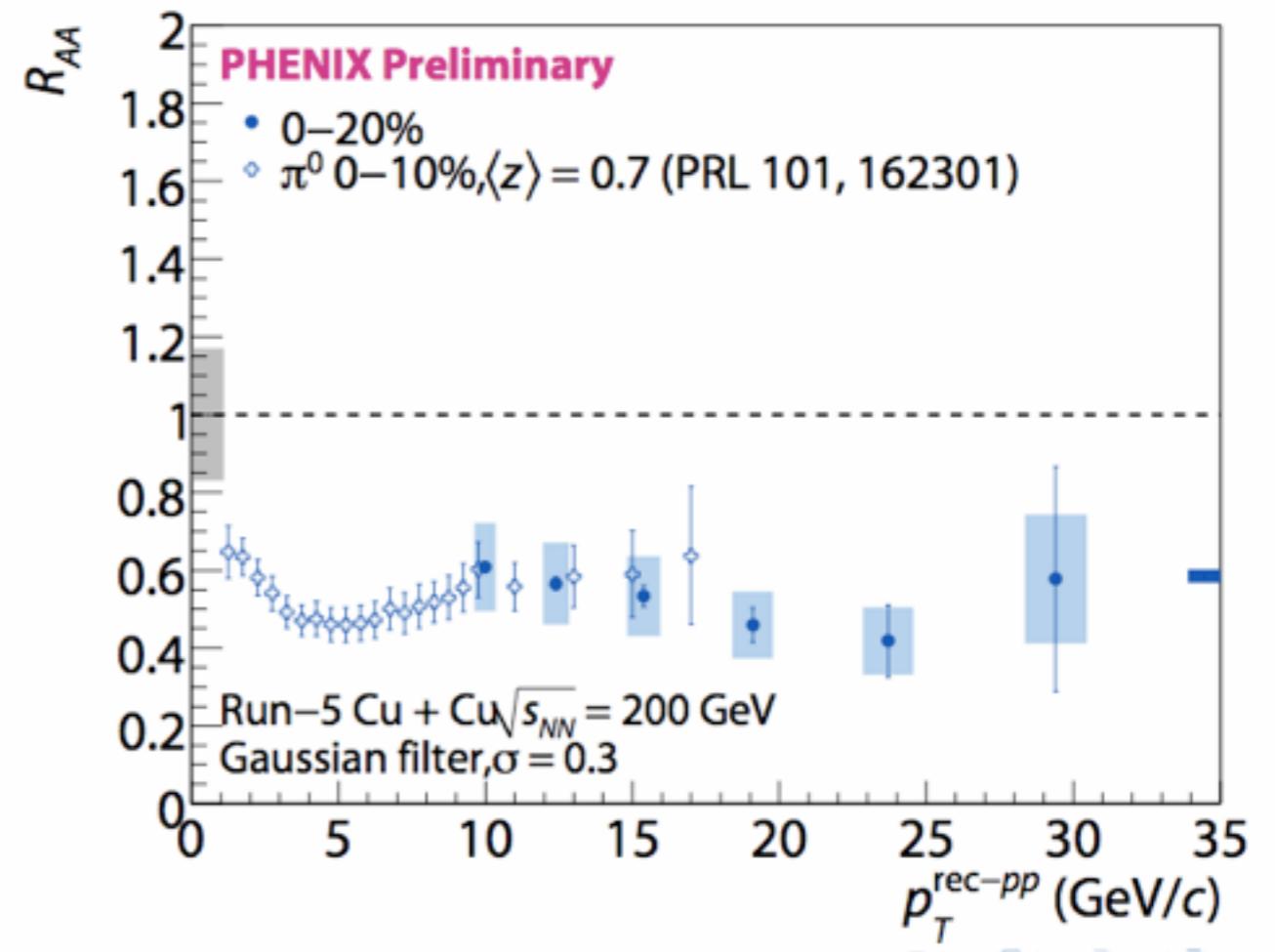
private communication, M Cacciari

tool for the future: jets



- leading particles sample high z part of the fragmentation function
- little sensitivity to modification patterns...that's where the energy loss physics is \rightarrow radiated gluons, broadened jet profile...

jets: algorithm matters!

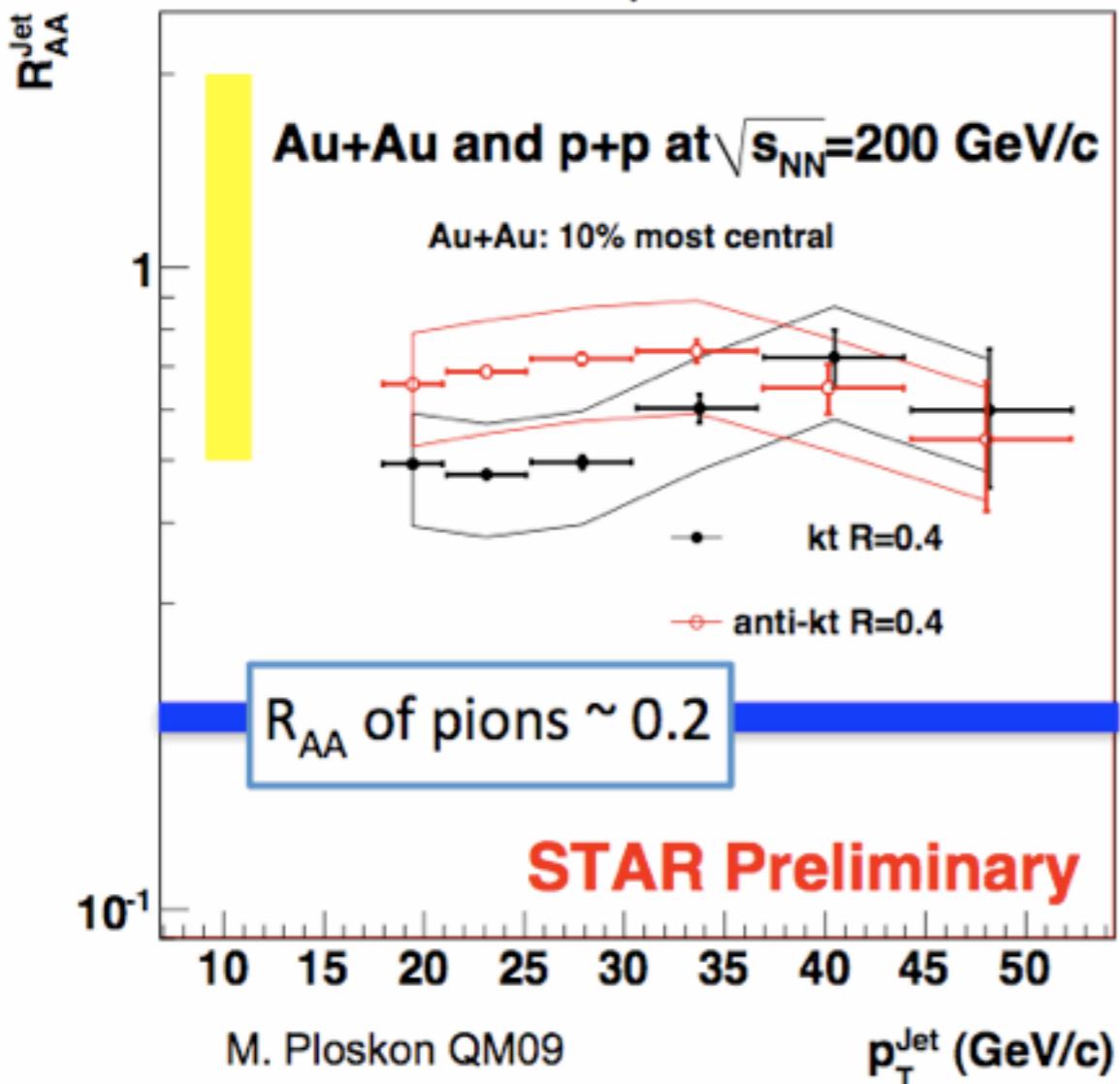


STAR: $R_{AA}(\text{jet}) \neq R_{AA}(\pi^0)$
large uncertainties

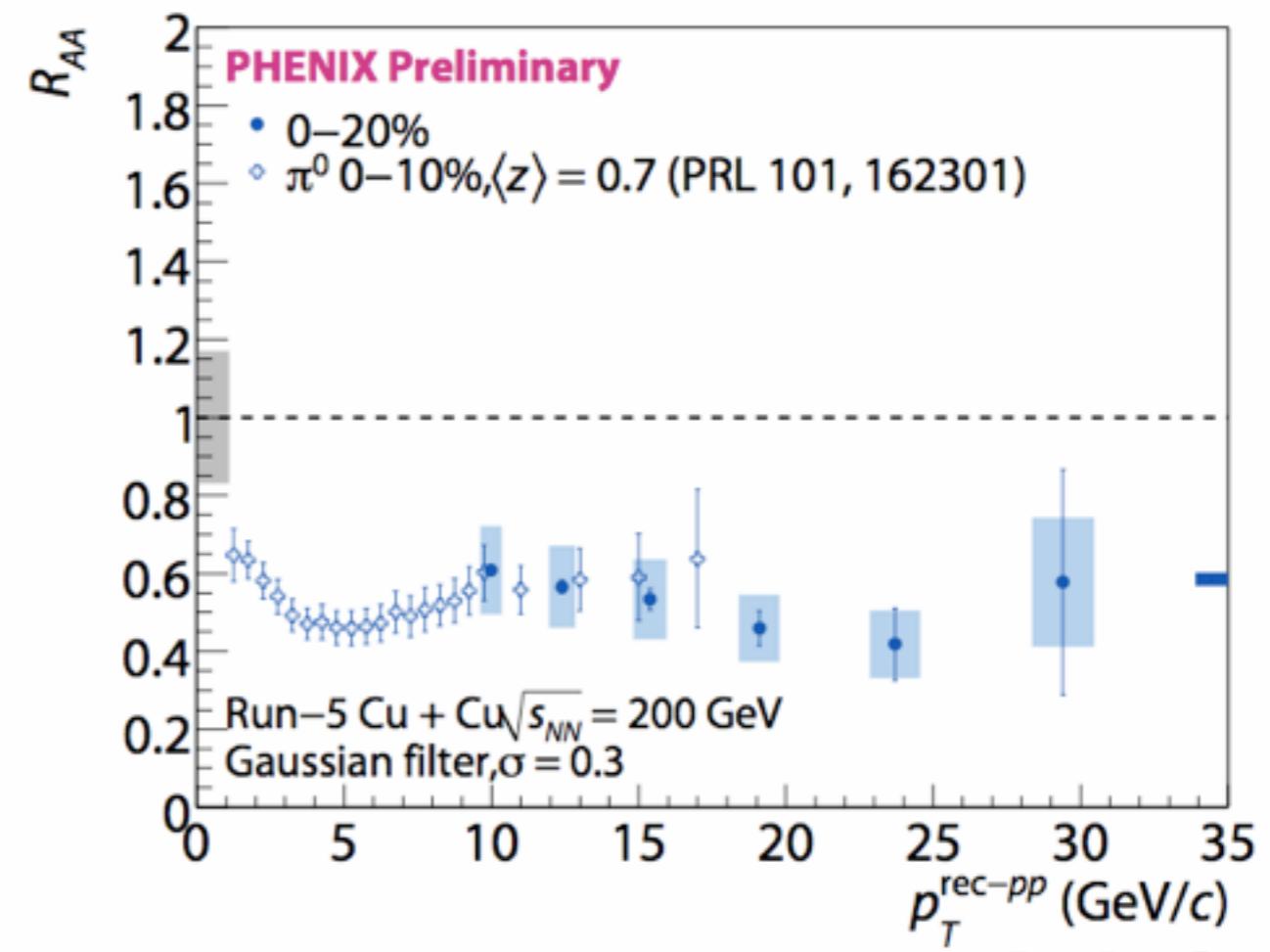
PHENIX: $R_{AA}(\text{jet}) = R_{AA}(\pi^0)$
small uncertainties

jets: algorithm matters!

Au-Au, R=0.4

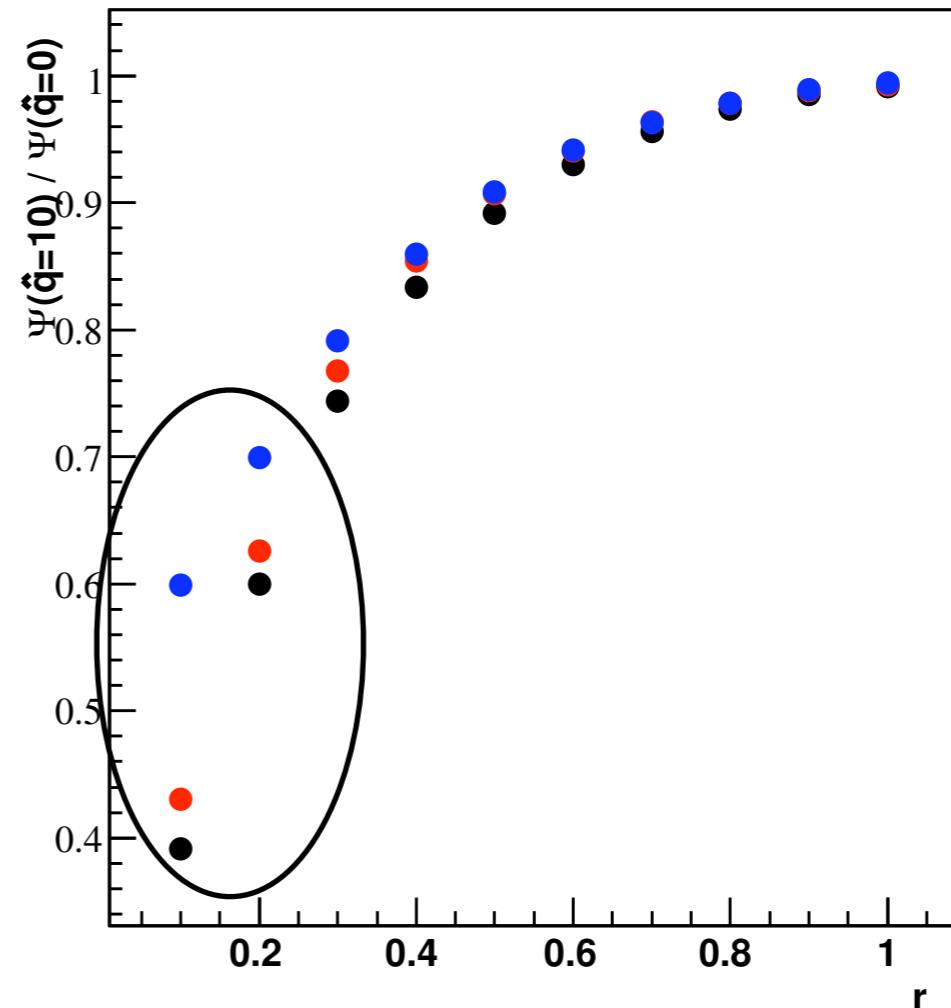
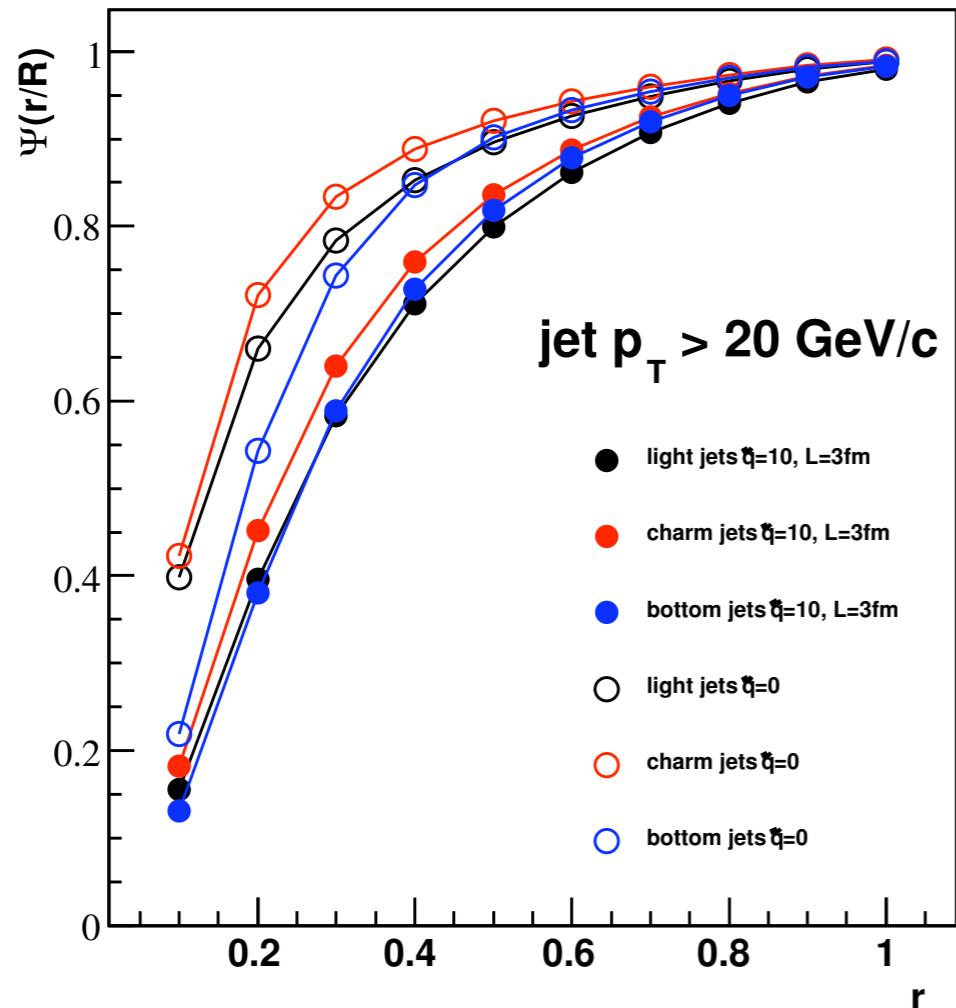


STAR: $R_{AA}(\text{jet}) \neq R_{AA}(\pi^0)$
large uncertainties

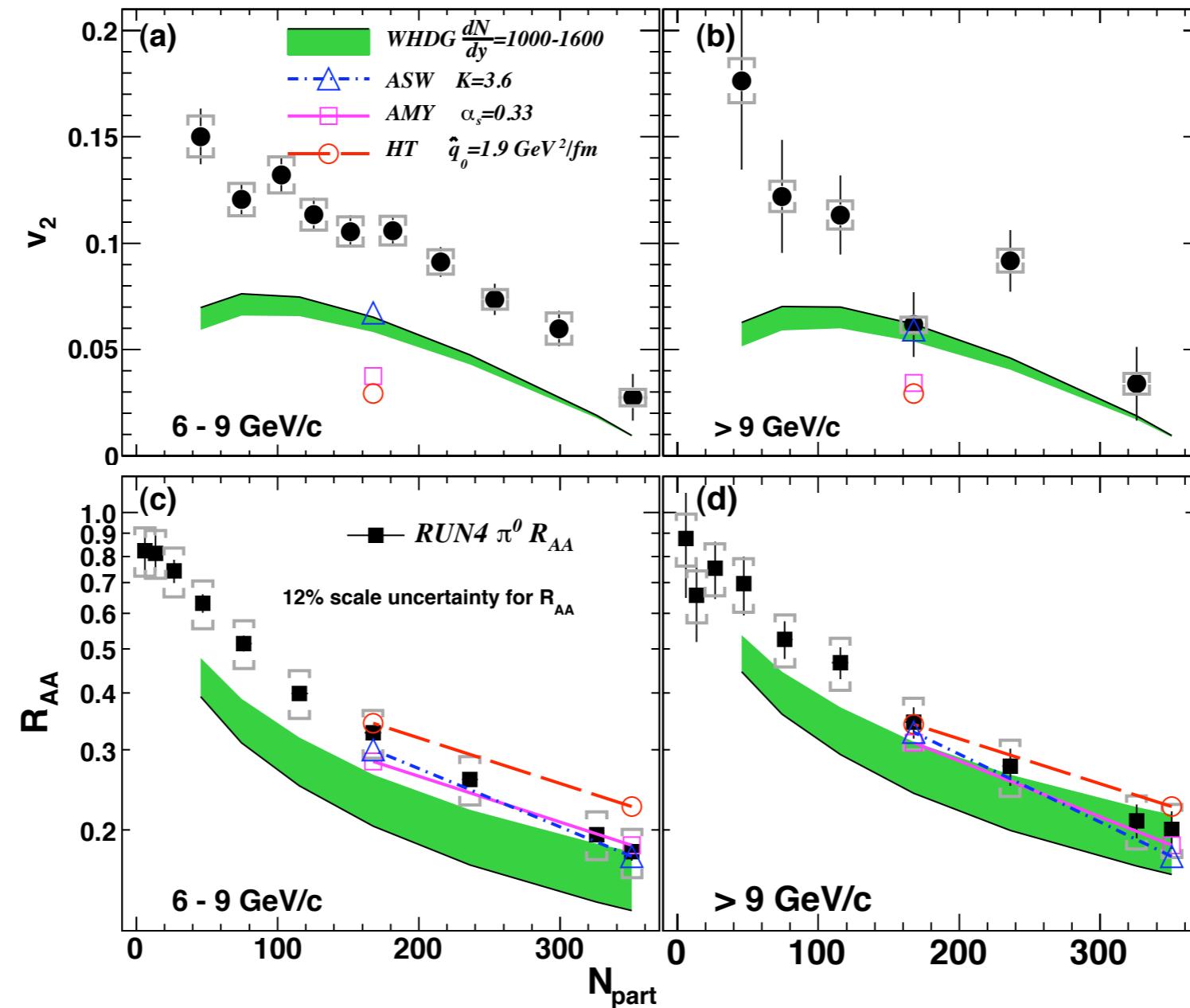


PHENIX: $R_{AA}(\text{jet}) = R_{AA}(\pi^0)$
small uncertainties

jet shape studies

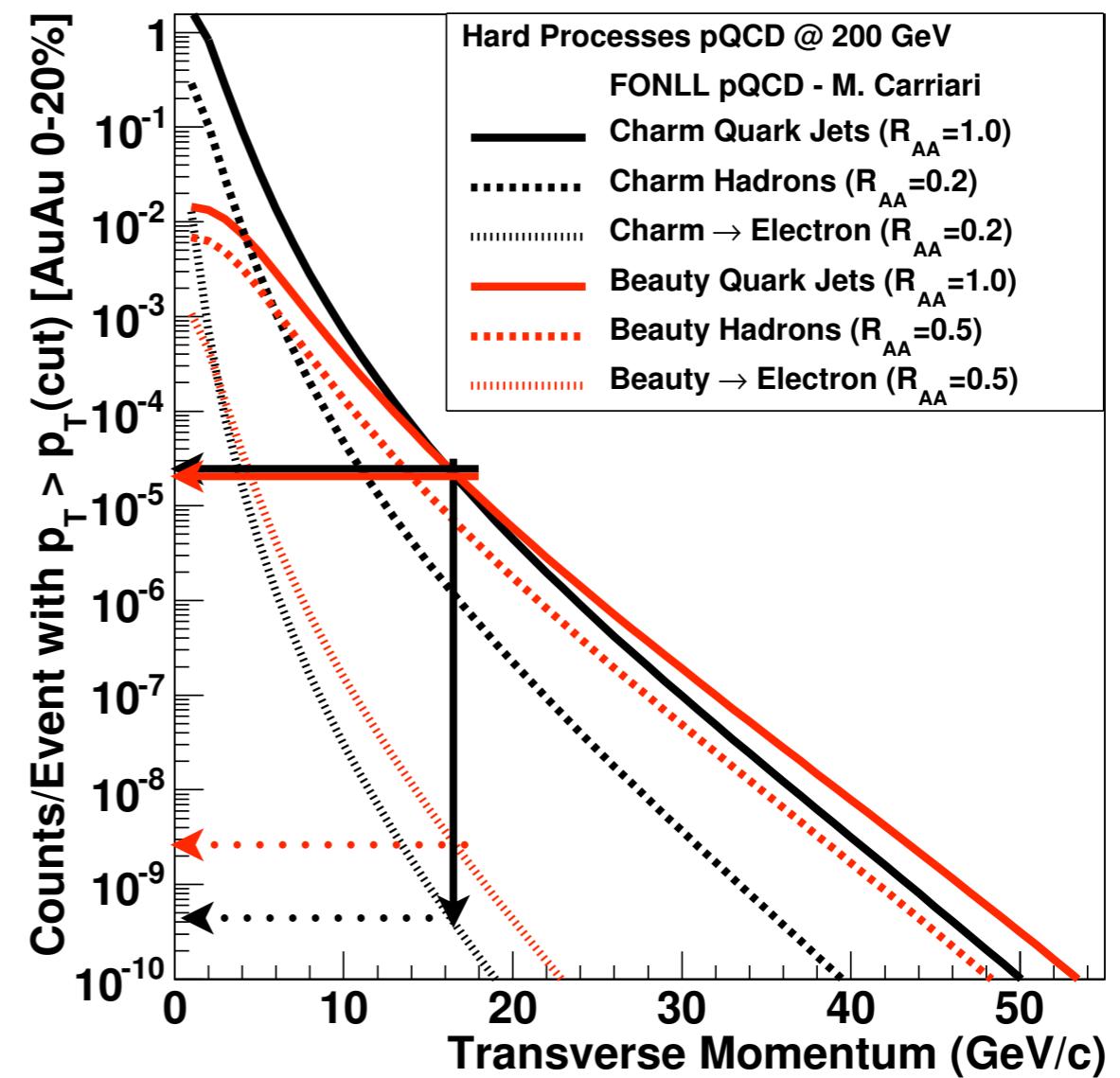
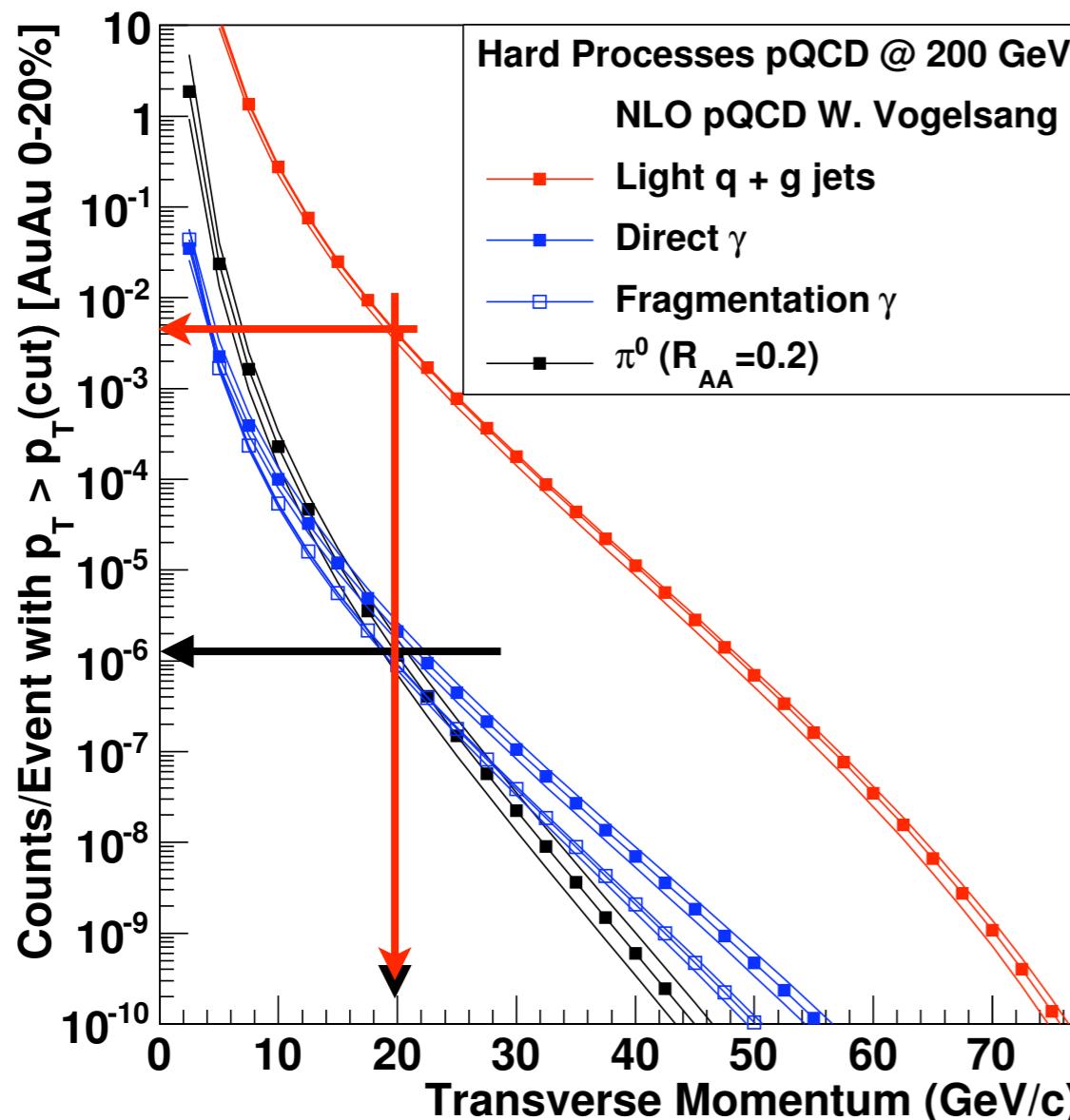


high pt

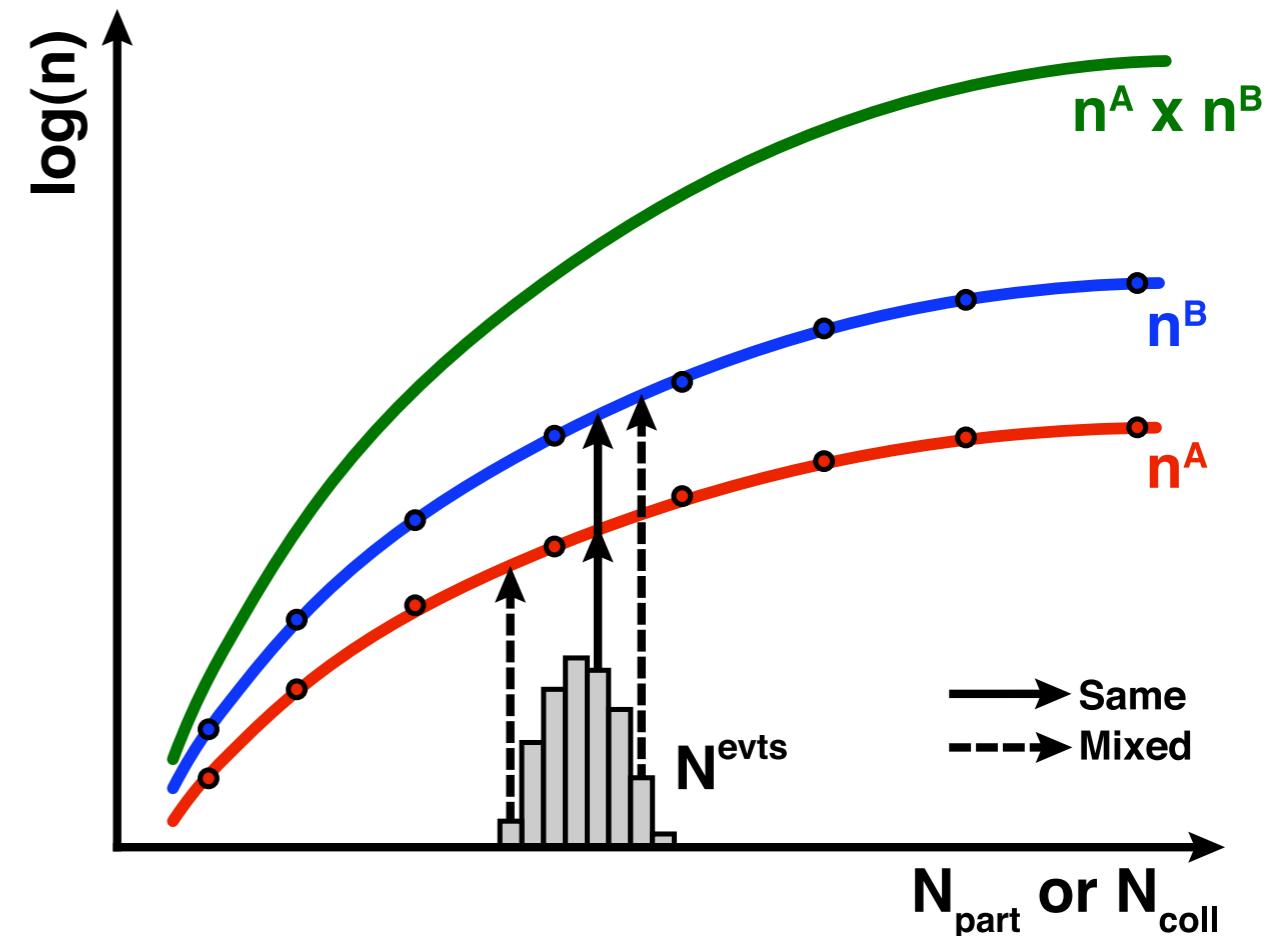


rate!

all hard physics at RHIC is statistics limited!

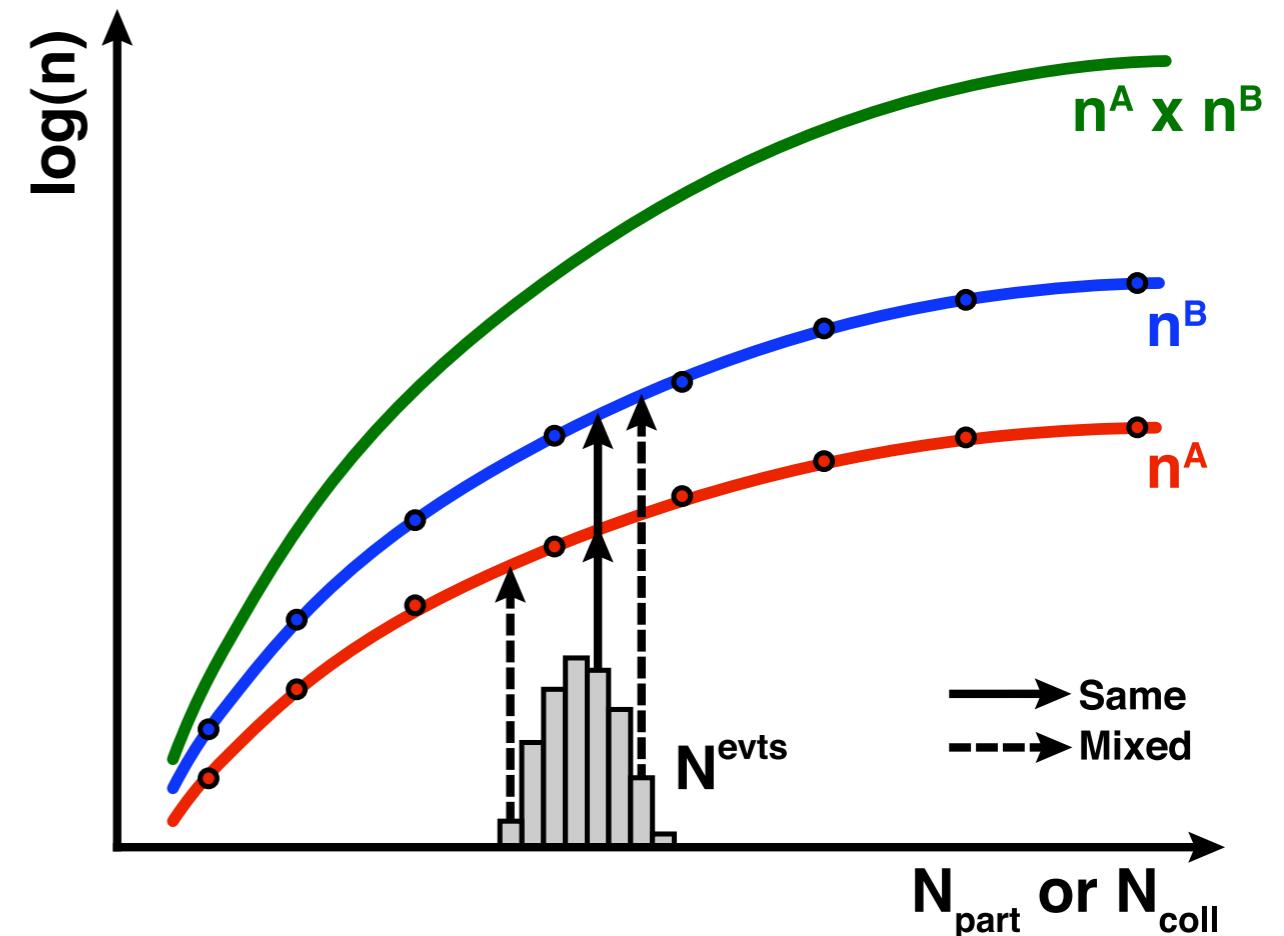


b_0 determination



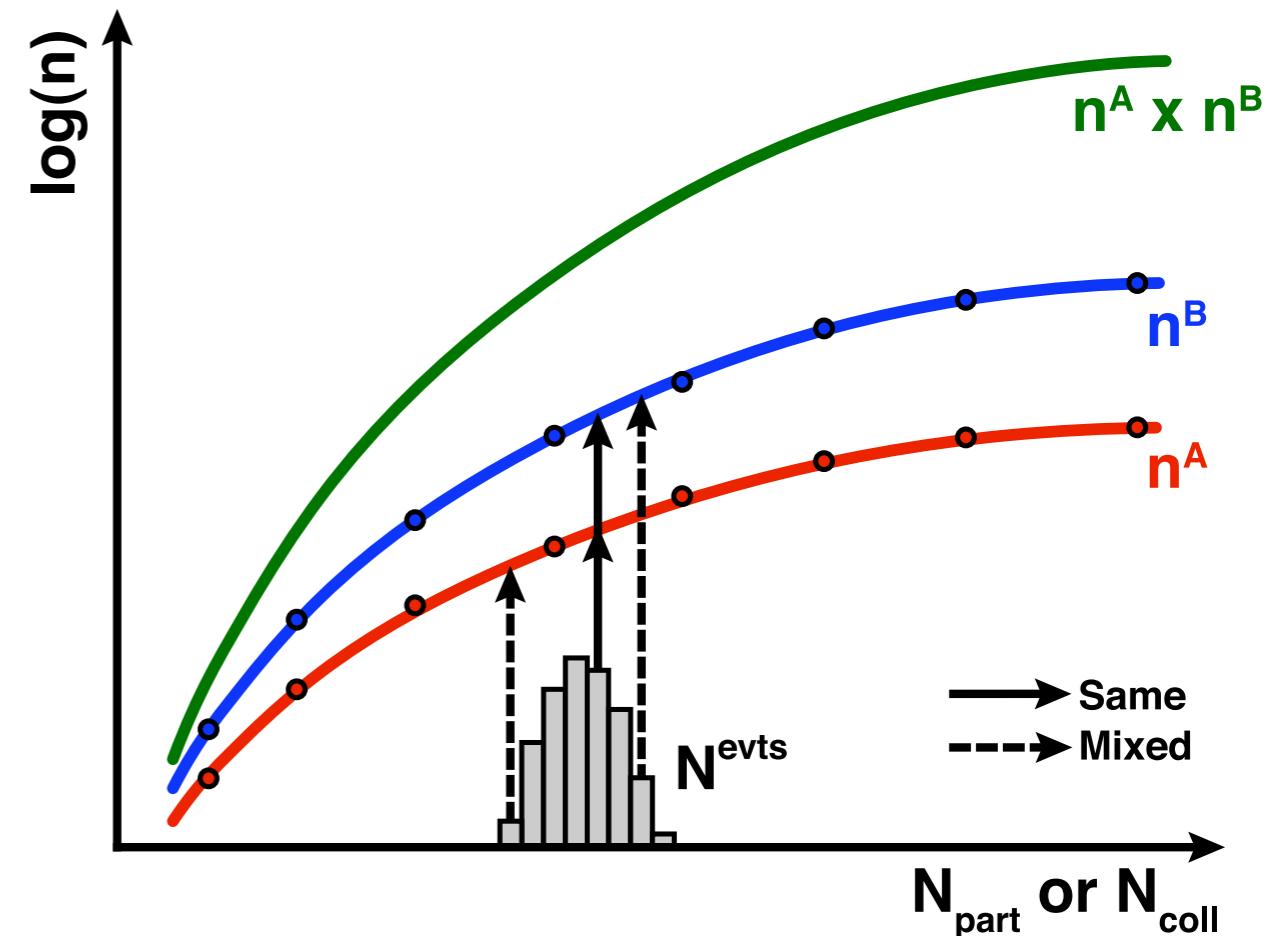
b_0 determination

- in general $b_0 \sim \langle n_{\text{trig}} \rangle \langle n_{\text{assoc}} \rangle$



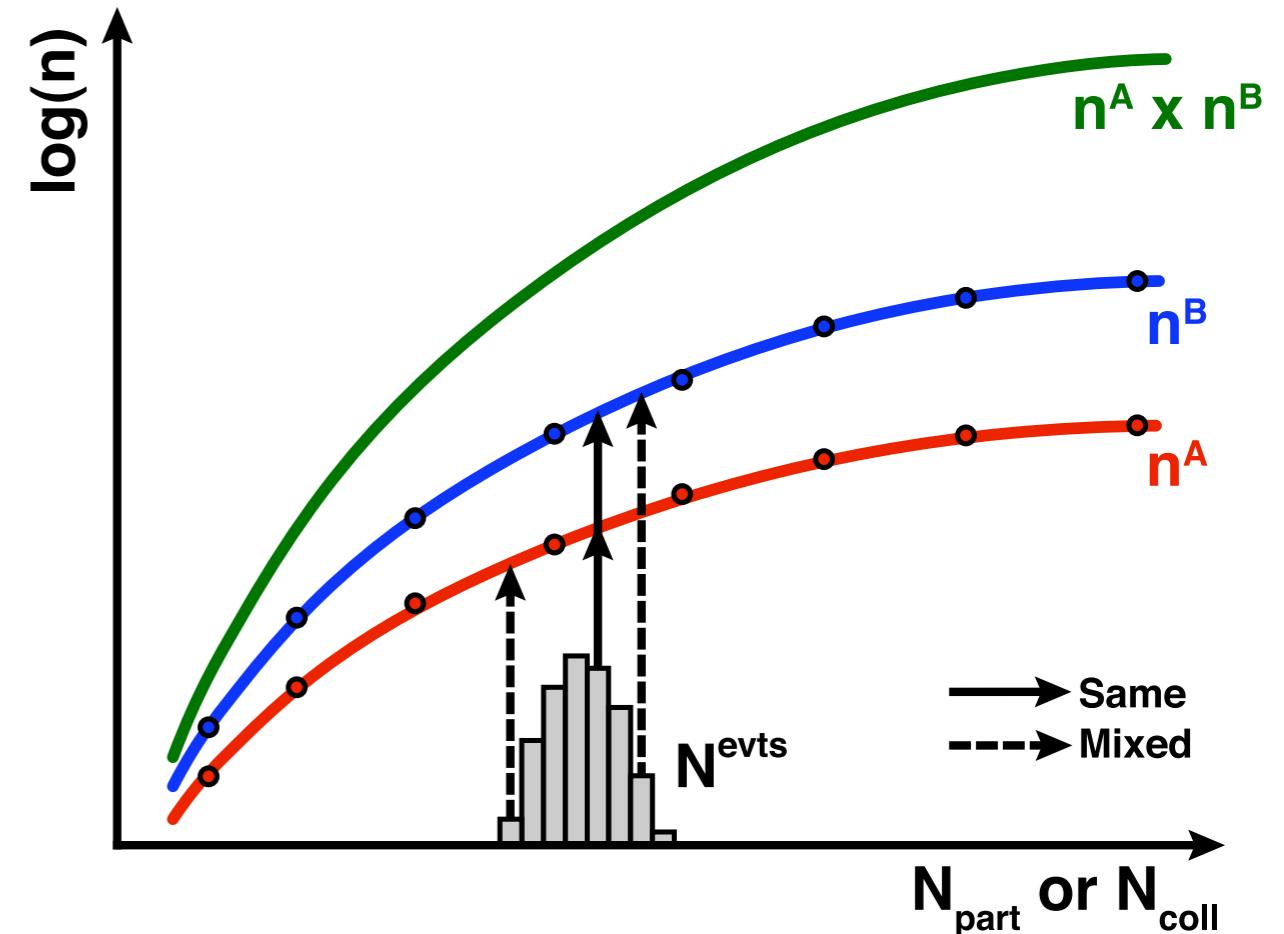
b_0 determination

- in general $b_0 \sim \langle n_{\text{trig}} \rangle \langle n_{\text{assoc}} \rangle$
- additional centrality dependent factor, ξ



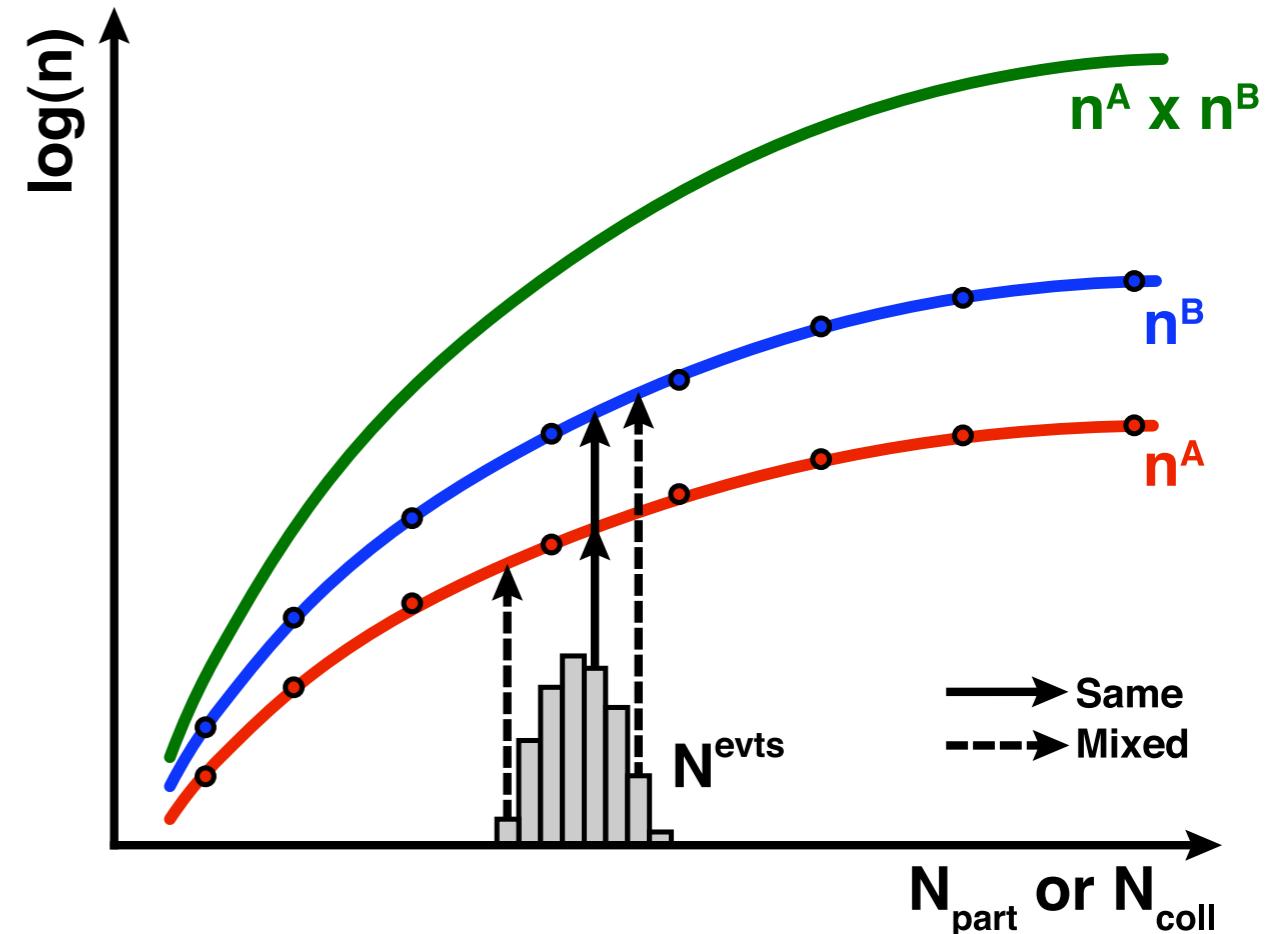
b_0 determination

- in general $b_0 \sim \langle n_{\text{trig}} \rangle \langle n_{\text{assoc}} \rangle$
- additional centrality dependent factor, ξ
- more central events contain more pairs



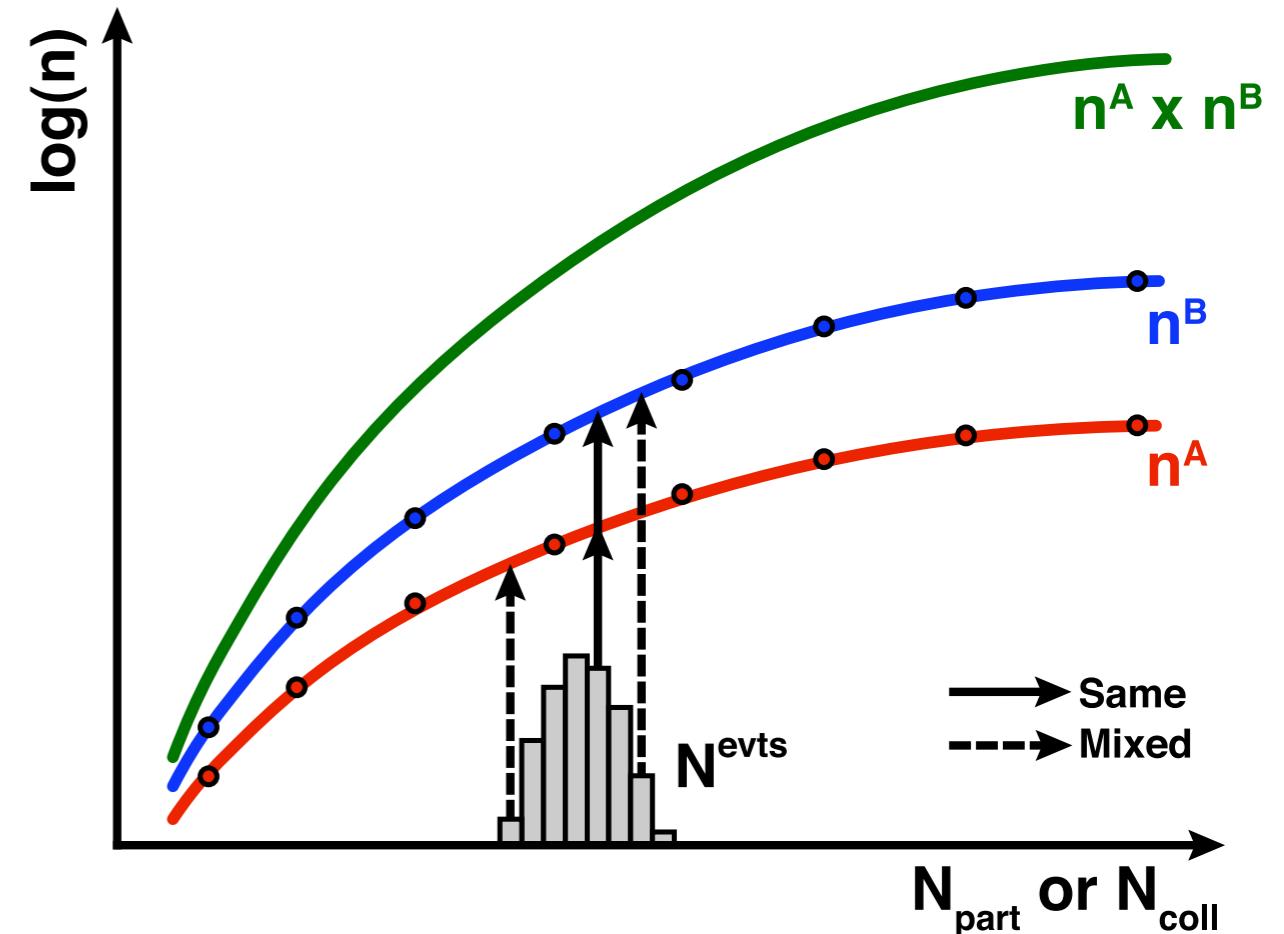
b_0 determination

- in general $b_0 \sim \langle n_{\text{trig}} \rangle \langle n_{\text{assoc}} \rangle$
- additional centrality dependent factor, ξ
 - more central events contain more pairs
- not new, used in



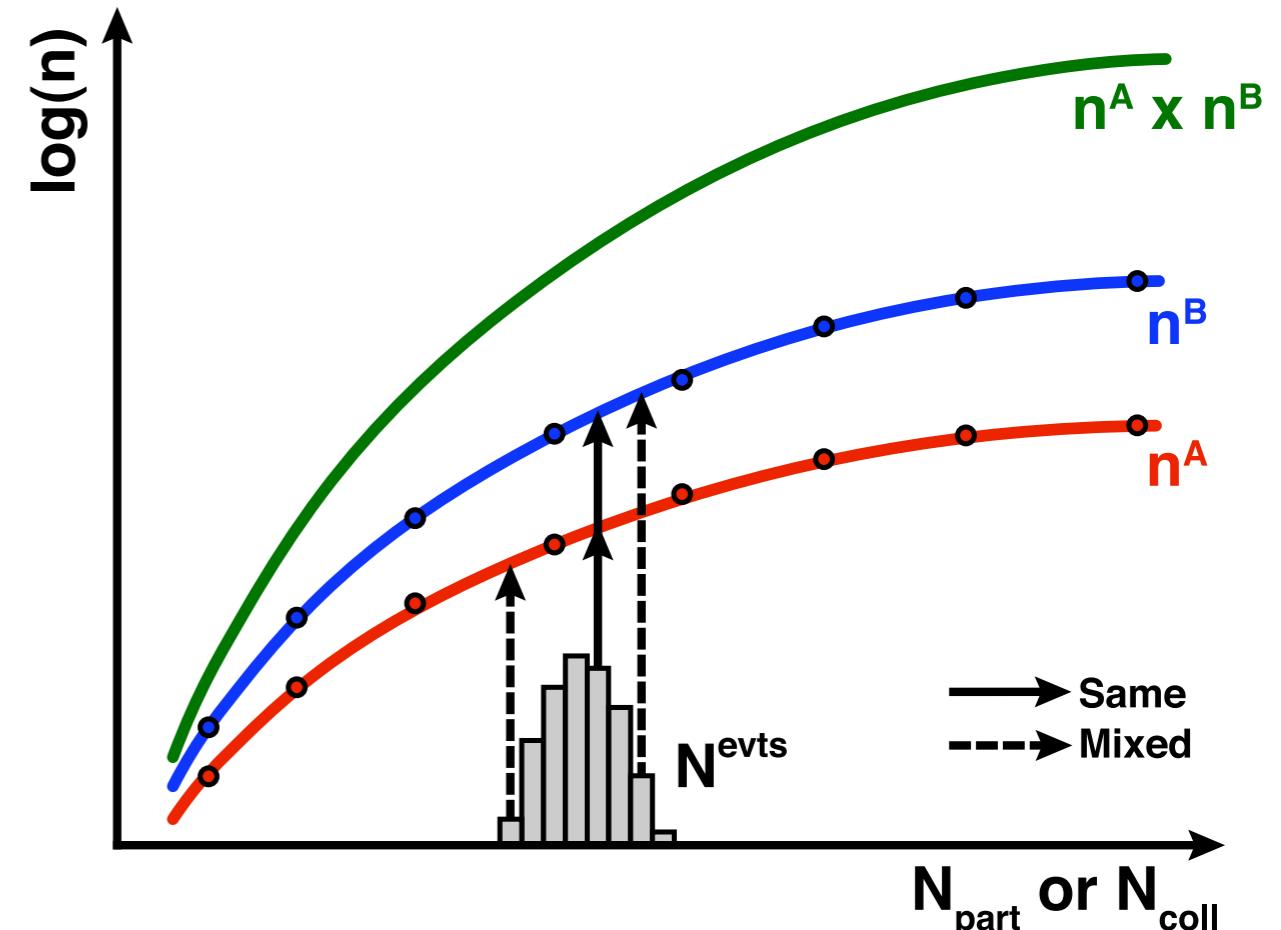
b_0 determination

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 - more central events contain more pairs
- not new, used in
 - PHENIX, PRC 71 051902



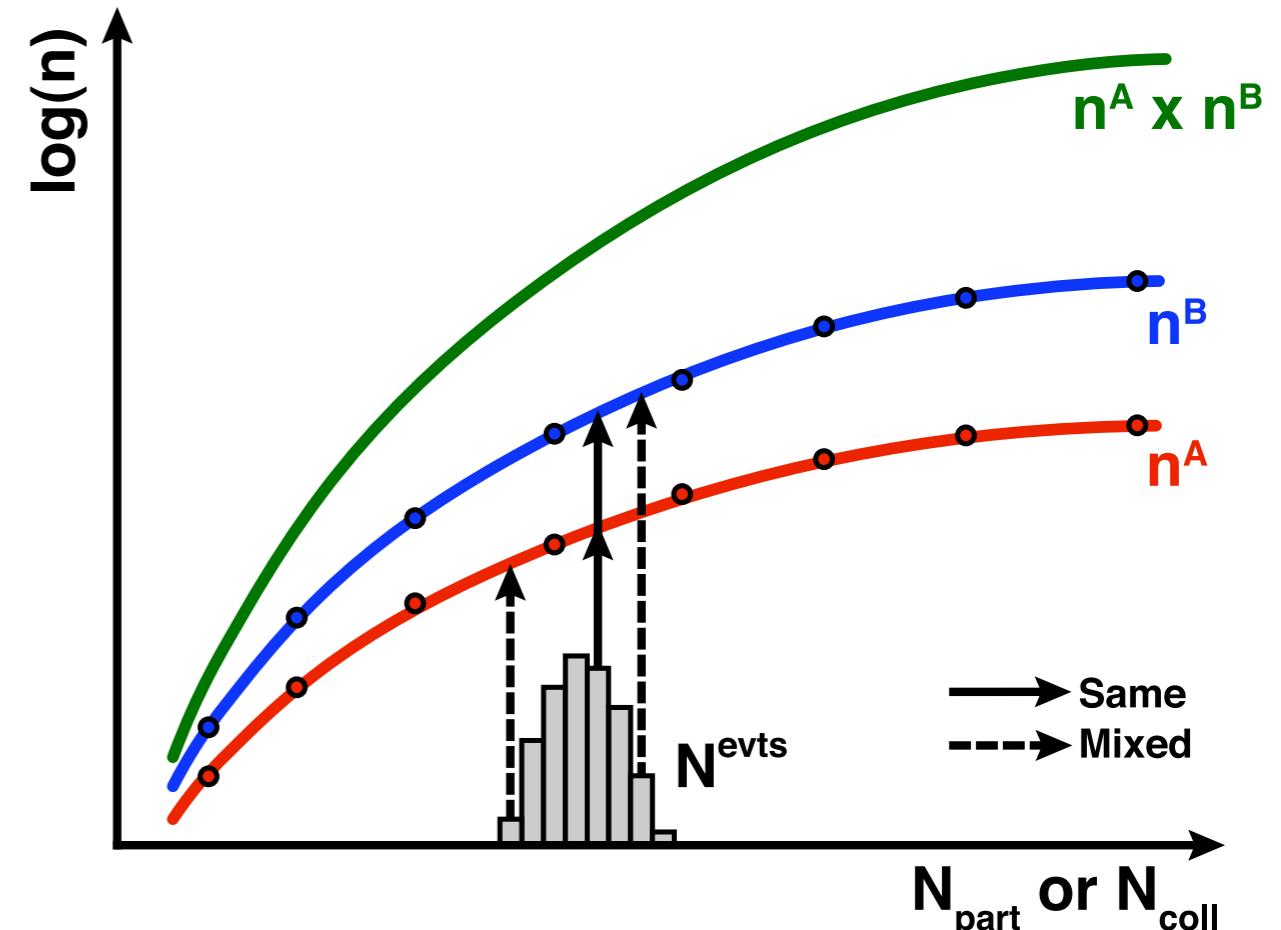
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 - PHENIX PRL 98 232302



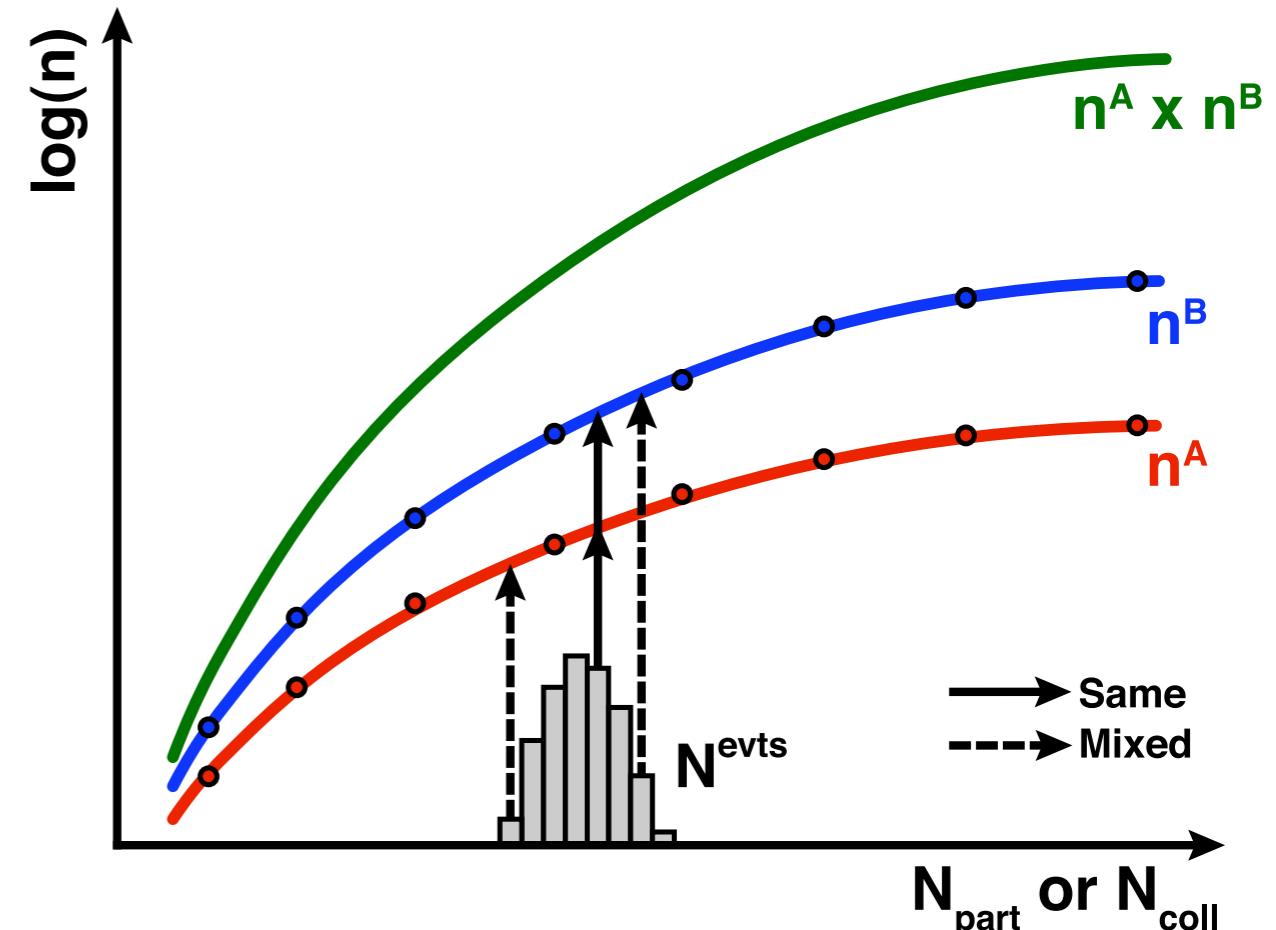
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 - PLB 649 359 (2007)



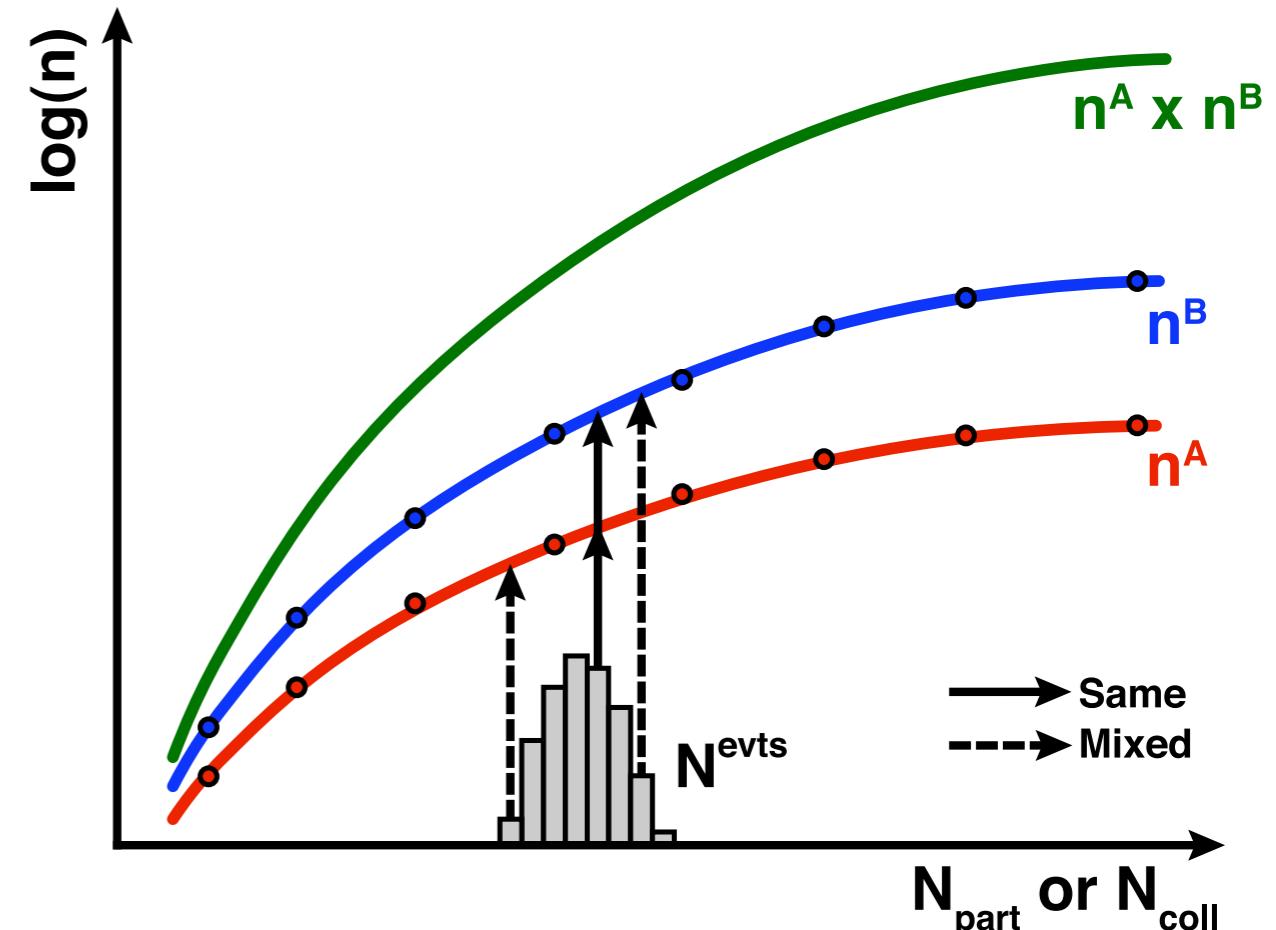
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 - PLB 649 359 (2007)
 - PHENIX PRC 80 024908



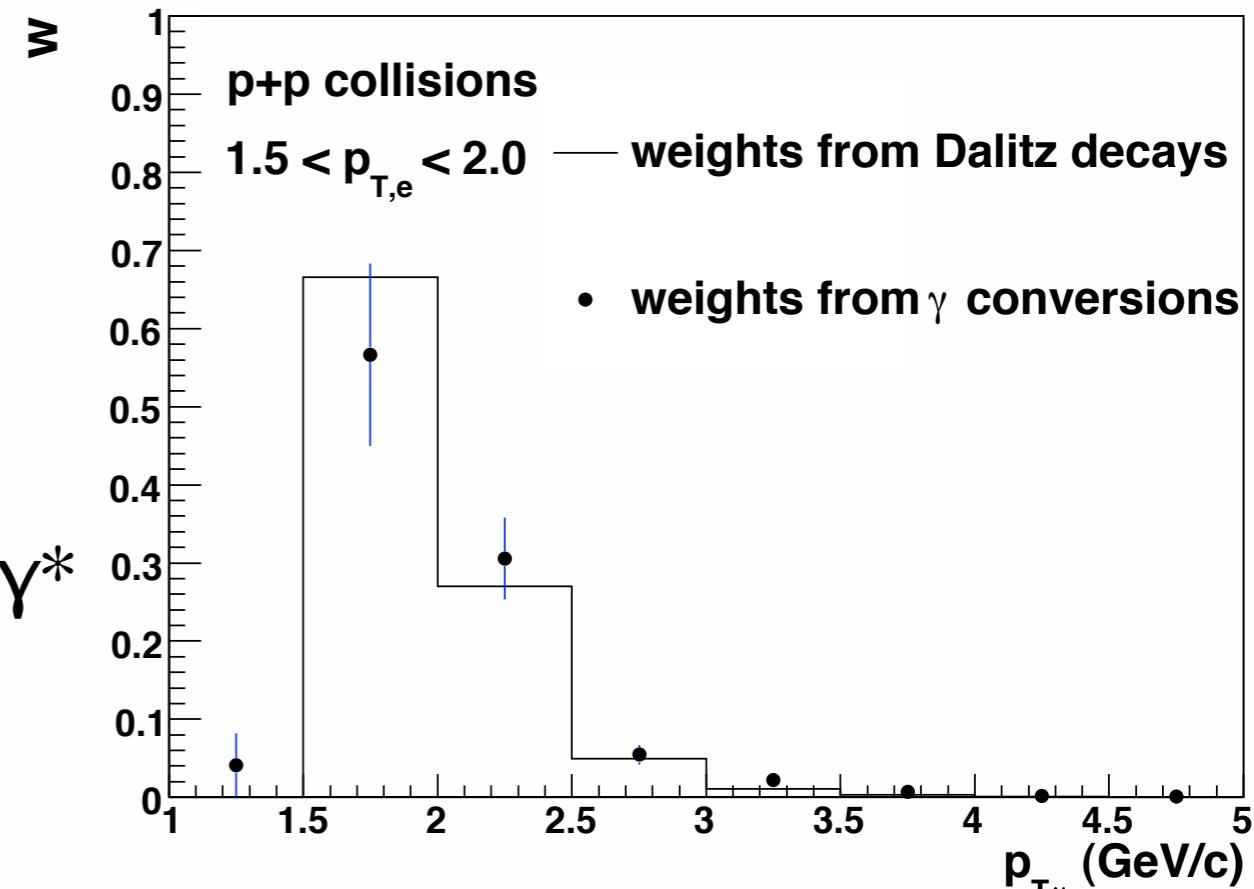
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 - PHENIX PRC 80 024908
 - PHENIX arXiv:1002.1077



e_{phot}-h correlations (II)

- $\gamma_{\text{inc}}(p_T) \rightarrow e_{\text{phot}}(p_T)$?
- **conversions**: $\gamma_{\text{inc}}(p_T) + \text{PHENIX}$
GEANT + reco. eff.
- **Dalitz decays**: $\pi^0(p_T) \rightarrow \gamma e^+ e^-$ get γ^* from $e^+ e^-$
- both methods: $e_{\text{phot}}(p_T) \sim \gamma_{\text{inc}}(p_T) \approx \pi^0(p_T)$
- π^0 spectrum falls very steeply



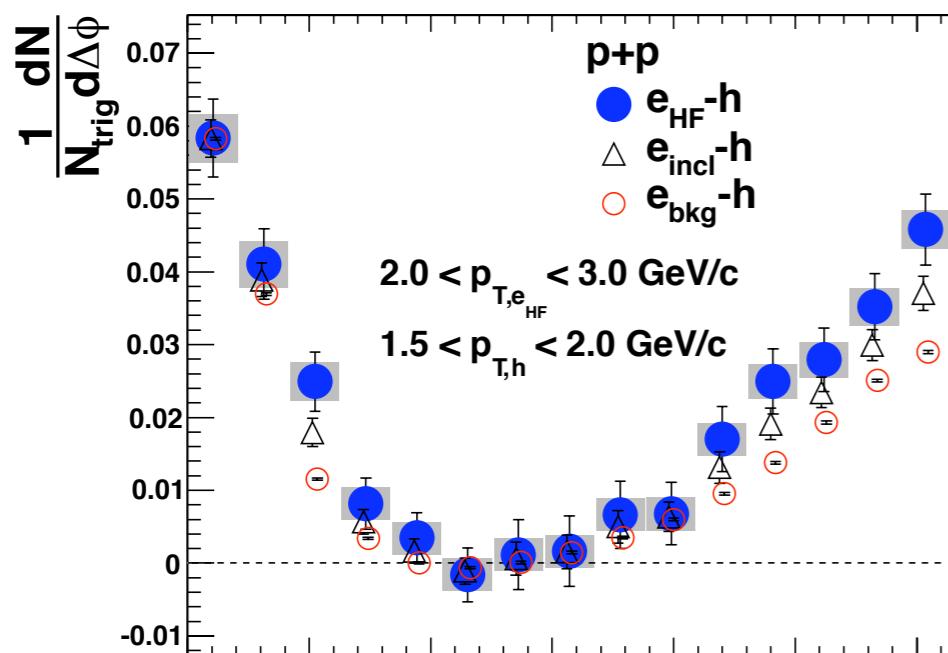
$$Y_{e_{\text{phot}}-h}(p_{T,i}) = \sum_j w_i(p_{T,j}) Y_{\gamma-h}(p_{T,j})$$

why heavy flavor?

- m_c & m_b large compared to Λ_{QCD} and T_i
- these quarks provide a partonic variation of the quark probing the matter
 - --fundamental handle
 - clean, production only in initial stages of the collision, before the matter is formed

moving to Au+Au collisions

moving to Au+Au collisions



moving to Au+Au collisions

